Rheophysical Investigation in Concentrated Particle Suspensions

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Abstract. An optical visualization apparatus has been designed to measure the particle-velocity and solid-concentration profiles of highly concentrated coarse-particle suspensions in a wide-gap Couette rheometer. The main objective is to investigate the frictional-viscous transition, a phenomenon that has been already reported in recent papers [1–4], but still remains partially understood. For wide-gap viscometers and complex fluids, a related issue is the Couette problem, which underpins the rheometrical treatment for viscometric flows in coaxial-cylinder rheometers; we compare shear-rate computations obtained by solving the Couette problem (bulk estimate) and by differentiating the velocity and concentration profiles (local measurement).

Keywords: Granular matter, non-colloidal suspensions, frictional-collisional transition, rheophysics, fluorescent particle image velocimetry

PACS: 47.57.E-, 45.70.-n, 45.70.Ht, 45.70.Mg

INTRODUCTION

A large number of natural gravity-driven geophysical flows involve suspensions of particles in a fluid. Typical examples include debris flows, snow avalanches, turbidity currents, pyroclastic flows, etc. A longstanding practice is to consider these suspensions as one-phase or two-phase continua on the bulk scale, which makes it possible to use a fluid-mechanics treatment to compute the motion features (velocity, flowdepth, spreading, etc.). The constitutive equation of granular suspensions of particles is known only for limiting flow conditions, where only one type of particle contact prevails. Examples include kinetic theories used to infer motion equations for rapidly sheared flows of particles [5]. In this case, we consider that the main interactions between particles are collisions and the part played by the fluid phase in the generation of stress can be disregarded. Likewise, in the viscous regime the particles interactions are mainly lubricated contacts, in which both the particles and the fluid play a key role. Finally, the frictional behavior exhibited at very low shear rates is usually modeled using the phenomenological law of Coulomb [6, 7]. In this case, it is shown that the bulk stresses result from sustained contacts between particles, which carry frictional forces throughout the bulk [8]; the role of the fluid phase is mainly limited to the fluid pressure in the pores. In many practical cases of interest, the flow regime is intermediate between two limiting regimes; the interplay of two interactions gives rise to more complicated behaviors, which are yet partially understood. For the frictional-viscous transition, Ancey [3] suggested that particle lubrication is the key mechanism. It occurs at a given critical shear rate, which depends on the particle diameter: at sufficiently high shear rates, fluid inertia increases; part of the fluid can then break and lubricate contacts between particles, which leads to a “fluidization of the material”. Another interpretation has been suggested by geophysicists [9]: a concentrated suspension of coarse non-buoyant particles behaves like a soil and according to Coulomb theory, shear strength drops to zero when pore fluid pressure is sufficiently high to balance particle buoyancy forces, which results in a “liquefaction” of the material.

When studying rheological properties of particle suspensions, experimentalists are faced with a number of issues resulting from the presence of particles. For many noncolloidal particle suspensions, the typical particle size is large relative to the standard rheometer gap. In practice, to avoid finite-size effect, a classical approach involves using large-size geometries, e.g., wide-gap Couette cells. For this kind of geometry, the so-called Couette inverse problem has to be solved using specific methods [10–15] as the thin gap approximation is no longer valid. An alternative way of obtaining the flow curve is to measure the velocity profile across the gap, then differentiate it to derive the local shear rate. The locally derived measurements (shear rate, concentration) can finally be used as benchmark data to test out the various techniques developed for solving the Couette inverse problem (e.g., Tikhonov regularization, spline interpolation, wavelet-vaguelette decomposition). We will present the results of this benchmark.
A CLEAR AND HIGHLY CONCENTRATED COARSE-PARTICLE SUSPENSION

To gain insight into the delicate questions concerning the frictional-viscous transition and the associated Couette inverse problem, we are conducting experiments with an iso-index (clear) particle suspension [16–19]. The suspensions is made up of spherical PMMA particles of 200μm within a mixture of three Newtonian miscible fluids to control both the buoyancy forces and refractive index [see Fig.1]. Care must be taken in the preparation of the suspension and the rheometrical experiments to control precisely the fluid temperature because the particle buoyancy and the refractive index matching are strongly dependent of it. To optimize the suspension at the 532 nm used laser wavelength the procedure shown on Fig.2 is performed so as to maximize the transmitted light energy. Tagging the particles with rhodamine 6G a fluorescent dye, we use a non-invasive fluorescent particle image velocimetry (FPIV) technique to obtain the velocity and concentration profiles.

**particle properties**
- sphericity
- granulometry
- excellent optical properties

**fluid properties**
- compatibility with PMMA (wetting and chemical interaction)
- low light absorbtion and excitation

**FIGURE 1.** Particle suspension properties

**FIGURE 2.** Schematic diagram of the turbidity experiment

**EXPERIMENTAL FACILITY**

The facility is made up of a 2.4-m-long optical table, a second harmonic Nd:YAG laser (532 nm), and a Bohlin Gemini 200 rheometer [see Fig. 3(a)]. The rheometer tools are an inner cylinder or a vane (diameter 25 mm) and an outer quartz cup (60mm in diameter). As shown on Fig. 3(b), an horizontal laser light sheet cuts the Couette cell at different given heights. The laser light excite the fluorescence of the rhodamine-impregnated particles. The emitted fluorescent light in the 550-nm to 580-nm range is then recorded with a CCD camera at 30 fps. Scattered laser light is blocked by a high-pass optical filter placed in front the camera. Using fluorescent particle image velocimetry (FPIV) and particle tracking techniques (FPTV) to process the images, we finally deduce the velocity and concentration fields.

**FIGURE 3.** (a) the rheo-optical facility, (b) sketch of the local measurement technique
PRELIMINARY RESULTS

For validation purpose, we used the Newtonian three-fluid mixture and same PMMA particles as seeding particles for the PIV/PTV treatment. As shown in Fig. 4, good agreement is found for the velocity profiles between the experiment and exact analytical solution. At the moment, experiments with highly concentrated suspensions are in progress.

![Graph showing velocity profile comparison]

**FIGURE 4.** Validation velocity profile comparison in the wide-gap Couette cell for a Newtonian fluid, \(\frac{v_\theta}{v_{\theta,in}}\) is the non-dimensionalized tangential velocity and \(\frac{v_r}{v_{\theta,in}}\) is the non-dimensionalized radial velocity.

ACKNOWLEDGMENTS

The work presented here was supported by the Swiss National Science Foundation under grant number 200021-105193/1 and specific funds provided by EPFL (vice-présidence à la recherche).

REFERENCES