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A conveyor belt experimental setup to study the internal dynamics of granular avalanches

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Abstract This paper shows how a conveyor belt setup can be used to study the dynamics of stationary granular flows. To visualise the flow within the granu-lar bulk and, in particular, determine its composition and the velocity field, we used the refractive index matching (RIM) technique combined with particle track-ing velocimetry and coarse-graining algorithms. Implementing RIM posed varied technical, design and construction difficulties. To test the experimental setup and go beyond a mere proof of concept, we carried out granular flow experiments in-volving monodisperse and bidisperse borosilicate glass beads. These flows resulted in stationary avalanches with distinct regions whose structures were classified as: (i) a convective-bulged front, (ii) a compact-layered tail and, between them, (iii) a breaking size-segregation wave structure. We found that the bulk strain rate, represented by its tensor invariants, varied significantly between the identified flow structures, and their values supported the observed avalanche characteris-tics. The flow velocity fields' interpolated profiles adjusted well to a Bagnold-like profile, although a considerable basal velocity slip was measured. We calculated a segregation flux using recent developments in particle-size segregation theory. Along with vertical velocity changes and high expansion rates, segregation fluxes were markedly higher at the avalanche's leading edge, suggesting a connection between flow rheology and grain segregation. The experimental conveyor belt's results showed the potential for further theoretical developments in rheology and segregation-coupled models.

27 Keywords Refractive index matching · Granular flows · Particle-size segregation

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28 1 Introduction

Granular flows are often studied using steady-state experiments in long flumes with constant feed rates (e.g. MiDi, 2004; Delannay et al., 2017). Dam-break experiments, in which a finite volume of granular material is released down a slope, have also been performed (e.g. Savage and Hutter, 1989; Pouliquen, 1999; Gray and Ancey, 2009; Johnson et al., 2012; Saingier et al., 2016), but less frequently given the difficulty of capturing internal front dynamics. A convenient way to remove this difficulty is to create a steady granular avalanche on a conveyor belt (Davies, 1988, 1990). Conveyor belts have a mobile, rough bottom that drags materials from one place to another, and they are commonly used in industry (e.q.Dhillon, 2008; Pane et al., 2019). If a granular material flows under the effect of gravity while subject to a controlled drag that counterbalances the gravitational effect, the resulting flow should reach a steady state. Looking at this particular situation is then equivalent to moving a camera with the flow front in a dam-break experiment.

The internal dynamics of granular flows affect their propagation. For instance, their runout distance depends crucially on grain friction and composition (Linares-Guerrero et al., 2007; Roche et al., 2008; Iverson et al., 2010; Mangeney et al., 2010; Kokelaar et al., 2014), whereas self-generated internal structures such as levees (Deboeuf et al., 2006; Mangeney et al., 2007; Rocha et al., 2019) and breaking size-segregation waves (Gray and Ancey, 2009; Gajjar et al., 2016; van der Vaart et al., 2018) or reverse segregation (Thomas and D'Ortona, 2018) regulate the spread of the flow. Polydisperse granular materials are prone to separate themselves by particle size, in a process called particle-size segregation (Gray, 2018). In gravity-driven shallow granular avalanches, large particles are often encountered in the flow's leading edge and near the free surface, whereas small grains are more likely to be found in the tail and along the bottom (Gray and Thornton, 2005; Gray and Ancey, 2009; Johnson et al., 2012; Gray, 2018). To appropriately investigate the connection between flow and segregation, it is thus important to create the experimental conditions that make it possible to observe flows with well-defined fronts and subject to inversely-graded particle arrangements.

A better understanding of the link between the flow dynamics and internal structure of granular flows is central to modelling them. Experimentally, this understanding can be achieved by visualising and measuring flow characteristics within the granular bulk. Among the laboratory-scale methods used for studying granular flows, techniques based on refractive index matching (RIM) have been used increasingly in recent years (Budwig, 1994; Wiederseiner et al., 2011; Di-jksman et al., 2012; Sanvitale and Bowman, 2016; Poelma, 2020). Applying RIM to granular avalanches is fraught with difficulties, however. When the setup is not immersed, light-scattering (Byron and Variano, 2013), free-surface effects and bubbles (Cui and Adrian, 1997) are problematic. Immersing the whole setup in an index-matched fluid usually solves these problems, but this solution has the disadvantage of requiring large volumes of fluids in long inclined flumes (van der Vaart et al., 2018). Another difficulty common to RIM techniques is the limited number of fluid-grain combinations that come close to real-world magnitudes of fluid viscosity and density ratios (Wiederseiner et al., 2011; Dijksman et al., 2012). Since Davies (1988)'s pioneering experiments, conveyor belts have been used in-creasingly to study granular flows (Perng et al., 2006; Martínez, 2008; Marks et al.,

2017; van der Vaart et al., 2018). The articles by Marks et al. (2017) and van der Vaart et al. (2018) deserve special mention because of their focus on particle-size segregation. Marks et al. (2017) studied size segregation in stationary avalanches using a two-dimensional conveyor belt. One drawback of this configuration is that it leads to flow features that are not observed in three dimensional configurations, i.e., significant sidewall effects, convection cells and reduced percolation of the finest grains (Thomas and Vriend, 2019; Trewhela et al., 2021b). van der Vaart et el. (2018) for the dimensional configuration is developed to the set of the s

et al. (2018) found mobility-feedback dynamics similar to those of (Marks et al.,
2017), but using a three-dimensional conveyor belt.

This paper presents an experimental three-dimensional setup based on a con-veyor belt and RIM techniques that we used to study stationary granular avalanches. The setup was an enhanced version of the prototype built by van der Vaart et al. (2018). During their preliminary experiments, van der Vaart et al. (2018) iden-tified various technical difficulties requiring solutions. This work describes these problems and how we solved them. We then conducted experiments using sets of monodisperse and bidisperse granular media to investigate the dynamics of stationary granular avalanches. We provide a qualitative and quantitative picture of these avalanches by showing their bulk compositions, velocity profiles, strain-rate tensor invariants and segregation fluxes.

5 2 Theoretical framework

5 2.1 Granular flow equations

⁹⁷ We consider a conveyor belt inclined at θ to the horizontal, creating a stationary ⁹⁸ avalanche. We assume that in this flow configuration, the granular avalanche can ⁹⁹ be decomposed into a steady uniform layer and a leading edge. The momentum ¹⁰⁰ balance equation for the uniform layer is

$$\frac{\mathrm{d}\tau_{xz}}{\mathrm{d}z} = -\varrho g \mathrm{sin} \ \theta,\tag{1}$$

$$\frac{\mathrm{d}\sigma_z}{\mathrm{d}z} = \varrho g \mathrm{cos} \,\theta,\tag{2}$$

where τ_{xz} is the shear stress, τ_z is the normal stress in the z-direction, and ρ denotes the bulk density. The x-direction is aligned with the bottom and the the z direction is normal to the bottom. We assumed a stress-free condition at the free surface z = h. Integrating Eqs. (1) and (2) leads to the well-known shear and normal stress distributions that hold independently of the bulk's constitutive equations:

$$\tau_{xz}(z) = \varrho g \sin \theta \ (h-z), \tag{3}$$

$$\sigma_z(z) = -\varrho g \cos \theta \ (h-z). \tag{4}$$

For granular flows in a frictional-collisional regime, bulk stresses are generated by collisional and frictional contacts between particles. Ancey and Evesque (2000) argued that for this regime to hold, the constitutive equation should depend on a

dimensionless number that reflects the balance between these antagonistic contact forces

$$I = \frac{\dot{\gamma}d}{\sqrt{\sigma_z/\varrho}},\tag{5}$$

where $\dot{\gamma} = |du/dz|$ is the shear rate and d is the particle diameter. This dimensionless number was subsequently renamed inertial number (MiDi, 2004). By compiling experimental data, Jop et al. (2006) deduced a generalized Coulomb relationship called the $\mu(I)$ rheology: $\tau_{xz} = \mu(I)\sigma_z$, where μ denotes the bulk friction coefficient. Under steady uniform flow conditions, Eqs. (3) and (4) also impose that $\tau_{xz}/\sigma_z = \tan \theta$, and thus $\mu(I) = \tan \theta$. Inversing this condition leads to the following expression of the inertial number I for a given slope θ :

$$I = I_0 \frac{\tan \theta - \mu_1}{\mu_2 - \tan \theta} \tag{6}$$

¹¹⁹ where I_0 , μ_1 and μ_2 are empirical parameters. This equation implies that a steady ¹²⁰ uniform flow can be achieved with a limited range of inclinations: $\mu_1 < \tan \theta < \mu_2$ ¹²¹ (MiDi, 2004). This expression along with Eq. 5 and the basal velocity condition ¹²² $u_0 = u_b$ (where u_b denotes the belt velocity) yields a Bagnold-like velocity profile

$$u(z) = -u_b + \frac{2I\sqrt{g\cos\theta h^3}}{3d} \left(1 - \left(1 - \frac{z}{h}\right)^{3/2}\right).$$
 (7)

This velocity profile is characteristic of steady uniform granular flows of monodisperse grains (Silbert et al., 2001; Mitarai and Nakanishi, 2005). When granular flows involve polydisperse materials, they may exhibit a different velocity profile due to segregation-induced grain rearrangement (Tripathi and Khakhar, 2011).

127 2.2 Size segregation equations

The internal composition of the stationary granular avalanches can be studied in
terms of particle movement and size segregation by using a continuum approach.
For a bidisperse granular mixture of grains of different diameters, the volumetric
concentrations of the particle species satisfy

$$\sum_{\nu} \phi^{\nu} = 1, \tag{8}$$

where ϕ^{ν} is the partial volume fraction for each grain species $\nu = \{s, l\}$, which is characterized by a diameter d_{ν} . The bidisperse size segregation equation for the ν species is then given by (Gray, 2018):

$$\frac{\partial \phi^{\nu}}{\partial t} + \nabla \cdot (\phi^{\nu} \boldsymbol{u}) + \nabla \cdot \boldsymbol{F}^{\nu} = \nabla \cdot (\mathcal{D}_{sl} \nabla \phi^{\nu}), \qquad (9)$$

where u is the bulk velocity and $F^{\nu} = f_{sl}\phi^s \phi^l g/|g|$ are the segregation fluxes, which are oriented with the direction of gravity and satisfy:

$$\sum_{\nu} \boldsymbol{F}^{\nu} = 1. \tag{10}$$

$$\boldsymbol{u}^{l} - \boldsymbol{u} = -f_{sl}(\boldsymbol{\phi}^{s})\boldsymbol{\phi}^{l}, \tag{11}$$

$$\boldsymbol{u}^{s} - \boldsymbol{u} = f_{sl}(\phi^{s})\phi^{s}, \qquad (12)$$

where f_{sl} corresponds to the theoretical segregation flux function for large and small particles. This function has been proposed to be cubic (Bridgwater et al., 1985), quadratic (Dolgunin and Ukolov, 1995), asymmetric (Gajjar and Gray, 2014; van der Vaart et al., 2015) and highly non-linear (Trewhela et al., 2021a). The asymmetric nature of the size segregation phenomenon is highly significant: small particles segregate faster than their large counterparts. This asymmetry has been observed in numerical simulations and laboratory experiments (Gajjar and Gray, 2014; van der Vaart et al., 2015; Jones et al., 2018; Trewhela et al., 2021a). The experimental results presented in this paper used a coarse-graining tech-nique to infer the continuous distributions of the bulk density ρ , partial con-centrations ϕ^{ν} and velocity fields u from particle positions r_i and velocities u_i determined experimentally (e.g., Goldhirsch, 2010; Tunuguntla et al., 2016) (see §3.3 for further information). The velocity fields for each species u^{ν} were also com-puted. Based on these computations and following the recent work of Trewhela et al. (2021a), we defined f_{sl} as

$$f_{sl} = \mathcal{B} \frac{\varrho_* g \dot{\gamma} d^2}{\mathcal{C} \varrho_* g d + p} \mathcal{F}(R, \phi^s), \tag{13}$$

where $\mathcal{B} = 0.3744$ and $\mathcal{C} = 0.2712$ are two constants determined from segregation experiments in a three-dimensional shear box. \mathcal{F} is a function that depends mostly on the size ratio $R = d_l/d_s$, for intermediate values of ϕ^s , and will be considered to be equal to R-1. $\dot{\gamma}$ is the shear rate, $d = d_s \phi^s + d_l \phi^l$ is the concentration-averaged diameter and $p = \varrho_* g \Phi(h-z) \cos \theta$ is the pressure, considered to be lithostatic for a flow of height h. An expression for d as a function of ϕ^s was then derived:

$$d = Rd_s \left(1 - \left(1 - \frac{1}{R} \right) \phi^s \right) = Rd_s d_\phi.$$
(14)

¹⁶¹ By inserting the latter into Eq. (13), we determined a simplified segregation flux ¹⁶² function

$$f_{sl} = \mathcal{B} \frac{\dot{\gamma} (Rd_s d_\phi)^2}{\mathcal{C} Rd_s d_\phi + \Phi(h-z) \cos \theta} (R-1).$$
(15)

The shear rate calculation, which involved the strain-rate tensor invariants, is detailed in the next subsection.

The expression proposed by Trewhela et al. (2021a) was developed from experiments (in a three-dimensional shear box) to account for the asymmetric nature of size segregation. The expression's segregation timescale was set by the shear rate and depended on the size difference R and pressure distribution p. Their expression has also been used in numerical simulations (Barker et al., 2021) and validated for two-dimensional experiments (Trewhela et al., 2021b).

171 2.3 Strain-rate tensor invariants

172 Based on the velocity field u, the strain-rate tensor is defined as

$$\boldsymbol{D} = \frac{1}{2} (\nabla \boldsymbol{u} + (\nabla \boldsymbol{u})^T), \tag{16}$$

where T denotes the transpose. The strain-rate tensor's first invariant, also called the expansion rate, can be calculated as

$$I_{\boldsymbol{D}} = \operatorname{tr}(\boldsymbol{D}) = \boldsymbol{\nabla} \cdot \boldsymbol{u}. \tag{17}$$

A tensor decomposition determines the deviatoric strain-rate tensor $S = -\frac{1}{2}I_D \mathbf{1} + D$, which is useful for calculating the strain-rate tensor's second invariant:

$$II_{\boldsymbol{D}} = \left(\frac{1}{2}\mathrm{tr}(\boldsymbol{S}^2)\right)^{1/2},\tag{18}$$

¹⁷⁷ where $\dot{\gamma} = 2II_D$. Throughout this paper, mentions of or discussions on the shear ¹⁷⁸ rate refer to the strain-rate tensor's second invariant.

¹⁷⁹ **3** Materials and techniques

180 3.1 Refractive index matching

Most granular materials are opaque, and in most experimental facilities, this prop-erty restricts any inspection of them to their boundaries. Even when grains are transparent, refractive index differences between the interstitial medium and the grain material impedes observation within the granular bulk. To overcome such natural restrictions, it is desirable to match the refractive indices of the granular material and the interstitial fluid. Furthermore, using laser-induced fluorescence, light can be shone through the bulk, making the grains appear as dark shapes. This technique is possible in a laboratory environment if the fluid temperature is stable (as its refractive index retains a known value). This is called refractive index matching (RIM) and has been used not only to study granular flows but also other fluids (Budwig, 1994; Li et al., 2005; Wiederseiner et al., 2011; Dijksman et al., 2012; Bai and Katz, 2014; Clément et al., 2018; Rousseau and Ancey, 2020).

The present study used a RIM mixture composed of borosilicate glass beads immersed in a fluid solution of ethanol and benzyl alcohol. Their refractive in-dices n_r , densities ρ_* and suppliers are detailed in Table 1. Two additional RIM mixtures were considered for this study but rejected due to their interstitial-fluid properties. The first alternative was a combination of Triton X-100 fluid and poly (methyl methacrylate) particles (PMMA) (for details on this combination, see Dijksman and van Hecke, 2010; Wiederseiner et al., 2011; Dijksman et al., 2012). This was rejected due to the fluid's high viscosity ($\eta = 270$ cP) and the low den-sity difference between the particles and the fluid, $\varrho' = (\varrho_p - \varrho_f)/\varrho_p = 0.102$. The second was a combination of an aqueous sodium iodide solution (for studies using this combination, see Narrow et al., 2000; Bai and Katz, 2014; Clément et al., 2018) and borosilicate glass beads, but the interstitial fluid was too dense and the beads showed positive buoyancy. Finally, we retained borosilicate glass

Table 1 Refractive indices n_r , intrinsic densities ρ_* and suppliers of the materials used for our RIM experiments.

Material	n_r	ϱ_*	Supplier
Borosilicate glass Benzyl alcohol Ethanol	$1.4726 \\ 1.5396 \\ 1.3656$	$2.23 \\ 1.044 \\ 0.789$	Schäfer Glas Acros Organics Fisher Scientific

for the particles and a mixture of ethanol and benzyl alcohol for the interstitial fluida combination recently used by van der Vaart et al. (2015) and Rousseau and Ancey (2020). The mixture's viscosity was close to that of water: $\eta \approx 3$ cP. The density contrast between the borosilicate and the fluid mixture was negative and sufficient to replicate the physics of wet granular flows $\varrho' \approx 1.34$.

The beads' refractive index $n_r = 1.4726$ (Tab. 1) was initially matched using 35 parts ethanol and 65 parts benzyl alcohol by weight (Chen et al., 2012). We then tuned the mixture's refractive index by adding small volumes of either ethanol or benzyl alcohol until the precise index was obtained. The n_r was constantly mea-sured during this adjustment stage using a Atago RX 5000 α refractometer in a 20 °C temperature-controlled environment. It was impossible to reduce uncertainties below $\pm 2\times 10^{-4}$ because of the large volume of fluid required for our experiments (about 40 L). Although this large volume was mixed using a motorized mixer, it was difficult to obtain a perfectly homogeneous mixture. Furthermore, the mix-ing process caused some ethanol to evaporate, leading to a slight mismatch in the fluid's refractive index and the formation of bubbles that enhanced the evaporated ethanol's carriage to the surface.

223 3.2 Image acquisition

The RIM technique is often combined with laser-induced fluorescence (Sanvitale and Bowman, 2012, 2016). When used alone, RIM produces a transparent medium, and it is impossible to distinguish between the fluid and solid phases. By mixing a fluorescent dye into the fluid and exciting it using a laser sheet, the solid phase can be made visible to a given light wavelength. For our experiments, we mixed our RIM fluid with a small amount of Rhodamine 6G (Acros Organics) and used a 4W Viasho laser with a $\lambda = 532$ nm wavelength (green) to produce the laser sheet. When filmed, particles then appeared as black circles. We used a Basler A403k camera mounted with a 28-mm Nikon lens, operated at a fixed rate of 40 frames per second for all experiments; image resolution was of 2352×600 pixels.

²³⁴ 3.3 Particle tracking and coarse-graining

Image sequences were analysed using circle identification and particle tracking algorithms. The imfindcircles algorithm included in Matlab was used to distinguish the various-sized circles. Particles' positions were determined over image sequences and then correlated using the tracking algorithm developed by Crocker and Grier (1996) to obtain particle trajectories $r_i(x, z, t)$ over time, and particle velocities $u_i(x, z, t)$.



Fig. 1 Diagram of the conveyor belt setup. The enclosed aluminium flume (centre) is closed off by a rectangular windowed lid that allows the passage of the laser sheet from above. A rough belt made from 300 independent pieces of POM circulates around the flume, guided via grooves in its front and back aluminium walls. The slope control (left) sets the vertical position of the flume's uphill end, with its downhill end attached to a sliding chariot where the fluid pump rests (right). Conveyor belt velocity u_b is controlled electronically (centre). Image were acquired using a Basler A403k camera placed in the front of the flume and equipped with a Nikon 28-mm lens and a 532-nm filter. A movie showing the operation of the conveyor belt is available online.

One recurring difficulty in studying granular flows involves transforming dis-crete information into continuous profiles or fields an indispensable step for com-paring experimental data and the predictions from continuum models. To over-come this problem, coarse-graining techniques have been developed to convolute discrete experimental and numerical results into continuum fields (e.g. Weinhart et al., 2012; van der Vaart et al., 2015; Tunuguntla et al., 2016). The advantages of coarse graining are numerous (Goldhirsch, 2010), for example: (i) it is possible to obtain continuous, smooth, differentiable fields and profiles, which is a particu-larly helpful feature close to the boundaries; and (ii) the fields derived satisfy both mass and momentum conservation equations (provided that the coarse-graining functions are differentiable and integrable). Our experimental analysis, we used a fourth-degree Lucy polynomial (Lucy, 1977) previously used in the post-analysis of discrete particle simulations (Tunuguntla et al., 2016).

²⁵⁴ 4 The experimental conveyor belt setup

We designed and built a conveyor belt flume to study stationary granular flows (see Fig. 1). The setup included an aluminium flume 141 cm long, 14 cm wide and 42 cm high. A sealed rectangular panel with a glass window was placed on top allowing the laser attached to the setup to create a laser sheet perpendicular to it. Two grooves carved in the flume's front and back aluminium panels guided the longitudinal movement of the rough conveyor belt made up of 300 independent

pieces and around four transversal aluminium rollers, with one pair located at each end of the aluminium flume. Each roller pair was arranged vertically to create walls that confined the granular material to the conveyed volume over the belt's moving parts. The conveyed volume was 104 cm long, 10 cm wide, and 15 cm high. The aluminium flume had a glass window in the sidewall, parallel to the flow and compatible with image acquisition and the visualisation of the entire conveyed volume. A mixer was located behind the pair of rollers at each end of the flume's aluminium structure to homogenise fluid. Various valves, beneath and above the setup, helped the processes of filling and emptying it.

An analogue electro-mechanical system set the flume's slope by vertically adjusting the flume's uphill end. The flume's downhill end (fixed to a mobile cart) moved simultaneously in the horizontal direction. The slope could be adjusted to a wide range of values. Gentle or very steep slopes were inadvisable and impractical because particles might overflow the upper rollers and create mechanical issues.

Each independent piece of the rough belt was a half-cylinder of polyoxymethylene (POM) screwed to an aluminium band. Roughness could be changed easily by replacing the POM half cylinders. For our experiments, we used a uniform roughness given by half cylinders of 4 mm in radius. Pieces were inserted into the grooves, next to each other, and were kept in place by the compression that the pieces applied against each other and were restrained vertically by the grooves.

The conveyor belt was operated using a motor located behind the setup. The motor rotated the bottom uphill roller, whose geared wheel pushed the POM pieces along between the grooves in the sidepanels. Half of the pieces had two bolts beneath them so that the geared wheel could push against them and, move the belt. Pieces were alternately bolted and non-bolted to avoid breaking the geared wheel, the roller or the POM pieces. Motor speed was controlled using a dimmer switch that could apply a continuous range of belt velocities u_b . The analogue controller did not give the u_b value directly, and it had to be measured using a sensor that counted the motor axis revolutions as a function of time. These revolutions were then easily translated to a precise u_b value using the radius of the geared wheel.

The final setup was the outcome of a long, iterative process, which resulted in complex machinery that may be difficult to replicate. Although numerous difficulties which arose during the construction were successfully solved, we failed to solve all of them (for other setup-related issues, see §7).

²⁹⁶ 5 Experimental dataset

²⁹⁷ The conveyor belt was used to study the internal dynamics of granular flows made ²⁹⁸ of monodisperse or bidisperse media. Conveyor belt velocity and slope were ad-²⁹⁹ justed so that stationary avalanches could be observed in the flume. Experiments ³⁰⁰ were thus characterised by the slope θ and belt velocity u_b (see Tab. 2). All the ³⁰¹ experiments presented here were carried out with the flume inclined at $\theta = 15^{\circ}$ to ³⁰² the horizontal.

Two experiments were initially carried out using monodisperse beads to determine a base state for later comparison with bidisperse experiments. The granular material used for these two runs was a 6-kg bulk of borosilicate beads of either $d_s = 6$ or 8 mm diameter (see Experiments 1 and 6 in Tab. 2). We determined



Fig. 2 (a) Bulk's solids volume fraction Φ , (b) longitudinal velocity field u and (c) vertical velocity field w at t = 229.25 s for Experiment 1 (see Tab. 2). Longitudinal distances were measured from the wall formed by the POM pieces passing around the flume's downhill par of rollers. Two differing flow sections can be distinguished from the images with a sharp transition at $x \approx -25$ cm: (i) for $x \lesssim -25$ cm, a well-arranged particle flow flowing in layers, and; (ii) for $x \gtrsim -25$ cm, a convective-bulged front where particles recirculate. The discontinuous lines correspond to (b) vertical or (c) horizontal profiles of the velocity field. Velocity profile values are plotted using continuous white lines. These values are only shown to illustrate relative fluctuations along the profiles and visualise their shape. A movie of Experiment 1 is available as supplementary material.

Table 2 Parameters of the experimental dataset. Φ^s is the overall small particle proportion of the bulk, the slope θ and the measured speed of the conveyor belt u_b .

Experiment no.	d_s	d_l	$\Phi^s~(\%)$	θ (°)	$u_b \ (\mathrm{cms}^{-1})$
1 (monodisperse)	6	-	100	15	8.16
2 (bidisperse)	6	14	90	15	7.74
3 (bidisperse)	6	14	80	15	7.76
4 (bidisperse)	6	14	70	15	8.24
5 (bidisperse)	6	14	60	15	7.62
6 (monodisperse)	8	-	100	15	7.94
7 (bidisperse)	8	14	90	15	7.69
8 (bidisperse)	8	14	80	15	8.09
9 (bidisperse)	8	14	70	15	7.82
10 (bidisperse)	8	14	60	15	8.16

³⁰⁷ bulk concentrations and velocity fields as functions of time. Next, we time-averaged
 these fields to obtain general trends and to describe processes that instantaneous
 frames were unable to show.

The main body of experimental work consisted of eight stationary bidisperse granular avalanches. To include large particles in the bulk, we replaced part of the weight of small particles with large particles keeping the same total weight and only changed Φ^s . The overall general small particle concentration Φ^s , therefore, ranged from 90% to 60%, with the large particle concentration varying complementarily, i.e., $\Phi^l = 100 - \Phi^s$. Since both species had the same intrinsic material density ρ_* , the overal bulk volume concentration remained the same in every run. In addition

Before data acquisition, the experiments were run until a stationary and, when possible, uniform flow was achieved. For each experiment, we first prepared the granular bulk of small and large particles (when needed) in the desired propor-tions. The particles were then put inside the flume and mixed as it rested almost horizontally. This resting position prevented particles from moving and altering their initial arrangement. We mixed the bulk before each experiment to have a close-to-homogeneous and reproducible initial condition. The fluid pump (shown in Fig. 1) was used to fill the flume with the interstitial fluid, and once full, we in-clined the flume and turned on the motor. Only after stationary flow condition was achieved, image acquisition could begin. The flow was considered stationary when the flow's height profile and the avalanche front did not vary notably over sev-eral minutes. Image acquisition was performed for 5 minutes, and we took 12,000 frames per run. The flume was then returned to a horizontal position and emptied before the next experiment.

Due to the flume's dimensions, the region of interest (ROI) for image acqui-sition did not cover the entire flume length. Our experimental images captured a length of 44 cm focused on the flow's leading edge, near the downhill end of the flume. Thus, our experimental results involved 42% of the whole bulk. Full image acquisition of the entire avalanche would have implied lower image resolution, and the benefits in terms of physical insights would have been limited because the re-circulation of large particles in our experiments took place within the avalanche's leading edge, whereas the unimaged flow behaved similarly to the flow in the ROI.

343 5.1 Belt velocity

We can consider u_b as an input parameter or a measurement. Indeed, although u_b was set before experimental image acquisition, its value varied with θ , the load on the belt and the friction imposed by the belt's pieces. Many processes can alter motor torque and thereby belt velocity (see §4). Instead of calibrating of u_b as a function of the electrical power supplied to the belt engine-a process fraught with uncertainties—we decided to measure its velocity directly after the desired stationary regime was achieved. Table 2 recaps the features of this work's experimental dataset, with the measured u_b values shown in the last column.

352 6 Results

353 6.1 Monodisperse experiments

The monodisperse avalanches showed two distinctive flow sections: one at the front and the other at the back, with a marked transition between the two. Towards the flow front, at the flume's downhill end, a convective, bulged region was observed. This front bulge was similar to that studied recently by Denissen et al. (2019) for a bidisperse flow. Henceafter, we refer to this region as the flow's convective-bulged

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Fig. 3 Time-averaged velocity profiles $\bar{u} = \bar{u}(z)$ (left column); time-averaged bulk's solids volume fraction field $\overline{\Phi}$, and free-surface velocity u_h (black line) and slip u_s (green line) velocity (centre column); and normalised velocity profiles $u^* = u^*(1-(1-z/h)^{3/2})$ (right column). Top and bottom rows show results for monodisperse 6-mm and 8-mm experiments (Experiments 1 and 6 in Tab. 2, respectively). The velocity profiles are plotted in grayscale from white to black, from the back to the front of the flow's ROI, respectively.

front, or expanded front. In the rest of the conveyed volume, towards the flume's uphill end, the particle flow transitioned into a well-arranged structure of particle layers that moved on top of each other. Naturally, this compact, ordered region was referred to as the layered flow. To illustrate these flow regions, Fig. 2 shows an experimental image and its corresponding extracted fields. This image was taken from Experiment 1 at t = 229.25 s, and its bulk volumetric concentration Φ , longitudinal (in the direction of the flow) velocity u and vertical velocity w fields are plotted on top of it. Fig. 2 reveals the particle structures in the background and a glimpse of the described flow regions. Overall bulk concentrations Φ varied between the described regions. The front showed a more diluted flow $\Phi \approx 0.3$, whereas the tail was more concentrated ($\Phi \approx 0.5$). The flow height h also showed marked differences, with height at the front reaching its maximum at h = 6 cm, or $\approx 10d_s$, whereas it was close to 4 cm at the back, or $\approx 7d_s$.

To highlight some sections of the velocity field, we plotted profiles along the inclined flume's longitudinal and transverse sections (see continuous white plots in Fig. 2(a) and (b)). The velocity field measurements revealed a quasi-uniform behaviour for u(z), with particles at the top moving faster than those at the bottom and a significant basal-slip condition, which was to be expected in such granular experiments (Louge and Keast, 2001; Ancey, 2001; Hsu et al., 2008). Vertical velocity w(x) profiles were notably less consistent along the flow, where we observed much more vertical particle movement in the flow's leading edge than in its tail, where particle layers just moved on top of each other. As mentioned, the flow could be separated into two sections at $x \approx -25$ cm, measured longitudinally from the flume's downhill end. A sudden change of $w \approx 4 \text{cm s}^{-1}$ marked the transition between the tail and leading-edge sections, from where particles started to recirculate within the bulged front. Only particles that had become tightly attached to the belt managed to escape the leading edge and, after reaching the flume's uphill end, they were reincorporated into the avalanche.

Time-averaged $\overline{\Phi}$, \overline{u} and \overline{w} fields were calculated to refine these general observations. When time-averaged, velocity fields became smoother and the $\overline{u}(z)$ profiles showed consistent behaviour in the longitudinal direction. In general, these $\overline{u}(z)$



Fig. 4 Time-averaged strain-rate tensor invariants in Experiment 1: (a) expansion rate \overline{I}_D and (b) shear rate \overline{II}_D . The vertical dashed lines correspond to vertical profiles and the corresponding values for the strain-rate tensor invariants are plotted as continuous white lines.

³⁹⁰ profiles showed Bagnold-like characteristics, but subject to a strong basal slip u_s . ³⁹¹ Fig. 3 shows a normalised velocity profile u^* defined as

$$u^* = \frac{\bar{u} - u_0}{u_h - u_0} \tag{19}$$

where $u_h = \bar{u}(h)$ is the surface particle velocity, and $u_0 = \bar{u}(0)$ is the basal particle velocity, which in turn defined the slip velocity as the difference between belt speed and basal velocity, i.e. $u_s = u_b - |u_0|$. Therefore, u^* is the time-averaged velocity field u normalised to the velocity difference between the base and the surface, and it is plotted as a function of $1 - (1 - z/h)^{3/2}$ (Fig. 3). We considered this expression for normalised velocity to show the influence of basal slip u_s on the overall velocity profile, which was negligible close to z = h. Close to the flow's free-surface, most u^* profiles adjusted well to $1 - (1 - z/h)^{3/2}$, which is characteristic of a Bagnold-like profile (Bagnold, 1954; Silbert et al., 2001). In terms of longitudinal variation in the u^* profiles, we saw that, towards the front, slip decreased and surface velocities increased (see u_s and u_h in the centre-column subplots of Fig. 3). As a result, the u^* profiles shown in Fig. 3's right column subplots were in better agreement with the Bagnold scaling as we approached to the flow's leading edge (darker lines are for vertical sections closer to the flume's downhill end). However, at the very front of the flow, the agreement with the theoretical Bagnold profile decreased again. From a hydraulic point of view, this behaviour might be related to the changes in u_s, u_h , and the free-surface profile.

We determined the strain-rate tensor invariants to quantify how expanded or sheared the two flow regions were. Fig. 4 shows the time-averaged expansion rate \overline{I}_D and shear rate \overline{II}_D fields corresponding to the strain-rate tensor's time-averaged first and second invariants (see §2.3). Our results indicated that the leading edge was highly-sheared and expanded, with a marked vertical gradient for \overline{I}_D and constant \overline{II}_D close to the front. To the rear, \overline{I}_D fluctuated around 0, and \overline{II}_D showed a negative gradient to the flow's free-surface, with higher values at the bottom, as we would expect from the imposed boundary condition. Qualitatively, expansion and shear rates were significantly higher in regions where flow height was also high and Φ was low, right to the convective front. These observations were also related to low u_s values, as shown in Fig. 3. A decrease in basal slip might



Fig. 5 Time-averaged velocity profiles $\bar{u} = \bar{u}(z)$ (left column); time-averaged small particle concentrations $\bar{\phi}^s$, free-surface velocities u_h (black lines) and slip velocities u_s (green lines) (centre column); and normalised velocity profiles $u^* = u^*(1 - (1 - z/h)^{3/2})$ (right column). (a)–(d) are for Experiments 2–5, and (e)–(h) are for Experiments 7–10 (see Tab. 2). White arrows represent the normalised velocity fields $\bar{u}/\max_{\forall x,z}(\bar{u})$ and $\bar{w}/\max_{\forall x,z}(\bar{w})$. Velocity profiles in the left and right columns are plotted in grey scale, from white to black, from the uphill end to the downhill end of the flume's ROI.

explain the avalanche's blunt front appearance and high expansion rate, due to
the more effective shear transmission from the belt to the bulk.



Fig. 6 Segregation flux f_{sl} for the $\Phi^s = 90$ % experiment (Experiment 2, Tab. 2). f_{sl} was calculated using the formulation suggested by Trewhela et al. (2021a) and simplified in Eq. 13.

422 6.2 Bidisperse experiments

Adding large particles did not substantially change our avalanches' overall dynam-ics. When the concentration of large particles was low ($\Phi^l = 10-20\%$), the leading edge concentrated those large particles, recirculating them. For $\Phi^l > 20\%$, the well-defined regions observed at low concentrations became less apparent, whereas other structures emerged. Large particles were often dragged uphill, past the tran-sition between the bulged-front and layered-tail regions, altering the characteristic structures observed in the monodisperse experiments. When we time-averaged the velocity and concentration fields, we still observed the convective leading edge. As a result of particle-size segregation, large particles were found predominantly at the free surface and within the leading edge, due to strong segregation fluxes in the middle of the bulk. This behaviour probably reflected a more effective transmission of shear close to the front, or low slip, which was observed in the monodisperse experiments.

Figure 5 shows the time-averaged small particle concentration field $\bar{\phi}^s$ for our experiments (Fig. 5, centre column). As expected from size segregation theory, the time-averaged concentration fields show an inversely-graded bulk towards the flume's downhill end. We can infer from Fig. 5 that in experiments with larger R values (Experiments 2-5, (a)–(d) in Fig. 5), large particles recirculated within the flow's leading edge. This large particle concentration resulted from a relatively faster segregation flux f_{sl} for larger R values. To support this interpretation, we determined the segregation flux f_{sl} using the empirical expression 13 (Fig. 6). For this calculation, we assumed a hydrostatic pressure distribution, and the ϕ^s and $\dot{\gamma} = 2\overline{II}_D$ fields were determined from coarse-grained experimental data. Results presented in Fig. 6 indicate that the segregation flux was highest in the convective-front region. This was closely connected with the shear-rate distribution shown in Fig. 4 for the monodisperse case, since $f_{sl} \sim \dot{\gamma}$. The high values for f_{sl} at the front were still smaller than the w values at the transition between flow regions, presented in Fig. 2 ($w \approx 4 \text{ cm s}^{-1}$).

Segregation-induced large-particle recirculation was observed in all the experi-ments and is shown via normalised velocities, $\bar{u}/\max_{\forall x,z}(\bar{u})$ and $\bar{w}/\max_{\forall x,z}(\bar{w})$, in the form of white arrows (Fig. 5, centre column). For R > 2, expansion rates were found to be related to more efficient, and hence faster, segregation rates (Trewhela et al., 2021b), which was evidenced by our large particles in Experiments 2-5. Our results for $d_s = 6$ mm, i.e. R = 2.33, showed that large particles are probably to be constrained to the bulged-front, seen in Fig. 5 (a)–(d). For the experiments with R = 1.66 in Fig. 5 (e)–(h), we observed a less marked segregated state at

the front with lower large-particle concentrations, a sign that large particles weremore homogeneously distributed along the flume.

Breaking size segregation waves were observed in all the bidisperse avalanches. We can infer from Fig. 5 that the breaking-size segregation wave structure was similar to that observed by van der Vaart et al. (2018). From near the surface of the downstream end of the flow, large particles (red colour intensities in Fig. 5) fell onto the very front of the avalanche where they were overrun by the flow and dragged back into the bulk. Eventually, these large particles segregated and rose back to the surface onto the front, recirculating. The lens-shaped region (Gray and Ancey, 2009; Johnson et al., 2012; van der Vaart et al., 2018) where large and small particles were interchanged as a result of shear-induced segregation, can be seen in the middle part of the avalanche, between -40 < x < -10 cm for (a) to (h) in Fig. 5. Concentration gradients of $\bar{\phi}^s$ in this region indicate an apparent mixing, where large particles rise and small particles percolate as a result of segregation. Our results also showed that changes in the overall particle concentrations between different experiments induced variations in the characteristics of the breaking-sizesegregation waves. As we increased the overall concentration of large particles, they formed a thicker layer within the leading edge and the lens region extended uphill of the flow, disrupting the layered region described in §6.1.

The results shown in Fig. 5 follow the trend observed in the monodisperse media experiments. Slip u_s was lower, with values that changed along the direction of the flow and ranged from 40% to 80% of u_b (Fig. 5, green lines in centre column). From Fig. 5, we infer that the addition of large particles regularised slip by making the longitudinal gradient less steep than the low Φ^l and monodisperse media experiments. Surprisingly, the experiments with $d_s = 6$ mm showed an inversion of the u_s profile when Φ^l was increased: a higher u_s was measured near the flow when $\Phi^l > 10\%$. However, this result was not consistent with the experiment made using $d_s = 8$ mm, which suggests that bed roughness played an important part in shear transmission and should be considered when analysing the slip effect. Fig. 5's right column shows that u^* came close to $1 - (1 - z/h)^{3/2}$, indicating a Bagnold-like velocity profile (Bagnold, 1954; Mitarai and Nakanishi, 2005) for the bidisperse avalanches. Even though this result might have been expected, we found that velocity profiles were consistently uniform in shape. Similar to what was observed for monodisperse materials, basal slip tended to skew the profiles, particularly close to the belt, but further from the bottom, profiles were in good agreement with the Bagnold scaling. Average particle concentration influenced results in terms of consistency, as discussed: when Φ^l was increased, the slip all along the base became less variable and the velocity profiles matched the function $1 - (1 - z/h)^{3/2}$.

498 7 Conclusions

⁴⁹⁹ Using a specially constructed inclined conveyor belt, we ran experiments to study ⁵⁰⁰ granular avalanches. All ten experiments, carried out using monodisperse or bidis-⁵⁰¹ perse media, exhibited a quasi-uniform steady behaviour characterised by a con-⁵⁰² vective front at the downhill end of the inclined flume and a particle-layered tail ⁵⁰³ towards the flume's uphill end. Our experimental results revealed characteristics ⁵⁰⁴ and structures typical of granular flows, which have been described in the lit-

⁵⁰⁵ erature. These features included blunt fronts (Denissen et al., 2019), breaking
⁵⁰⁶ size-segregation waves (Thornton and Gray, 2008; Gray and Ancey, 2009; Johnson
⁵⁰⁷ et al., 2012; van der Vaart et al., 2018) and crystallisation (Tsai and Gollub, 2004).

Even for bidisperse media, time-averaged velocity profiles showed a $h^{3/2}$ scaling consistent with Bagnold's rheology and in agreement with earlier observations (Silbert et al., 2001; Mitarai and Nakanishi, 2005), and the $\mu(I)$ rheology (Jop et al., 2006). In this respect, the consistent behaviour exhibited by the u^* profiles suggests the existence of an equivalent particle diameter dependent on d_{ν} and ϕ^{ν} , as defined by Eq. (14) (Tripathi and Khakhar, 2011). Finally, these velocity profiles could be used as inputs to models coupling size segregation and granular avalanches as suggested by Gray and Ancey (2009). We moved a step further in that direction by computing the segregation flux f_{sl} using the expression proposed by Trewhela et al. (2021a). We found that f_{sl} was high within the avalanche's leading edge, and this was further confirmed by large-particles recirculation and high values for both strain-rate tensor invariants (Trewhela et al., 2021b).

Various velocity and slope conditions should be explored to identify similar-ities and differences with the results presented here. The influence of the belt's roughness and the vertical boundaries created by the upper rollers could also be addressed, but eliminating their influence on the flow is currently impractical and outside this article's scope. We believe that further work in that direction would not change the significance of the present experiments. Nonetheless, this experi-mental conveyor belt setup proved to be useful for the visualisation and study of the internal dynamics of granular flows.

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536 Conflict of interest

537 The authors declare that they have no conflict of interest.

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707 Appendix: Setup-related difficulties

708 Plastic-fluid interactions

Two important objectives of this setup were minimising the fluid volume used and the investigators' exposure to harmful, flammable vapours; we therefore devised an enclosed flume. Achieving these objectives required sealing the setup to avoid leaks and spillages, which can be extremely dangerous when dealing with flammable fluids. Although this might seem simple at the outset, using non-conventional fluids led to interactions with the setup's components. Sealing had to be done with plastics, but many of them reacted chemically with the ethanol and benzyl-alcohol mixture. For example, acrylics like poly (methyl methacrylate) (PMMA) were rapidly dissolved, and most rubbers lost some of their elastic properties-a feature fundamental for sealing. These materials had to be scrapped after a couple of hours or days of exposure to the fluid.

Among plastics, polyoxymethylene (POM) and polyvinyl chloride (PVC) re-sisted long exposure to the fluid well. We observed no important changes in their material properties. However, and in general, these plastics are slightly porous and tend to absorb small amounts of fluid when immersed for a long time. Even though that absorption was very small, we noticed that after long use, friction between the belt pieces and the flume's grooves increased to a point where the motor jammed. Not only did friction increase, but compression between the POM pieces became notably higher, which desynchronised them from the geared wheel. To determine how large the fluid absorption was, we measured the changes in length of two identical pieces of differing materials. Figure 7 shows measurements of two immersed belt pieces: one made of POM

⁷³⁰ Figure 7 shows measurements of two immersed beit pieces: one made of POM
 ⁷³¹ and one of PVC. Measurements were made after different fluid-exposure times, of
 ⁷³² up to 600 hours of submergence. To quantify the expansion, the material's relative
 ⁷³³ dilation was calculated as

Relative dilation (%) =
$$\frac{|L^i - L_0^i|}{L_0^i}$$
, (20)



Fig. 7 Measurements of relative dilation at different fluid-exposure times for identical POM (red) and PVC (turquoise) belt pieces. Dimensions L^i correspond to i := 1 for length, (a); 2 for width, (b); and 3 for height, (c). No stresses were applied to the pieces.

where $L^{i}(t)$ is the post-submergence measurement in mm (i = 1, 2, 3 for length, width and height, respectively) and L_0^i is the pre-submergence measurement in mm. We observed that POM pieces swelled much more, and more steadily, than their PVC counterparts. This swelling was sufficient to explain the problems cre-ated in the experimental setup. An expansion of $\sim 1\%$ in belt depth or length may seem negligible, but with 300 adjacent pieces, this expansion was equivalent to adding three extra pieces to the belt system. More than one extra piece was enough to desynchronise the geared wheel, which ended up blocked by the bolts getting caught in its teeth. Regarding side friction, this increased consistently with the extra compression resulting from the pieces expanding in the already compressed belt system. As we observed after our experiments, friction became great enough to gradually bring the motor to a halt.

In general, PVC expanded by less than half of POM's expansion, encouraging
us to use PVC in future experiments. PVC is also opaquer than POM, thus laser
reflection close to the belt was lower and image definition was improved.

Rubbers and silicones were required to seal setup joints and the screwed pieces that needed to be routinely changed between experiments. When exposed to the RIM fluid, rubber rapidly loses elasticity, and after long exposure it partially dis-solves, leading to leaks and fluid pollution, both of which are detrimental to safety and finances. We tested different types of rubber and silicone with little-to-no suc-cess. To the best of our knowledge, only Viton, a fluoroelastomer, was adequate for the o-rings or other rubber pieces. Common silicone could not seal the setup and was rapidly dissolved. Silicone LOCTITE SI 5910 managed to endure exposure to the fluid effectively for long periods without leakage.

758 Pollutants and filtering system

The conveyor belt pieces inevitably produced friction between themselves, the grooves and the rollers. Most of the friction was against aluminium and the scrap-ing released a very fine black dust that spreads throughout the setup. Long-running experiments accumulated enough dust to reduce fluid transparency, obstructing the laser and reducing image quality. To enhance image definition and increase light intensity, we changed acquisition parameters, like the gain and/or reduced the lens' focal ratio. Nevertheless, the black dust concentration would increase to a point where these improvements became pointless.

A filtering system was devised to remove the dust from the fluid. We could have used a wet sieving/filtering system, such as a Retsch AS200, but knowing nothing about its components and not wanting to damage it with exposure to our fluid, we decided to try a simpler method. A large reservoir dripped fluid into a funnel containing 40 μm filter paper. We were able to filter the fluid entirely in approximately one day, which was a reasonable amount of time in which to prepare the next experiment. With twice the amount of fluid, we were able to rotate the fluid batches and keep the amount of dust under control, thus not harming image quality. A reduction in dust production, via improvements such as stainless steel grooves, could certainly enhance the setup's performance and image quality in the future, but these were not used for this work.