1 Article title

2 Automated grain sizing from UAV imagery of a gravel-bed river:

3 benchmarking of three object-based methods and spatial analysis of grain

4 size distributions

5 Abstract

6 Measuring grain sizes in gravel-bed rivers is crucial when studying river 7 dynamics and sediment transport. Automated methodologies have been 8 developed in recent years for detecting individual grains and measuring their size on digital imagery. These object-based methodologies have 9 10 mainly been applied to handheld imagery. Low-cost and high-resolution 11 orthoimages covering long river reaches are nowadays accessible with the improvements in Uncrewed Aerial Vehicles (UAV) and Structure-from-12 Motion (SfM) photogrammetry. Applying object-based grain sizing 13 methodologies to such orthoimages may provide wide-scale information 14 15 about the grain-size spatial distribution along streambeds. We first 16 examined how accurate three object-based models (BASEGRAIN, PebbleCountsAuto and GALET) were, by comparing their outcomes to in-17 18 field manual measurements of grain sizes and manual grain labelling. We found that BASEGRAIN and PebbleCountsAuto underestimated grain sizes 19 20 on average, whereas GALET generally overestimated grain size percentiles. Grain size measurements obtained by manually labelling grain 21 features were consistent with in-field measurements. We then show that 22 spatial statistics applied to automatically detected grain features allowed 23

- 24 us to draw information about the grain-size organisation in an Alpine
- 25 braided river. Spatial statistics were instrumental in consistently
- 26 identifying patches of different grain sizes and thereby provided evidence
- 27 for marked grain-size patchiness.

28 Keywords

- 29 Automated grain-size measurements; UAV; spatial statistics; grain-size
- 30 organisation; gravel-bed rivers.

31 **1. INTRODUCTION**

River beds are seldom composed of sediments of uniform size. Quantifying 32 the size distribution of sediment mixtures is fundamental for 33 understanding and modelling river flows, morphodynamics and sediment 34 35 transport processes (Bunte and Abt, 2001). For instance, a number of flow 36 resistance equations involve grain size guantiles (e.g., Strickler, 1923; Keulegan, 1938; Hey, 1979; Smart and Jaeggi, 1983; Ferguson, 2007; 37 Rickenmann and Recking, 2011). Another example is provided by the 38 methods for predicting the threshold of incipient motion and transport 39 40 rates (e.g., Recking, 2013; Recking, 2016; Hodge et al., 2007). When 41 studying bedload transport in mountain rivers—whose sediment deposits are often prone to grain sorting processes, such as bed armouring and 42 size-dependent selective transport—accurate quantification of local grain 43 44 size distributions is particularly important for assessing bedload transport 45 mechanisms (Schlunegger et al., 2020).

A variety of field sampling procedures have been developed for 46 characterising river-bed grain-sizes in guantitative terms. Mechanical 47 sieving of volumetric samples and individual measurements of surface 48 49 grains are commonly used techniques (Kellerhals and Bray, 1971). Nonetheless, these procedures can be laborious and entail limitations for 50 the assessment of spatial variations of bed-material grain-sizes (Bunte 51 and Abt, 2001). To mitigate these issues, automated grain sizing methods 52 53 based on remote sensing technologies have emerged in recent decades. A 54 number of research studies have been dedicated to utilizing images for

55 measuring grain sizes (see Carrivick and Smith, 2019; Piégay et al., 2020). Parallelly, recent improvements in Uncrewed Aerial Vehicles (UAV) 56 and Structure-from-Motion (SfM) photogrammetry software packages 57 have allowed to produce easily and at relatively low-cost valuable 58 59 topographic datasets, which typically comprise orthoimages, digital surface models (DSM) and dense point clouds. Combining UAV-SfM 60 imagery and image-based grain sizing techniques can provide access to 61 grain size estimates over large spatial scales, in a cost- and time-efficient 62 63 manner (Carrivick and Smith, 2019).

64 The first image-based methodologies for measuring grain sizes in rivers relied on the visual interpretation of nadir photographs (e.g., Adams, 65 1979; Ibbeken and Schleyer, 1986). Grain size distributions (GSD) were 66 67 estimated by measuring the projected intermediate axis (b-axis) of grains on photographs. Although less field time is required (only photographs 68 need to be taken), this method still necessitates large processing times to 69 70 measure grain features individually (Bunte and Abt, 2001). Since the early 71 2000s, numerous studies were dedicated to automatizing grain sizing procedures on images (McEwan et al., 2000; Butler et al., 2001; Graham 72 et al., 2005). Two distinct approaches have been followed. The first 73 approach involves deriving grain sizes from image statistics (Carbonneau 74 et al., 2004; Buscombe, 2013; Woodget and Austrums, 2017; Woodget et 75 76 al., 2018). This methodology derives characteristic grain sizes using image texture metrics, autocorrelation or wavelet transformations. Such 77 methods are based on regression between single parameters and grain 78

sizes (e.g., Carbonneau et al., 2004; Warrick et al., 2009; Woodget et al., 79 2018), or on more novel methods based on Convolutional Neural 80 81 Networks (CNN; e.g., Buscombe, 2020; Lang et al., 2021). The second 82 approach focuses on detection and measurement of individual grain 83 features, and is thus referred to as 'object-based'. Individual surface grains can be identified by using image thresholding and segmentation 84 processing (e.g., Graham et al., 2005; Detert and Weitbrecht, 2012; 85 Purinton and Bookhagen, 2019), or with most recent object detection 86 87 algorithms based on CNN (e.g., Soloy et al., 2020; Mörtl et al., 2022; 88 Chen et al., 2022). The advantages of object-based grain sizing over 89 image statistics-based methods are (i) that the former does not require 90 site-specific calibration and (ii) that one can derive more information from 91 object-type data (e.g., grain arrangement). Object-type data can also be 92 converted into grid-type data whose cell provide the local GSD.

The grain size distribution of gravel-bed rivers presents significant 93 94 variations at local scale (Bluck, 1979). Many studies regarding the local 95 GSD variability have been based on sparse manual grain size measurements combined with visual analyses (e.g., Lisle and Madej, 96 1992; Dietrich et al., 2006; Guerit et al., 2014). The first object-based 97 grain sizing tools have been initially developed for applications on 98 handheld imagery or images from pole-mounted camera (e.g., Butler et 99 100 al., 2001; Graham et al., 2005). This imagery approach limits the 101 investigation to local spatial scales. Applying object-based grain sizing 102 methodologies to orthoimages may provide information on spatial

103 variations in GSD that occur over distances spanning from several104 hundred meters to a few decimeters.

105 The quality of the grain size information derived from orthoimages and its 106 potential for understanding geomorphological processes depend a great deal on the accuracy of the applied technique. Therefore, testing the latest 107 108 object-based methodologies on high-resolution orthoimages is key to 109 identify specific limitations and biases. Mair et al. (2022) evaluated the 110 uncertainties in grain size measurements on aerial imagery with regard to the UAV-SfM approach. A performance assessment of a set of existing 111 112 grain sizing routines has been conducted by Chardon et al. (2022) for applications to handheld imagery. To the best of our knowledge, no study 113 114 evaluated multiple object-based techniques for applications to high-115 resolution orthoimages.

116 In this context, we evaluated three object-based grain sizing software routines (BASEGRAIN, Detert and Weitbrecht, 2012; PebbleCountsAuto, 117 118 Purinton and Bookhagen, 2019; GALET, Mörtl et al., 2022) and compared 119 their outcomes to in-field manual measurements of grain sizes and manual labelling on orthoimages. We wanted to answer the following 120 121 questions. First, which automated grain-sizing software performs the best on orthoimages of a gravel-bed river? Second, which are the limitations of 122 123 each tool? We then investigated how the information issued from these software routines can be used for mapping and quantifying spatial 124 125 variations of surface grain sizes in a braided mountain river located in the

- 126 Swiss Alps. Global and local spatial autocorrelation statistics (e.g., Moran,
- 127 1948; Anselin, 1995) have been extensively used for assessing
- 128 geographical clustering in various scientific fields—from crop and landform
- 129 classifications (e.g., Maimaitijiang et al., 2020; Drăguţ and Eisank, 2012)
- 130 to criminological and epidemiological investigations (e.g., Baller et al.,
- 131 2001; Auchincloss et al., 2012). We wanted to explore their potential for
- 132 analysing the spatial distribution of grain sizes along a river reach.

134 **2. METHODS**

The surface grain size distribution of a mountain river (Sect. 2.1) was 135 investigated by conducting line sampling (Sect. 2.2). We designed UAV 136 137 surveys to reconstruct orthoimages of the study site based on SfM 138 algorithms (Sect. 2.3). Grain sizes were measured digitally on these orthoimages by using manual labelling (Sect. 2.4) and three object-based 139 grain sizing methods (Sect. 2.5). These digitally measured grain sizes 140 141 were compared to grain sizes measured manually in the field (Sect. 2.6). 142 Finally, we evaluated the spatial variability of surface grain sizes over the 143 study reach using one of the object-based grain sizing software (Sect. 144 2.7).

145 **2.1 Study site**

The Navisence is a mountain river located in the South-West Swiss Alps, tributary to the Rhône River (Figure 1a). This 23-km-long river drains a 257 km² catchment. Its main water source is the Zinal Glacier at 2300 m a.s.l. The river is hydrologically undisturbed upstream of the village of Zinal.

The study site is a 500-m-long and 60–90-m-wide river reach, located in the upstream part of a 2-km-long floodplain named "Plats de la Lée" with an average slope around 3% (Figure 1b). The Navisence flows across this alpine floodplain and develops a braided network upstream of the village of Zinal (1650 m a.s.l.). There, the catchment area is 77 km². A gauging station managed by a Walliser research institute (CREALP, Sion) is located

downstream of the study reach, and has gathered data since 2011 (flow 157 158 rates and bedload transport rates). The river has a glacio-nival 159 hydrological flow regime, with very low flow rates in winter and high discharges in summer related to snow and glacier melting, with significant 160 circadian variations (Travaglini et al., 2015). The typical low flow 161 162 discharge is 1 m^3 /s in winter, while maximum hourly discharge can exceed 25 m³/s in summer. Over the last five years, the morphology of 163 the braided network has been mostly impacted by a single major flood in 164 165 July 2018. Regarding the sediment lithology, the surface alluvial deposits found in the river bed at the Plats de la Lée are mostly composed of 166 167 metamorphic rocks (mainly orthogneiss). Therefore, sediments found on 168 the study reach often exhibit variations of rock texture inside single 169 grains, due to foliation or veins for example.



170

- 171 Figure 1. (a) Location of the study site and the Navisence River watershed in
- Switzerland (© swisstopo). (b) Location of the UAV surveys over the study reach (the 172
- 173 river flows northwise). The river image is an orthoimage obtained from a UAV survey 174
- carried out on 13 Sep 2022 (50-m-high flight). (c) Detailed view of the three 175 orthoimages which were reconstructed from UAV collected images, with positions of the
- 176 line sampling analysis, ground control points (GCPs) and check points (CPs).

178 **2.2 Manual measurements of grain sizes**

179 We used the line sampling procedure proposed by Fehr (1987). This 180 procedure has been specially devised for mountain rivers, and has thus 181 been used in numerous field studies of hydraulics and sediment transport 182 in mountain rivers across the Alps (e.g., Ramirez et al., 2022; Schneider 183 et al., 2016; Konz et al., 2011; Rickenmann and McArdell, 2007; 184 Rickenmann, 1997). There are alternatives to Fehr's method; for instance, 185 grid sampling protocols such as the Wolman pebble count (Wolman, 1954) and its variants are much more common than line sampling. The main 186 187 advantage of Fehr's method over other techniques is that it is much easier to georeference a sample line than a grid (or a random walk) in the field 188 189 and in orthophotographs. When comparing grain size estimates from field 190 measurements and automated methods, it is thus possible to sample the 191 same stones in the field and orthophotographs and thus, by doing so, we can benchmark methods on a fair basis. Another major advantage of 192 193 Fehr's method is that by considering all the stones crossed by the 194 sampling line, it requires a smaller sampling space than methods based on areal or random particle sampling, which is of great interest for 195 196 characterising spatial variations in grain size distribution when the riverbed involves patches of distinct grain sizes. A possible disadvantage 197 of Fehr's method is that its accuracy has been much less studied than 198 199 Wolman-based methods (Rice and Church, 1996; Daniels and McCusker, 2010). The recommendations drawn for Wolman-based methods should, 200 201 however, apply to Fehr's method: the sampling line has to cross a large

202 number of stones—as large as 400 according to Rice and Church (1996) if sufficient precision in the quantile (or percentile) estimation is desired. 203 204 In practice, this requirement is problematic for mountain rivers like the 205 Navisence because of spatial variations in grain size over short distances. 206 From a statistical viewpoint, the central limit theorem can help understand 207 why accuracy of grain size guantiles varies as the sample size's square root as Rice and Church (1996) found in their field study, and why this 208 209 result holds only when the sample is drawn from the same population, 210 with the same mean and variance. When the grain size distribution 211 exhibits substantial spatial variations, obtaining unbiased estimates 212 becomes particularly difficult: (i) if the sample size is small, then it is 213 probably representative of the local population, but estimates are 214 inaccurate, (ii) if the sample size is large, then in principle, a higher 215 accuracy is expected in quantile estimation, but measurements are 216 biased. The Navisence riverbed is characterised by a typical median stone 217 size of around 10 cm and patch length of approximately 10 m. These 218 features led us to consider that a sample size of about 150 stones—as 219 proposed by Fehr (1987)—provided a suitable trade-off between precision 220 and representativeness.

We collected samples over 17 lines distributed over areas A, B and C (Figure 1c). Following Fehr (1987), we stretched a string over the dry bed-material surface to be analysed. The b-axis of all stones underneath the string was measured. Stones with a b-axis smaller than 1 cm were not considered. The stones were divided into diameter classes and the number 226 of stones falling in each grain size interval was computed. Approximately 150 stones should be measured to ensure a good representativeness. This 227 228 led us to choose sampling lengths of 5 or 10 m depending on the local grain size. The largest stones (over 10 cm) were often imbricated or 229 230 clogged, which prevented a correct measurement of the b-axis. They were therefore manually extracted, which required significant effort and the use 231 232 of a pickaxe. For one sample and a single operator, this procedure lasted 233 about 1 hour. To georeference each line on geographic information 234 systems, we measured the starting and end point positions using a polemounted GPS/GNSS system—Leica Zeno 20 coupled with a GG04P 235 antenna, with real-time kinematic correction (Swipos-GIS/GEO network). 236

237 Fehr's method involves converting the line samples into approximate 238 volumetric-sample equivalents of the subsurface grains via empirical 239 relations between surface and subsurface grain sizes (Fehr, 1987). The frequency-by-number grain size distribution is converted into a frequency-240 241 by-weight distribution (describing the weight fraction of each grain size 242 interval), so that the results are comparable with standard volumetric sampling. The conversion is based on the voidless cube model (Kellerhals 243 and Bray, 1971), which was empirically adapted by Fehr (1987). As grains 244 whose b-axis is smaller than 1 cm are neglected during the sampling 245 process, the cumulative frequency of the components larger than 1 cm 246 247 has to be corrected to take neglected finer components into account. According to Fehr (1987) observations based on field mechanical sieving 248 in a large set of Swiss gravel-bed rivers, 20% to 30% of the subsurface 249

layer volume is smaller than 1 cm in diameter. Finally, the GSD is 250 extrapolated toward the finest grain sizes. Fehr (1987) observed that for 251 252 the Swiss Alps, the distribution of the fine fraction of the bed and bedload material generally follows a Fuller curve. When predicting the proportion 253 of fine material in the GSD, Fehr assumed that the final GSD follows a 254 Fuller curve for the undersampled finest grain sizes (see Supporting 255 256 Information for the detail). We consider this tail correction to be well suited to our field site, whose bed is mostly structured by coarse particles 257 258 and clogged by glacier flour (Figure 2).





Figure 2. Navisence: view from upstream of the riverbed in the southern sector of areaC.

263 2.3 UAV surveys and structure-from-motion photogrammetry

Areas A, B and C: data acquisition

265 Three UAV surveys were carried out over different sectors of the study reach. The covered areas were named A, B, and C and their location is 266 267 shown in Figures 1b and 1c. We conducted these surveys in order to 268 evaluate the accuracy of digital object-based grain sizing tools on 269 orthoimages, compared to in-field line sampling. Nine manually sampled lines were located in area A, seven in area B and four in area C. We used 270 271 a DJI Phantom 4 pro and a DJI Phantom 4 pro v2 UAVs. These rotatorywing quadcopters are equipped with a GPS for automated flights. They 272 have an integrated camera with a 20-mega-pixel resolution. The 273 274 automated flights were planned using Pix4Dcapture software (v. 4.13.1; developed by Pix4D, Lausanne, Switzerland). Images were taken vertically 275 276 on a predefined trajectory, with a frontal and lateral overlap between individual images in the order of 70%. During image acquisition, the UAV 277 stayed stationary to avoid motion blur. It then moved to the next 278 279 predefined position along the grid line map. In order to obtain the best 280 compromise between image resolution and spatial coverage, we 281 conducted our flights at an elevation of approximately 10 m above the 282 take-off position. As the UAVs flew horizontally, the effective flight height 283 varied depending on ground slope and local topographic features. Ground resolution ranged from 2.9 mm/px to 3.7 mm/px. The survey C was 284 285 conducted under sunny conditions, whereas the surveys over area A and B were conducted under shaded conditions, on clear days and before the 286

sun illuminated the study reach (see Table 1). These three UAV surveys
were always performed before manual line sampling. Further information
about the camera parameters used can be found in Tables S1 and S2 of
the Supporting Information.

291 Area D: data acquisition

292 In order to evaluate the spatial variability of surface grain sizes in the study reach, we carried out a large-scale UAV survey in a second step, 293 covering approximately 14'000 m² (named area D). The flight was 294 planned using the Map Pilot Pro software (v. 4.1.16; developed by 295 296 Automotive Data Research, California). The advantage of this UAV flight planning software over Pix4Dcapture is that it makes it possible to fly at a 297 constant height above a digital elevation model (DEM) generated from 298 NASA's Shuttle Radar Topography Mission (resolution of 30 m/px). 299 300 Therefore, images could be collected at similar flight height (about 10 m) 301 as the approximate floodplain topography was considered. The survey was carried out using a DJI Phantom 4 pro. To avoid motion blur in the 302 images, we selected a fast shutter speed (see Table S2 of the Supporting 303 304 Information for specific camera parameters). The survey was carried out 305 on a clear sky day when the river reach was shaded. Images were taken 306 along a single grid line map at a rate of one image per second and the flight speed of the drone was set at 2 m/s. The images had an overlap in 307 the order of 60% in flight direction and a lateral overlap of approximately 308 309 70%. The other characteristics of this survey are summarized in Table 1.

| Area name | Area size [m²] | Date | Weather | UAV model | Number of images | Number of tie points | Number of GCP CP | Ground sampling distance [mm/px] |
|--------------|----------------------|-------------------|---------------------|----------------------------|------------------------|----------------------------|------------------------|---|
| A | 2′500 | 5 Oct 2022 | Shady, clear sky | DJI Phantom 4 pro | 232 | 6′070′47 9 | 4 9 | 2.9 |
| В | 3′450 | 12 Oct 2022 | Shady, clear sky | DJI Phantom 4 pro | 223 | 6′053′89 8 | 3 5 | 3.7 |
| С | 5′850 | 26 Oct 2022 | Sunny | DJI Phantom 4 pro v2 | 419 | 12′511′9 31 | 6 6 | 3.3 |
| D | 14′350 | 11 Nov 2022 | Shady, clear sky | DJI Phantom 4 pro | 787 | 17'680'4 34 | 8 21 | 3.1 |

310 **Table 1**. Summary of the UAV surveys (GCP = Ground Control Points and CP = Check 311 Points).

312

313 Auxiliary georeferenced points

Ground control points (GCP) were distributed over the surveyed areas to 314 315 constrain more accurately the SfM photogrammetric reconstruction and to 316 assess errors. The GCP were marked with paint, and their position was 317 measured using the same GPS/GNSS system described in Section 2.2. 318 This provided a horizontal positioning accuracy close to 1 cm and a vertical accuracy in the 2–4-cm range. The GCP coordinates were 319 320 measured in the CH1903+/LV95 coordinate system (EPSG 2056). During the SfM reconstruction preprocessing steps, we located the GCP position 321 322 on the images. The start and end points of the manually-sampled lines 323 served as independent check points to evaluate the accuracy of the 324 reconstructed orthoimages. Some start and end points could not be located with certainty on the basis of the photographs taken in the field 325 (14 out of 34), and were therefore not considered check points. Eight 326 GCPs were defined in area D. Additional check points were defined on the 327

basis of three orthoimages produced from 50-m-high flights covering the
entire "Plats de la Lée" (UAV surveys pertaining to a different study).
Twenty-one fixed features were identified on these three orthoimages and
in the orthoimage of area D (see Table 1). The mean coordinates of these
features labelled in the three orthoimages served as check points. The
resulting orthoimage positioning errors are given in Table 2.

334 **Table 2**. Quality assessment of Structure-from-Motion photogrammetry results. Mean error

335 (ME) and standard deviation of error (STDEV) on ground control points and check points

after bundle block adjustment.

| Area name | Groun | d Control Poin | its | Check Points | | | |
|--------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|--|
| | X [cm] ME STDEV | Y [cm] ME STDEV | Z [cm] ME STDEV | X [cm] ME STDEV | Y [cm] ME STDEV | Z [cm] ME STDEV | |
| А | 0.0 0.8 | 0.0 0.9 | 0.0 1.0 | 0.2 1.5 | -2.8 2.3 | 0.3 2.8 | |
| В | 0.0 0.8 | 0.0 0.5 | 0.0 0.0 | -0.9 1.5 | -1.8 2.1 | -4.2 2.0 | |
| С | 0.0 1.0 | 0.0 0.9 | 0.0 1.2 | 0.8 1.8 | 0.7 1.7 | 2.8 1.4 | |
| D | 0.0 7.3 | 0.0 5.4 | 0.0 1.4 | -0.1 4.1 | 2.1 7.3 | 2.5 3.8 | |

337

338 Data processing

339 Geo-referenced orthoimages were obtained by processing the images with

340 the Pix4Dmapper software (v. 4.8.0; Pix4D, Lausanne, Switzerland). By

- 341 combining SfM photogrammetry and multi-stereo view algorithms, the
- 342 software reconstructs the three-dimensional (3D) surface topography. In
- 343 the SfM framework, the 3D positions of a large set of features
- 344 automatically extracted from images are retrieved, simultaneously with
- 345 camera positions and orientations by iteratively solving a highly redundant
- 346 system of triangulation equations (Westoby et al., 2012). This method
- 347 provides a point cloud, which can then be converted into a DSM and an

orthoimage. The main parameters used in Pix4Dmapper can be found inTable S3 of the Supporting Information.

350 **2.4 Digital manual labelling**

Manual labelling was performed by a single operator on the orthoimages 351 using the QGIS software (v. 3.22). We manually drew a polygon on all 352 visible grain features intersected by the georeferenced lines. This labelling 353 354 operation took approximately 10–15 minutes per line. We measured the b-axis of all labelled grains by automatically fitting an ellipse to each 355 356 feature (fitting based on the second central moment of the object geometry). The detailed ellipse fitting procedure is described in the 357 Supporting Information. The b-axis corresponds to the minor axis of the 358 fitted ellipse. This procedure for extracting the b-axis of each labelled 359 360 grain is similar to the ellipse fitting procedure used by the object-based 361 grain-sizing methods described in Section 2.5. Finally, we derived the GSD from the b-axis of the identified grain features for each line using Fehr's 362 363 (1987) method implemented in a Python script.

2.5 Description of selected object-based grain sizing tools

In this section, we describe the internal frameworks of the three objectbased grain sizing tools under investigation. We specify how each tool was implemented to derive grain size distributions that are comparable with those based on in-field manual samples. Figure 3 shows an example of detected grain features along a line using the different methodologies.



Figure 2. Example of digital line sampling with manual labelling and the software
 routines investigated. The blue line corresponds to the location of the georeferenced line.
 The grain features displayed for manual labelling and GALET are the original grain feature
 polygons and not the fitted ellipses. The BASEGRAIN image originates from the software
 GUI.

377 **BASEGRAIN**

We used BASEGRAIN (v.2.3), which is a free access MATLAB-based method developed by Detert and Weitbrecht (2012). It performs individual grain segmentation on digital top-view photographs in five preprocessing steps. Three out of five steps require supervised parameter tuning to optimise performance. Ellipses are then fitted to the detected objects, and the minor axis is considered as the b-axis of the grain feature.

384 Orthoimages were cut out into image tiles corresponding to the bed 385 surface patches where the line sampling was conducted. This splitting was 386 required because BASEGRAIN is not able to handle georeferenced orthoimages. The image tiles were rotated in order to position the line 387 vertically. The BASEGRAIN processing was much influenced by the 388 variations in colour and texture of the Navisence sediments, thus no 389 390 unique set of parameters allowed for optimised object detection for all 391 image tiles. Therefore, object detection had to be performed individually for each image tile when using BASEGRAIN. We tuned the different 392 parameters until a visually optimal segmentation of the grains was 393 394 obtained. No postprocessing was applied to the detected objects. The 395 virtual sampling line implemented in BASEGRAIN was placed so as to 396 match the position of each field sampling line. We extracted the dimensions of all the grains detected and intersected by the line in 397 BASEGRAIN. We then tallied grains using the same grain size intervals as 398 399 those used for manual sampling, and computed the GSD according to 400 Fehr's (1987) method.

401 **GALET**

402 GALET is a deep-learning image segmentation model for grain size 403 analysis developed by Styx4D (Bourget-du-Lac, France) and presented in Mörtl et al. (2022). The CNN model implemented in GALET was trained 404 405 using a dataset generated by a technique based on automated image 406 creation. Mörtl et al. (2022) used manually-cropped grain images and 407 synthesised artificial grain images to generate labelled training images. 408 During the grain detection and segmentation steps in GALET, orthoimages 409 are split into 512 or 1024 pixel-large tiles. The software performs grain 410 detection and estimates the shapes of overlapping grains. A final shapefile is produced in which all detected instances are vectorised. 411

The entire GALET segmentation process was applied on each orthoimage. 412 413 The routine detected the grain features and provided the corresponding 414 shapefiles. We measured the b-axis of all detected grains by automatically fitting an ellipse using the same method as the one utilised for manual 415 labelling. Digital line sampling was performed on these shapefiles in OGIS. 416 417 as the positions of the field sampling lines were georeferenced. We 418 classified the vectorised grains that intersected the georeferenced lines according to their b-axis. The same grain size intervals used for manual 419 sampling were considered and the GSDs were computed by using the Fehr 420 (1987) method. 421

422

424 **PebbleCountsAuto**

PebbleCounts is an open-source Python-based algorithm, developed by
Purinton and Bookhagen (2019). Here we used, its highly-automated
version named PebbleCountsAuto. It is an image segmentation method
that performs individual grain detection. Resulting grain features are
measured via ellipse fitting.

430 As PebbleCountsAuto requires significant computing time to process entire 431 orthoimages (Purinton and Bookhagen, 2021), grain feature detection was performed on image tiles cut out from the orthoimages (similarly to the 432 procedure used with BASEGRAIN). These tiles corresponded to the 433 locations where in-field line sampling was performed. PebbleCountAuto 434 435 only required us to manually tune the threshold level of Otsu's threshold 436 matrix. This parameter was tuned for each processed image tile in order to obtain a visually optimal segmentation of grain features. The default 437 parameter defining the minimum area in pixel for a feature to be 438 considered a grain was modified and set at 23 pixels in order to be 439 440 consistent with the same parameter defined in BASEGRAIN—value based on the limit of grain feature detectability in images (see Graham et al., 441 2005). The model uses a size cut-off criterion to discard grains whose b-442 axis is too small. By default, the cut-off value is set at 20 px, but we 443 decreased it to 3 px so that all grains with a b-axis exceeding 1 cm could 444 445 be considered. PebbleCountsAuto allows one to work with georeferenced orthoimages. Therefore, information about detected grain features such as 446 northing and easting coordinates in an UTM coordinate system, major and 447

minor axis of the fitted ellipses and their orientation could be exported as
text files. This data was used to reconstruct the detected features as
georeferenced ellipses in QGIS. Digital line sampling was then performed
by computing the GSD from grain features intersected by each
georeferenced line.

453 **2.6 Accuracy evaluation**

The grain size percentiles obtained by manually labelling images and those obtained by applying the three grain-sizing tools were compared with the grain sizes retrieved by on-field manual line sampling. The comparisons were done by normalising all digitally obtained grain size percentiles by their corresponding in-field manually measured grain size percentiles as follows:

460

$$d_{norm} = \frac{d_{digital}}{d_{manual}}$$

461 where $d_{digital}$ corresponds to the digitally obtained grain size percentiles, 462 while d_{manual} corresponds to the grain size percentiles obtained from in-463 field manual sampling. Therefore, if the digital measurements were 464 accurate, d_{norm} should be close to unity.

We considered the Normalised Root Mean Square Error (NRMSE) to quantify the errors of digitally-based grain size percentiles in terms of the corresponding fraction of the mean grain size percentiles obtained from in-field manual sampling. This error metric allowed us to directly compare the accuracy of the model estimates for different grain size percentiles, even if the grain scales were different (like for d₁₆ and d₈₄ values which
may not be of the same order of magnitude). For each grain size
percentile, the NRMSE was calculated as follows:

473
$$NRMSE = \frac{\sqrt{\sum_{i=1}^{n} (y_i - x_i)^2}}{\sqrt{n} \cdot x_{mean}}$$

474 where y_i is the value of the digitally estimated grain size percentile on 475 sample i, x_i is the value of the manually measured grain size percentile on 476 sample i, x_{mean} is the mean value of the manually measured grain size 477 percentiles and n is the number of line samples—n = 17 in this study.

478 **2.7 Spatial variability of grain sizes**

479 The spatial variability of surface grain sizes in the study reach was 480 investigated by considering the spatial distribution of the dataset of grain 481 geometries detected by the GALET software on the orthoimage covering 482 the area D reach. The objective was to determine whether grain sizes 483 were randomly distributed over the river bed, or whether some spatial 484 arrangements could be statistically identified in the grain-size samples. We investigated this spatial variability (i) in a regular grid of d_{50} estimates 485 486 computed from the detected grain features, and (ii) directly in a set of 487 discrete grain features.

The d_{50} estimates were computed on 2 × 2 m grid cells. This cell size was chosen as a trade-off between local GSD representativeness (that is, the cell was large enough to contain approximately 100 stones in most cells) and spatial variability (that is, the cell was small enough to exhibit grain492 size variations at the bar scale). Grid cells including water were not considered, as GALET is generally unable to detect underwater grain 493 494 features. We computed the GSD from the grain features detected by GALET, by considering all detected stones whose centroid was located in 495 496 the cells. This sampling procedure corresponds to areal sampling (Kellerhals and Bray, 1971). According to the voidless cube model, the 497 factor α for converting the frequency-by-number into equivalent 498 499 volumetric frequency-by-weight is equal to 2 for areal sampling (Church, 500 McLean and Wolcott, 1987). We applied a correction factor to the finest 501 fraction, as described in Fehr's method (which assumes that 25% particles 502 are smaller than 1 cm, and that the lower end of the GSD can be captured using the Fuller curve). We extracted the d_{50} value from the GSD on each 503 504 cell.

Metrics of spatial autocorrelation were computed to investigate whether 505 506 the grains are distributed randomly in space according to their size, and 507 thus to evaluate the overall clustering tendency. Spatial clusters are 508 defined by Knox (1989) as "geographically bounded groups of occurrences" 509 of sufficient size and concentration to be unlikely to have occurred by chance." A commonly used indicator of clustering is Moran's spatial 510 511 autocorrelation index (referred to as Moran's I; Moran, 1950; see Getis, 512 2010). It summarises the correlation between the value of one spatial unit 513 and the mean value of its neighbouring units, via a spatial weight matrix. 514 For the maps of d_{50} estimates, the neighbours (and thus spatial weights) of each cell were defined according to a queen contiguity, meaning that all 515

cells sharing a common border or one vertex are considered neighbours
(i.e. the 8 cells surrounding each cell). For the grain-feature shapefile, the
spatial weights were set for the 100 nearest neighbours of each feature.
This number corresponds to the size of typical surface samples (Bunte and
Abt, 2001), and thus allows to assess the spatial autocorrelation at a grain
sample scale.

522 Moran's I varies between -1 and 1, and takes values close to 0 when there 523 is no spatial autocorrelation (i.e. individual variables are independent from the mean variable of neighbouring units). It tends towards 1 or -1 when 524 525 there is strong positive or negative spatial autocorrelation, respectively. The variables considered here were the d_{50} estimates (grid-type data) and 526 527 the b-axes of the sample of discrete grain features. By plotting the 528 standardised variables (i.e., variables rescaled to have a mean of 0 and a standard deviation of 1) against the mean of standardised neighbouring 529 variables in a so-called Moran scatter plot, Moran's I can be computed as 530 531 the least square slope of the regression through the origin (Anselin, 532 1996). This procedure for computing Moran's I is equivalent to the formal definition of I, but also enables the visualization of spatial associations in 533 the dataset (Anselin, 1996). The statistical significance of Moran's I was 534 evaluated by testing the null hypothesis that Moran's I is equal to 0, 535 meaning that d_{50} estimates or grain-sizes would be distributed randomly 536 across the space. The reference distribution of Moran's I under the null 537 538 hypothesis was derived by applying a Monte-Carlo method. The attributes

of all individuals in the dataset were randomly moved over the locations 539 and Moran's I was computed. This process of randomisation followed by 540 Moran's I computation was performed 999 times, to infer the probability 541 density function of Moran's I under the null hypothesis. Finally, we 542 543 assessed the statistical significance through the pseudo p-value (Anselin, 1995). We compared Moran's I of the original dataset to Moran's I density 544 function obtained from the Monte-Carlo simulations and rejected the null 545 546 hypothesis if the p-value was lower than a significance level of 0.05.

Moran's I provides information about the overall trend towards clustering 547 548 in the spatial distribution of grain sizes; it does not give any indication about cluster location. To evaluate the strength variations in spatial 549 550 autocorrelation with location, we conducted an analysis of the Local 551 Indicator of Spatial Association (LISA; Anselin, 1995). Following Anselin (1995), we decomposed Moran's I into local coefficients for each individual 552 observation. The local Moran value I_i for each spatial unit is computed as 553 554 follows:

555
$$I_i = \frac{(x_i - \bar{x}) \cdot \sum_{j=1}^n w_{ij}(x_j - \bar{x})}{\sum_{i=1}^n (x_i - \bar{x})^2}$$

where x_i is the value of unit i (i.e. its d_{50} value or its b-axis size), x_j is the value of unit j, \bar{x} is the mean value of all units, w_{ij} is the weight that defines the relationship between units i and j ($w_{ij} = 1$ if j is a neighbour of i, $w_{ij} = 0$ otherwise) and n is the total number of spatial units. We assessed the statistical significance of each spatial unit's spatial

correlation with its neighbours (i.e. local Moran value), similarly to what 561 562 was done for the global Moran I. We computed a density function of the 563 local Moran for each spatial unit by running a Monte-Carlo simulation involving 999 random permutations (significance level of 0.05). In the 564 resulting LISA map, data were partitioned into five topological 565 relationships: 'high-high', 'low-low', 'low-high', 'high-low', and 'not 566 567 significant'. 'High-high' and 'low-low' indicated a positive spatial autocorrelation, which implies the presence of clustered high (respectively 568 569 low) values. 'Low-high' and 'high-low' indicated a negative spatial autocorrelation, implying a low value with a high-value neighbourhood 570 (respectively a high value with a low-value neighbourhood). 'Not 571 572 significant' indicated the absence of significant spatial autocorrelation. All spatial statistics were computed using the GeoDa software (Anselin et al., 573 574 2010).

576 **3. RESULTS**

577 Section 3.1 covers the results regarding the accuracy of digital grain sizing 578 methods. Section 3.2 presents the outcomes of the analysis of the grain-579 size spatial variability.

580 **3.1 Digital grain sizing accuracy**

581 Pairs of digitally and manually measured characteristic grain sizes are 582 presented in Figure 4 for the set of Fehr line samples collected during the field campaign. Grain size estimates from manual in-field line samples 583 were regarded as the reference "ground-truth" values when comparing 584 585 the performance of the different methods. Overall, the data pairs corresponding to digital manual labelling and their associated in-field 586 587 manual measurements proved to be mutually consistent. Grain size 588 estimates from digital manual labelling closely follow the 1:1 trend when 589 plotted against their in-field ground-truth counterparts (Figure 4). The 590 grain size estimates issued from GALET follow the 1:1 trendline with a 591 particularly-good agreement on the highest half of the grain size domain 592 for the d_m , d_{50} and d_{84} cases. However, the GALET estimates were often larger than the manual ones on the lowest half of the grain size domain 593 594 (Figure 4a, 4b and 4d).

595 PebbleCounts grain size estimates included three outliers. For the sake of 596 readability, the outliers were not plotted in Figure 4, as they differed 597 strongly from manually measured grain sizes for the d_m and d₈₄ grain sizes (their values ranged from 20 cm to 28 cm for the d_m grain size, and
from 42 cm to 62 cm for the d₈₄ grain size, see Figure S2 in Supporting
Information). These outliers arose because a large grain feature (b-axis >
40 cm) was detected in each of the three concerned samples. Such large
features resulted from the undersegmentation of sediment patches in
PebbleCounts.

When ignoring the above outliers, we found that PebbleCounts and
BASEGRAIN grain size estimates were often located under the identity line
in Figure 4. Particularly, the largest manually measured values were
systematically underestimated by BASEGRAIN and PebbleCounts routines

for all characteristic grain sizes.

609





612 sampling analysis performed. The black dashed line corresponds to the 1:1 trend.

614 The normalised grain size percentiles are presented in Figure 5. The median normalised grain size percentiles derived from manual labelling 615 616 are close to unity for all grain size percentiles. This indicates a good match with grain sizes issued from in-field manual sampling. The normalised 617 618 grain size percentiles computed by GALET were frequently in excess of the 619 grain size values derived from in-field manual measurements (median value above unity). This overestimation was particularly pronounced for 620 621 grain size percentiles smaller than d_{40} . Normalised grain size percentiles 622 obtained from BASEGRAIN and PebbleCounts (whose outliers were not 623 considered) underestimated grain size percentiles on average. This underestimation was less severe for larger grain size percentiles. If we 624 625 look at the q₂₅ and q₇₅ quartiles in Figure 5, the object-detection software 626 routines provide normalised grain size percentiles that are more scattered 627 in the lower half of the grain size percentiles (i.e. between d_5 and d_{50}) 628 than in the upper half, with a minimum scatter reached around the d_{80} grain size. This trend was also observed for manual labelling, but it was 629 630 less pronounced—the interquartile range of the normalised grain size 631 percentiles was relatively low compared to the object detection software 632 estimates.

The evolution of the NRMSE as a function of the grain size percentile is
presented in Figure 6. This error metric indicates that the digital
measurement procedures were most accurate around the d₈₄ grain size
percentile, except for PebbleCounts when its outliers were considered.
Grain sizes computed from digital manual labelling showed the lowest

NRMSE. Concerning the software routines, they exhibited mutually-similar error values for grain size percentiles between d_5 and d_{40} . Between the d_{40} and d_{90} grain sizes percentiles, GALET showed the lowest errors, whereas BASEGRAIN and PebbleCounts (without outliers) exhibited comparable higher NRMSE values. The NRMSE of grain size estimates of PebbleCounts was significantly reduced when removing the outliers from the error metric computation.



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Figure 5. Median normalised grain size percentile of each digital measuring procedure (thick line). The grain size percentiles were normalised by the in-field manually derived grain size percentiles (ddigital / dmanual). The q₂₅ and q₇₅ quartiles of the normalised digital estimates are represented by the dotted lines, meaning that 50% of the normalised estimates are located within the coloured area. Key grain size percentiles (i.e., d₁₆, d₅₀ and d₈₄) are indicated by vertical lines.



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Figure 6. Normalised Root Mean Squared Error (NRMSE) of each digital measuring procedures compared to in-field manual sampling, for each grain size percentile. Key grain size percentiles (i.e., d₁₆, d₅₀ and d₈₄) are indicated by vertical dotted lines.

658 **3.2 Spatial variability of grain sizes**

Given the performances of the GALET software and its capability to 659 process large orthoimages, we chose this tool to analyse the spatial 660 variability in surface grain sizes within the area D reach. Figure 7 shows 661 662 how heterogeneous the spatial distribution of surface grain sizes was over 663 area D. In particular, the d₅₀ estimates revealed important spatial 664 variations in the surface grain sizes over the study reach, with local d_{50} 665 estimates spanning from 2 cm to 40 cm (Figure 7b). Visual assessment 666 indicated that the grain size pattern identified in the map of d_{50} estimates 667 is consistent with the spatial distribution of grain sizes observed in the 668 orthoimage.

The Moran scatter plot (Figure 8) indicates that the spatial distribution of 669 670 d_{50} estimates in 2 × 2 m cells was characterised by a positive spatial autocorrelation. The test of significance suggested that the Moran's index 671 672 value I = 0.41 is statistically significant. The null hypothesis (stating that 673 d₅₀ estimates are randomly distributed across the space) was strongly rejected, as the computed pseudo-p-value resulted equal to 0.001 674 675 (meaning that no Moran's I computed via random permutations is as large 676 as the observed Moran's I). Therefore, the analysis of the Moran's I confirmed that sediments are sorted into patches of similar grain sizes on 677 678 the study reach.

679 The local indicator of spatial association (LISA) allowed us to locate680 statistically-significant clusters of large (high-high) and small (low-low)

681 d50 estimates (Figure 7c). Clusters are sets of contiguous units that 682 exhibit significant and similar spatial associations (Anselin, 1995). 683 Relatively few cells showed negative spatial autocorrelation (i.e. significant low-high or high-low spatial associations with their neighbours). 684 685 Among the clusters identified on the LISA map, three are highlighted in 686 Figure 7c, which makes it possible to compare their location with that of the clusters identified at the grain scale in Figure 10. Note that given their 687 size and morphology, these clusters are generally referred to as "patches" 688 689 in the gravel-bed literature (e.g., Lisle and Madej, 1992; Dietrich et al., 2006). We use the term "cluster" thereafter for consistency with the 690 691 definition used in the field of spatial statistics given by Anselin (1995).

692 To study the spatial variability in the grain sizes within a single 693 geomorphological unit at the grain scale, we selected the detected 694 features located over a gravel bar in area D (Figure 10). Moran's I computed from the resulting dataset indicates that the spatial grain size 695 696 distribution was characterised by a positive autocorrelation (Figure 9). The 697 Moran's index value I = 0.12 was statistically significant, as the null 698 hypothesis of random spatial distribution of grain sizes was strongly 699 rejected (pseudo-p-value = 0.001). The positive Moran's I value indicated that the surface stones were generally clustered according to their 700 dimensions in the surveyed river reach. The large number of grain 701 702 features presented in the Moran scatter plot and the relatively weak 703 correlation makes it difficult to visually detect a clear trend in the data 704 scatter around the linear regression line (Figure 9). The smallest

705 standardised b-axis values are located within one standard deviation from 706 the origin. This indicates that the grain-size distribution was largely 707 skewed towards fine particles (approximately 70% of the detected particles were smaller than the mean b-axis value of 6.2 cm). We recall 708 709 that the amount of information related to the finer grain sizes was 710 hindered by the image resolution. The smallest particles which could be 711 detected by GALET were of 2 cm in diameter; this limitation imposed a 712 lower bound in the data scatter.

The cluster map generated from the LISA allowed us to visualise different 713 714 grain size clusters (Figure 10). A complex pattern of different surface 715 grain sizes was observed on this bar, where the clusters 1, 2 and 3 716 identified in Figure 7c are located. It is worth recalling that LISA outcomes 717 and cluster identification could be influenced, to a certain degree, by the characteristics of the data sample considered (e.g., size and internal 718 variability). The clusters identified from the LISA map computed from d_{50} 719 720 estimates on a grid matched reasonably well-in location and extent-721 those identified from the LISA analysis based on discrete grain features (Figure 10). This good agreement means that, in our case, the dataset of 722 samples located on the single geomorphological unit considered were 723 724 highly representative of the grain size distribution over the entire area D.



c) Local indicator of spatial association of $d_{\rm 50}$ estimates.

Figure 7. Maps of the spatial distribution of d_{50} estimates. (a) Orthoimage of area D on 11 Nov 2022, with discharge of 1.2 m³/s. The water flows northwise. (b) d_{50} estimates based on detected grain features by GALET in 2 × 2 m grid cells. (c) Cluster (i.e. patches) identification using the local indicator of spatial association (based on the local Moran's I), three clusters are indicated for further discussion.



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Figure 8. Moran scatter plot for the measure of the overall size clustering tendency of the grid d_{50} estimates. The mean standardised d_{50} estimates of neighbouring cells are plotted against the standardised d_{50} estimates. The global Moran's I corresponds to the

r36 slope value of the regression line (dashed red line).

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Figure 9. Moran scatter plot for the measure of the size clustering tendency of grain
features. The mean standardised b-axis estimates of the 100-nearest neighbouring
stones are plotted against the standardised b-axis of the 125'000 detected stones by

742 GALET. The global Moran's I corresponds to the slope of the regression line (dashed red

743 line).



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Figure 10. Particle-size clusters (i.e. patches) identification using a local indicator of spatial association (local Moran's I). The region of interest is a single gravel bar located in area D. The contours of the clusters 1,2 and 3, as identified from the LISA map for d₅₀ data, are plotted for comparison (solid black lines).

749 **4. DISCUSSION**

The accuracy of digital manual labelling and of object-based grain sizing methods compared to in-field line sampling is discussed in Sections 4.1 and 4.2, respectively. Section 4.3 addresses how spatial statistics of detected grain features can be used to describe the spatial organisation of surface grain sizes.

755 **4.1 Digital manual labelling accuracy**

756 The characteristic grain size values derived from manual labelling of orthoimages showed a great similarity with the values derived from in-757 758 field manual sampling (Figure 4 and 5). This similarity contrasts with 759 previous studies on manual labelling of individual grains in photographs, 760 which found that grain sizes were generally underestimated compared to in-field sampling results (e.g., Adams, 1979; Ibbeken and Schleyer, 1986; 761 Church, 1987; Garefalakis et al., 2023). These authors linked this 762 763 underestimation to the partial information accessible in photography-764 based grain sizing methods, since only the exposed part of grains is visible 765 in nadir photographs. Partial burying of grains, grain imbrication or 766 foreshortening of grains due to the angle of the photograph can lead to underestimate the true grain sizes (Graham et al., 2010). 767

In our study, grain size percentiles derived from digital manual labelling did not suffer from underestimation, most likely because it was difficult to identify smallest particles (b-axis < 2 cm approximately) owing to the orthoimage resolution or to their location in-between coarser particles.

The weak detection of finest particles resulted in different calibrations of 772 the Fuller curves that describe the lower end of the GSDs and probably led 773 774 to higher NRMSE values for grain size percentiles in the d_{10} - d_{40} range (Figure 6). In our samples, percentiles smaller than d₁₀ corresponded to 775 776 grain sizes smaller than 1 cm and no grain-sizing method (including in-777 field sampling) provided direct measurements for such small grains. 778 Therefore, under d₁₀, the Fuller interpolation in the Fehr method completely determined the grain-size percentiles, made the GSD tails 779 780 mutually-similar and provided lower NRMSE values. The undersampling of fine grains likely counterbalanced the size underestimation for the largest 781 particles, thus providing average grain size estimates that were similar to 782 783 those derived from in-field manual sampling. It is worth mentioning that manual labelling was performed by a single operator and we did not 784 785 investigate how the results may differ depending on the operator.

786 **4.2** Accuracy of object-based grain sizing methods

787 Comparing the three software routines (BASEGRAIN, GALET and 788 PebbleCountsAuto) revealed differences in accuracy and limitations. 789 GALET tends to overestimate in-field grain sizes issued from line 790 sampling. The main explanation for this phenomenon is that GALET did 791 not detect the smallest grains (b-axis < 2-3 cm). Mörtl et al. (2022) noted that the resolution of orthoimages determines the smallest 792 detectable grain size by GALET. The resolution of the generated 793 794 orthoimages (approximately 0.3 cm/px) was likely too low for the

detection of the smallest grains. Fine grained samples (with d_m smaller
than 7 cm, Figure 4a) were therefore particularly affected by the absence
of small grains in GALET grain size estimates and thus led to
overestimated values. To reduce the detection limit for small grains,
shorter ground sampling distances would be required.

Visual inspection of the grain features detected by GALET suggested that 800 801 the software performance was not affected by different rock texture 802 patterns inside individual grains. The CNN training dataset used by Mörtl 803 et al. (2022) is probably well suited to applying the routine to the 804 Navisence bed images. A significant number of grains was not detected in 805 the GALET routine. Overall, GALET detected 40% less grain features, regardless of their size, along the lines compared to the manual labelling 806 807 conducted by a human operator. The largest grains (b-axis > 20 cm) 808 sometimes appeared over-segmented by a vertical or horizontal line. This feature splitting was caused by the edges of the finite-size moving window 809 810 used for grain feature detection in GALET. This issue did not arise with 811 large grain features along the lines, but it could lead to a size 812 underestimation for some of the largest stones present in the river bed.

BASEGRAIN and PebbleCounts produced similar results, as both software routines generally underestimated characteristic grain sizes. For three sampling lines, PebbleCounts outcomes were affected by several feature merging occurrences and missed grain detections (the outliers mentioned in Section 3.1). These errors were likely caused by glacial flour, which 818 partially covered pebbles. This led to a large overestimation of grain size 819 percentiles for these lines. The grain sizes of the other lines were 820 generally underestimated because the largest stones were often not 821 detected, which may be due to the presence of intergranular textures that 822 prevented optimal edge detection. In addition, direct sun illumination on 823 orthoimage C caused size underestimation of the detected stones, as the 824 shaded grain faces were not included in the detected object boundaries. 825 Finally, we observed that the grain masks identified by PebbleCounts were 826 generally smaller than the apparent size of stones in the orthoimages. 827 This shortcoming in PebbleCounts led to grain size underestimation. PebbleCounts showed a poor detection rate along the lines on the 828 829 orthoimages, as the number of grain features detected is 62% smaller 830 than that resulting from manual labelling.

Concerning BASEGRAIN, rock-texture variations inside single grains (e.g. 831 due to foliation or veins) can be detected as grain edges during the 832 833 segmentation procedure. Therefore, large particles often appeared over-834 segmented. This resulted in the detection of several smaller particles instead of a single large particle. These over-segmentation errors were 835 less frequent for small particles, whose detection was less influenced by 836 rock texture details—apparently because of the limited image resolution. 837 BASEGRAIN suffered from the same problem identified in PebbleCounts: it 838 839 often did not merge shaded grain-surfaces into the object boundaries. This resulted in underestimation of the real size of grain features. Rock 840 texture variations induced BASEGRAIN to detect fictitious edge patterns. 841

Non-detection of large particles might arise when BASEGRAIN was unable
to reconstruct a closed grain boundary from these edge patterns. The
large number of tunable parameters in BASEGRAIN makes the
performance highly dependent on the operator's choices. Meticulous
parameter tuning and visual checks of the quality of the object detection
were performed in the present study, but it cannot be excluded that
different operators could have obtained different results.

Systematic grain size underestimation from automated image-based
methods induced by rock texture is an issue pinpointed by earlier studies
(e.g., Strom et al., 2010). We found that PebbleCounts results were
relatively less influenced by rock texture patterns than BASEGRAIN ones.
Over-segmentation errors with BASEGRAIN may be even more severe
when no parameter tuning is performed (see Chardon et al., 2022).

855 Among the routines considered here, GALET, based on deep-learning for object detection, emerged as the best-suited tool for grain size analysis 856 857 when studying gravel bars from orthoimages. GALET was designed to fit 858 the wide range of rock texture found in gravel-bed rivers and to conduct 859 grain feature detection on long stream reaches. The object-detection 860 performances of deep-learning methods (see Zhao et al., 2019), the recent implementation of deep learning in object-based grain-sizing 861 techniques (e.g., Soloy et al., 2020; Chen et al., 2022) and the results of 862 863 the present study indicate that the deep-learning technology may enable a 864 step forward in automated optical granulometry.

4.3 Spatial variability of grain sizes

In Section 3.2, we provided quantitative information about the grain-size 866 867 variability along the study reach. We conducted a statistical analysis on 868 the d_{50} grid estimates and on the grain features detected by GALET. The accuracy evaluation of GALET revealed that this software performs at its 869 870 best for grain size percentiles above d_{40} . Therefore, the d_{50} map presented 871 in Figure 7 and the associated identified clusters should correspond closely 872 to the real grain size variability on the field. Our analysis demonstrated 873 how variable the bed-surface material size was in the surveyed floodplain. 874 We found that grains were arranged in patches (i.e. spatial clusters), 875 consistently with what has been observed for bars in gravel-bed rivers 876 (e.g., Dietrich, 2006; Guerit et al., 2014).

878 **5. CONCLUSIONS**

We presented a benchmarking study of three object-based grain sizing 879 880 models (BASEGRAIN, PebbleCountsAuto, and GALET) on a mountain river 881 bed. The main difference between them was that GALET uses deep 882 learning technology whereas the two others are based on image 883 thresholding for grain segmentation. The three methods were applied to 884 orthoimages obtained from UAV surveys and Structure-from-Motion 885 photogrammetry. In-field estimates of grain sizes obtained using Fehr's 886 line sampling technique served as a reference dataset to evaluate the 887 accuracy of each grain sizing method. We supplemented the comparison by manually labelling grain features on the same orthoimages. By 888 computing the grain size distributions within Fehr's (1987) framework, we 889 890 ensured that all methods were comparable on the same footing.

Manual labelling provided estimates that were fully consistent with field measurements. BASEGRAIN and PebbleCountsAuto underestimated grain sizes on average, whereas GALET generally overestimated grain size percentiles.

We identified some limitations in the three models. BASEGRAIN often led to over-segmentation in grain features due to the rock-texture influence on object detection. PebbleCountsAuto outcomes were often affected by missed detections of large grains. Shaded grain faces and glacier flour also influenced grain detection in PebbleCountsAuto. The available image 900 resolution prevented the detection of the smallest grain features with901 GALET.

Our case study confirms that automated grain-size measurement methods 902 are cost-effective solutions for monitoring river-surface grain sizes with 903 904 high spatial coverage. Such automated techniques are expected to 905 progress in upcoming years with the advent of new grain-sizing procedures based on the deep learning technology. 906 907 We studied how grain sizes were distributed over the bed surface, by mapping characteristic grain sizes variations. Computing Moran's I and 908 909 LISA statistics revealed a significant grain-size clustering and the location 910 of such grain-size patches (i.e. spatial clusters).. We believe that the

911 combined use of automated grain sizing techniques (applied to large scale

912 orthoimages) and spatial statistics will give a new impetus to

913 understanding the processes that drive sediment sorting in gravel-bed914 rivers.

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