

Fluid avalanches

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Outline

- Context: the dam-break problem
- Laboratory insight: flow visualization
 - Newtonian flow
 - Viscoplastic material
 - Concentrated particle suspension
- Summary and references

Introduction

- **The dam-break problem**

- Scientific issues
- Induced sediment transport
- Related phenomena
- Muddy debris flow
- Glide avalanches
- Laboratory avalanches

Newtonian fluids

Viscoplastic material

Concentrated particle suspension

Conclusions

The dam-break problem

In engineering, dam break: sudden release of water



Teton dambreak (Idaho, 1976)

Scientific issues

Introduction

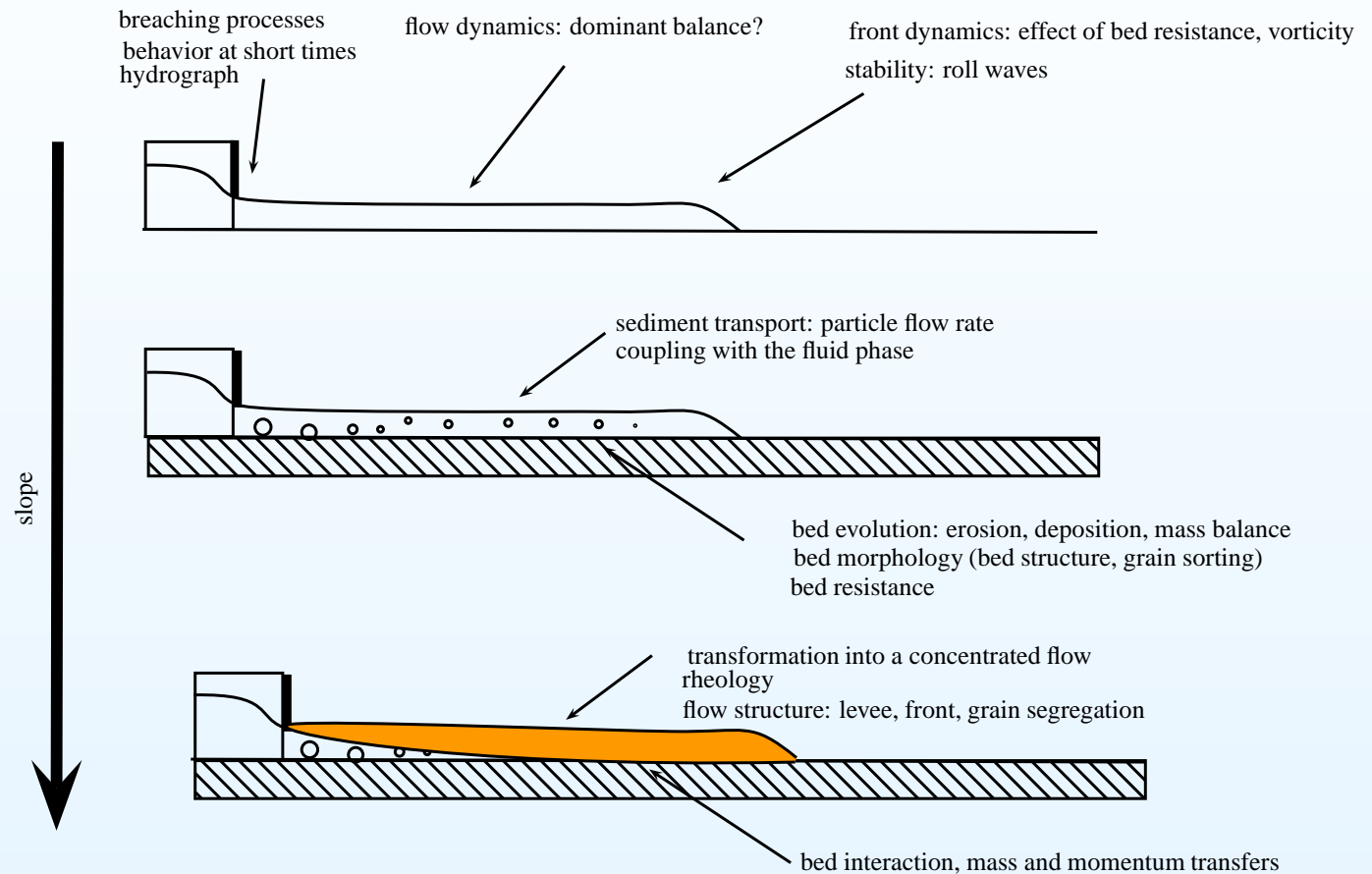
- The dam-break problem
- **Scientific issues**
- Induced sediment transport
- Related phenomena
- Muddy debris flow
- Glide avalanches
- Laboratory avalanches

Newtonian fluids

Viscoplastic material

Concentrated particle suspension

Conclusions



Introduction

- The dam-break problem
- Scientific issues
- **Induced sediment transport**
- Related phenomena
- Muddy debris flow
- Glide avalanches
- Laboratory avalanches

Newtonian fluids

Viscoplastic material

Concentrated particle suspension

Conclusions

Induced sediment transport

Taum Sauk dam break
(Missouri, Dec. 2005)
intense erosion of the bed
(down to the bed rock) and
sediment transport



Related phenomena

Introduction

- The dam-break problem
- Scientific issues
- Induced sediment transport
- **Related phenomena**
- Muddy debris flow
- Glide avalanches
- Laboratory avalanches

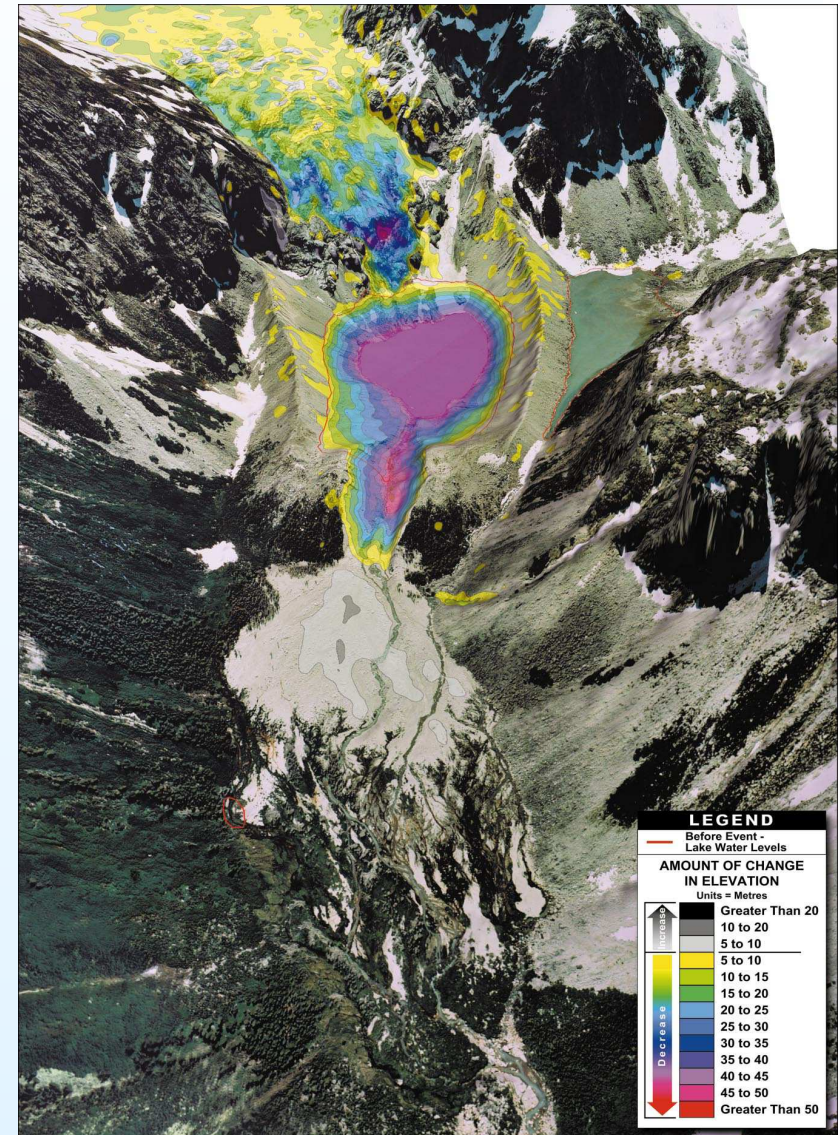
Newtonian fluids

Viscoplastic material

Concentrated particle suspension

Conclusions

Outburst flood: Lake Nostetuko (British Columbia, Canada) July 1983



Muddy debris flow

Introduction

- The dam-break problem
- Scientific issues
- Induced sediment transport
- Related phenomena
- **Muddy debris flow**
- Glide avalanches
- Laboratory avalanches

Newtonian fluids

Viscoplastic material

Concentrated particle suspension

Conclusions



Glide avalanches

Introduction

- The dam-break problem
- Scientific issues
- Induced sediment transport
- Related phenomena
- Muddy debris flow
- **Glide avalanches**
- Laboratory avalanches

Newtonian fluids

Viscoplastic material

Concentrated particle suspension

Conclusions



Laboratory avalanches

Introduction

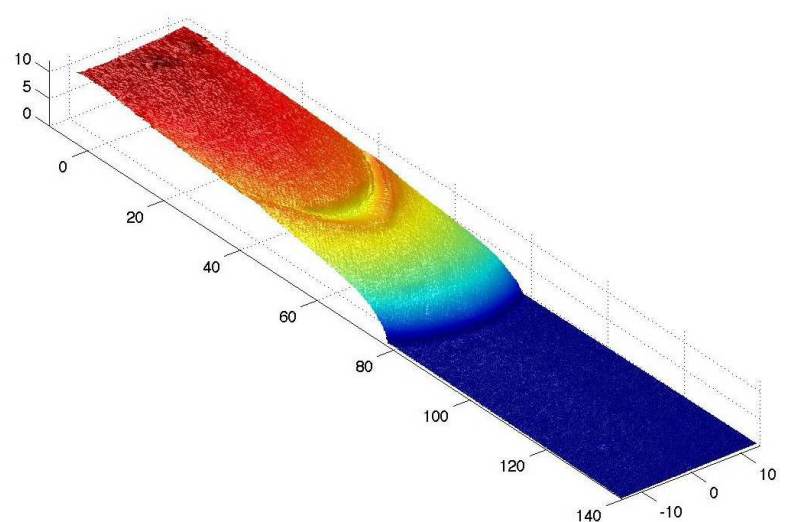
- The dam-break problem
- Scientific issues
- Induced sediment transport
- Related phenomena
- Muddy debris flow
- Glide avalanches
- **Laboratory avalanches**

Newtonian fluids

Viscoplastic material

Concentrated particle suspension

Conclusions



Introduction

Newtonian fluids

- The dam-break problem
- Navier-Stokes equations
- Flow regimes
- Diffusive regime
- Diffusive regime at $t \ll 1$
- Diffusive regime at $t \gg 1$
- Comparison with experiments

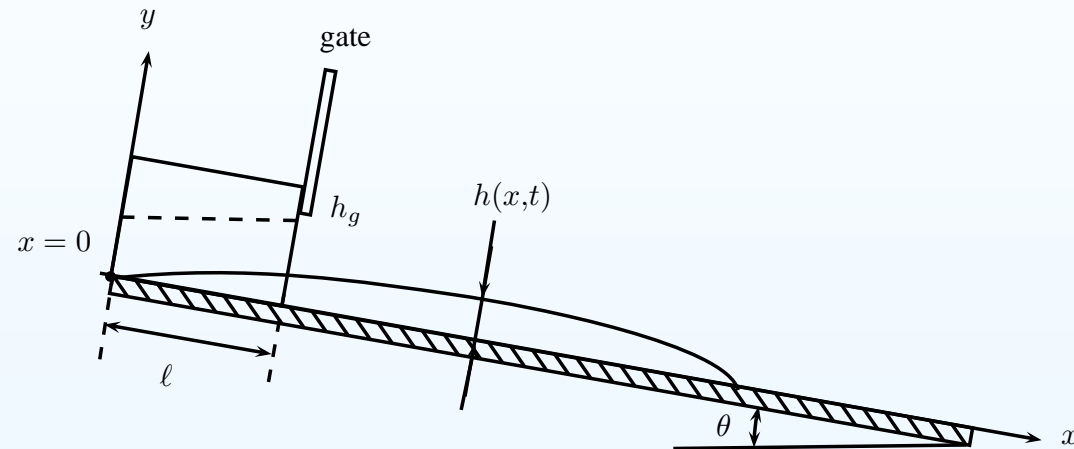
Viscoplastic material

Concentrated particle suspension

Conclusions

The dam-break problem

Release of a fixed volume of fluid



Questions:

- Front position over time $x_f(t)$?
- Flow depth profile $h(x,t)$?
- Velocity profile within the flow (far from the sidewall) ?
- Further questions: stability, slip, influence of surface tension, etc.

Introduction

Newtonian fluids

- The dam-break problem

• Navier-Stokes equations

- Flow regimes
- Diffusive regime
- Diffusive regime at $t \ll 1$
- Diffusive regime at $t \gg 1$
- Comparison with experiments

Viscoplastic material

Concentrated particle suspension

Conclusions

Navier-Stokes equations

Dimensionless form

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0,$$

$$\epsilon \text{Re} \frac{du}{dt} = \phi \cos \theta \left(\tan \theta - \epsilon \frac{\partial p}{\partial x} \right) + \epsilon^2 \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2},$$

$$\epsilon^2 \text{Re} \frac{dv}{dt} = -\phi \cos \theta \left(1 + \frac{\partial p}{\partial y} \right) + \epsilon^3 \frac{\partial^2 v}{\partial x^2} + \epsilon \frac{\partial^2 v}{\partial y^2},$$

with $\phi = \rho g H_*^2 / (\mu U_*)$ a dimensionless group and $\epsilon = H_* / L_* \ll 1$ the aspect ratio.

$Ca = \mu U_* / \gamma \gg 1$ and $Re = \rho U_* H_* / \mu \ll 1$: capillary and Reynolds numbers.

L_* and H_* selected so that $L_* H_* = \tilde{V}$, viz, $L_* = \sqrt{\tilde{V} / \epsilon}$ and

$$H_* = \sqrt{\epsilon \tilde{V}}$$

Introduction

Newtonian fluids

- The dam-break problem
- Navier-Stokes equations
- **Flow regimes**
- Diffusive regime
- Diffusive regime at $t \ll 1$
- Diffusive regime at $t \gg 1$
- Comparison with experiments

Viscoplastic material

Concentrated particle suspension

Conclusions

Flow regimes

Dominant balance:

- *Diffusive regime.* Balance between the pressure and shear stress gradients : $U_* = \rho g H_*^3 / (3\mu L_*)$ and $\phi = 3/\epsilon$
- *Advection diffusion regime.* Balance between the body force and shear stress gradient + pressure gradient within the leading edge: $\epsilon = \tan \theta$, $U_* = \rho g H_*^2 \sin \theta / (3\mu)$, and $\phi = 3/\sin \theta$
- *Steep slope regime.* Increasing role of the body force: $\epsilon = \tan^2 \theta$, $U_* = \rho g H_*^2 \sin \theta / (3\mu)$, and $\phi = 3/\sin \theta$

Introduction

Newtonian fluids

- The dam-break problem
- Navier-Stokes equations
- Flow regimes
- **Diffusive regime**
- Diffusive regime at $t \ll 1$
- Diffusive regime at $t \gg 1$
- Comparison with experiments

Viscoplastic material

Concentrated particle suspension

Conclusions

Diffusive regime

Diffusive regime observed for $Ca \rightarrow \infty$, $Re = O(1)$, and $\theta \ll 1$.
Dimensionless governing equation for $\theta > 0$

$$\frac{\partial h}{\partial t} + \frac{\partial h^3}{\partial x} = \frac{\partial}{\partial x} \left(h^3 \frac{\partial h}{\partial x} \right).$$

Dimensionless governing equation for $\theta = 0$

$$\frac{\partial h}{\partial t} = \frac{\partial}{\partial x} \left(h^3 \frac{\partial h}{\partial x} \right).$$

No analytical solution (available), but asymptotic solutions at short or long times t with the following change of variable

$$h(x, t) = t^{-n} H(\xi, t)$$

- short-time solution: $n = 1/5$ (Nakaya, 1974 ; Huppert, 1982) ;
- long-time solution: $n = 1/3$ (Huppert, 1982 ; Lister, 1982).

Introduction

Newtonian fluids

- The dam-break problem
- Navier-Stokes equations
- Flow regimes
- Diffusive regime
- **Diffusive regime at $t \ll 1$**
- Diffusive regime at $t \gg 1$
- Comparison with experiments

Viscoplastic material

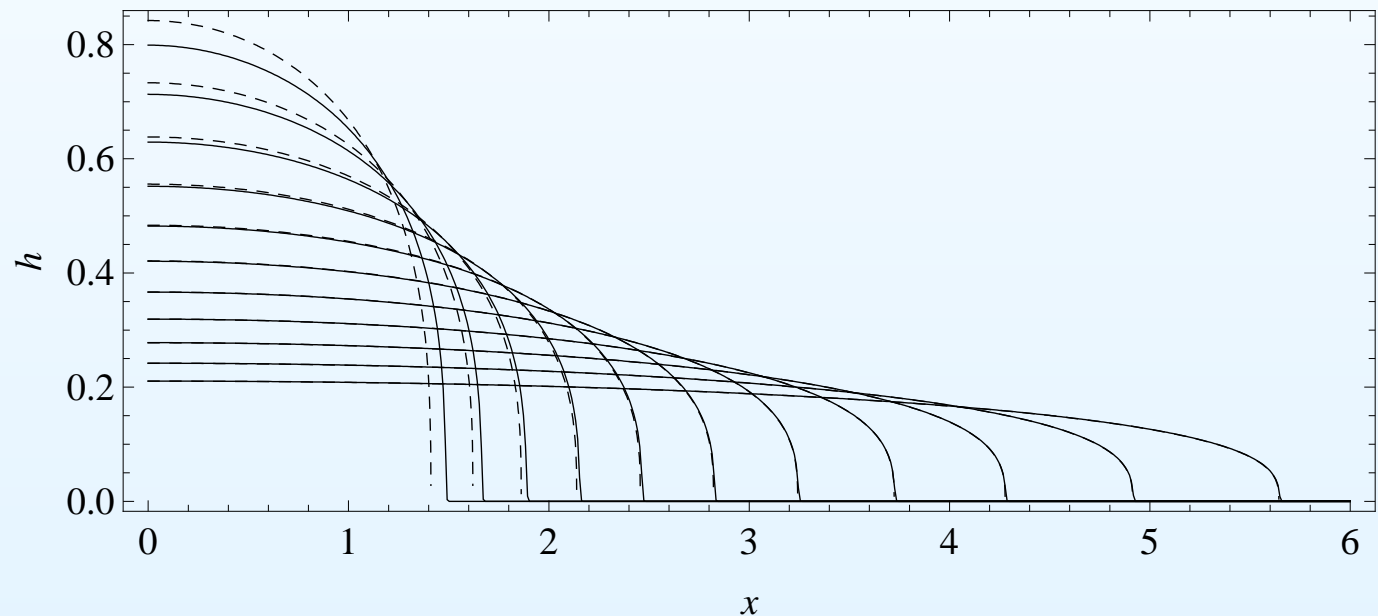
Concentrated particle suspension

Conclusions

Diffusive regime at $t \ll 1$

Huppert's (or Barrenblatt-Pattle's) solution

$$h(x, t) = t^{-1/5} \left(\frac{3}{10} (\xi_f^2 - \xi^2) \right)^{1/3} \text{ avec } \xi_f = V_0^{3/5} \left(\frac{\sqrt[3]{\frac{3}{10}} \sqrt{\pi} \Gamma\left(\frac{1}{3}\right)}{5\Gamma\left(\frac{5}{6}\right)} \right)^{-3/5}$$



Comparison between the numerical solution and Huppert's self-similar solution at $t = 1, 2, 4, 8, 16, 32, 64, 128, 256, 512, \text{ and } 1024$

Introduction

Newtonian fluids

- The dam-break problem
- Navier-Stokes equations
- Flow regimes
- Diffusive regime
- Diffusive regime at $t \ll 1$
- **Diffusive regime at $t \gg 1$**
- Comparison with experiments

Viscoplastic material

Concentrated particle suspension

Conclusions

Diffusive regime at $t \gg 1$

Huppert's solution (+ higher-order terms Ancey, JFM 2009)

$$h(x, t) = t^{-1/3} \left(\sqrt{\frac{1}{3} \frac{x}{t^{1/3}}} + K_0 \left((\xi_f - x t^{1/3}) t^{2/3} \right) - \sqrt{\frac{\xi_f}{3}} \right).$$

with the position of the front given by

$$x_f = \xi_f t^{1/3} + \left(\log 2 - \frac{1}{2} \right) \sqrt{\frac{\xi_f}{3}} t^{-1/3},$$

with

$$\xi_f = \left(\frac{3\sqrt{3}}{2} V \right)^{2/3}$$

This solution requires a boundary-layer treatment at the front as the diffusive effects (pressure gradient) prevail over the advection term.

Introduction

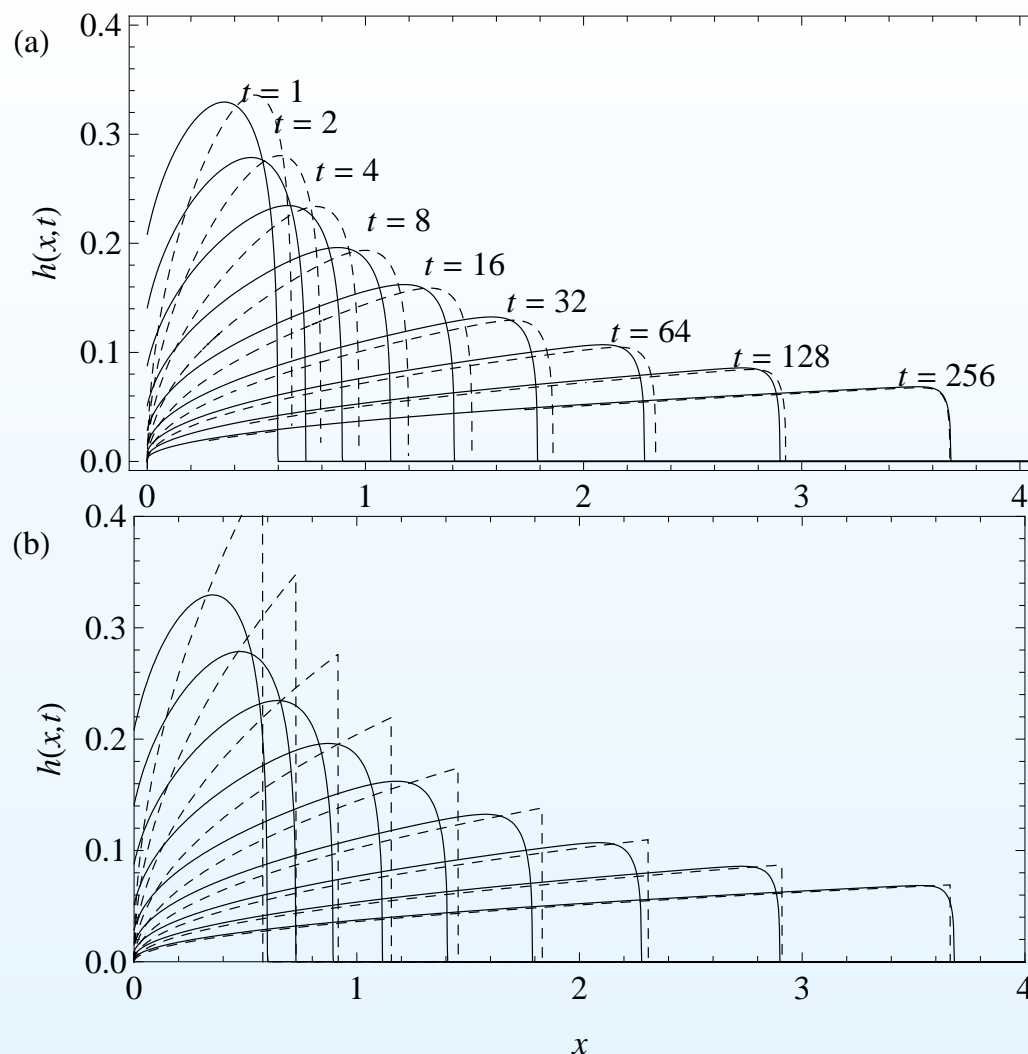
Newtonian fluids

- The dam-break problem
- Navier-Stokes equations
- Flow regimes
- Diffusive regime
- Diffusive regime at $t \ll 1$
- Diffusive regime at $t \gg 1$
- Comparison with experiments

Viscoplastic material

Concentrated particle suspension

Conclusions



Comparison of flow depth profiles: numerical solution (solid line) and asymptotic solution (dashed line), with diffusion included (a) or not (b), for slope $\theta = 6^\circ$, at times $t = 1, 2, 4, 8, 16, 32, 64, 128, 256$.

Introduction

Newtonian fluids

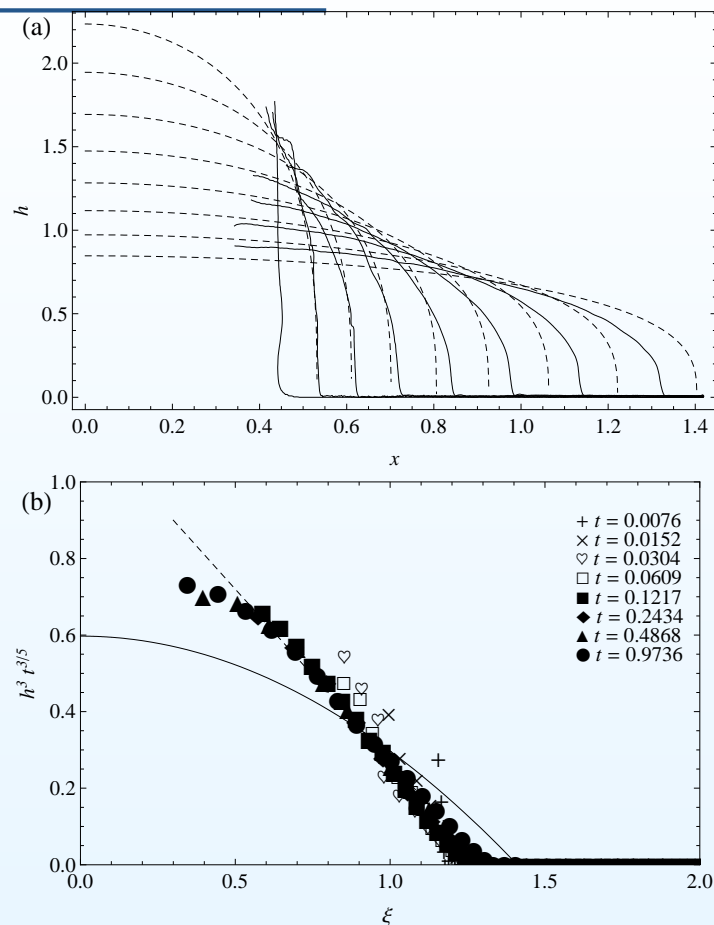
- The dam-break problem
- Navier-Stokes equations
- Flow regimes
- Diffusive regime
- Diffusive regime at $t \ll 1$
- Diffusive regime at $t \gg 1$
- Comparison with experiments

Viscoplastic material

Concentrated particle suspension

Conclusions

Comparison with experiments



Comparison of flow depth profiles for $\theta = 0^\circ$. For (b), we show the self-similar solution and the experimental trend
 $(h/t^{-1/5})^3 = \frac{9}{10}(1.3 - \xi)$. Fluid: glucose ($\mu = 345 \text{ Pa s}$)

Introduction

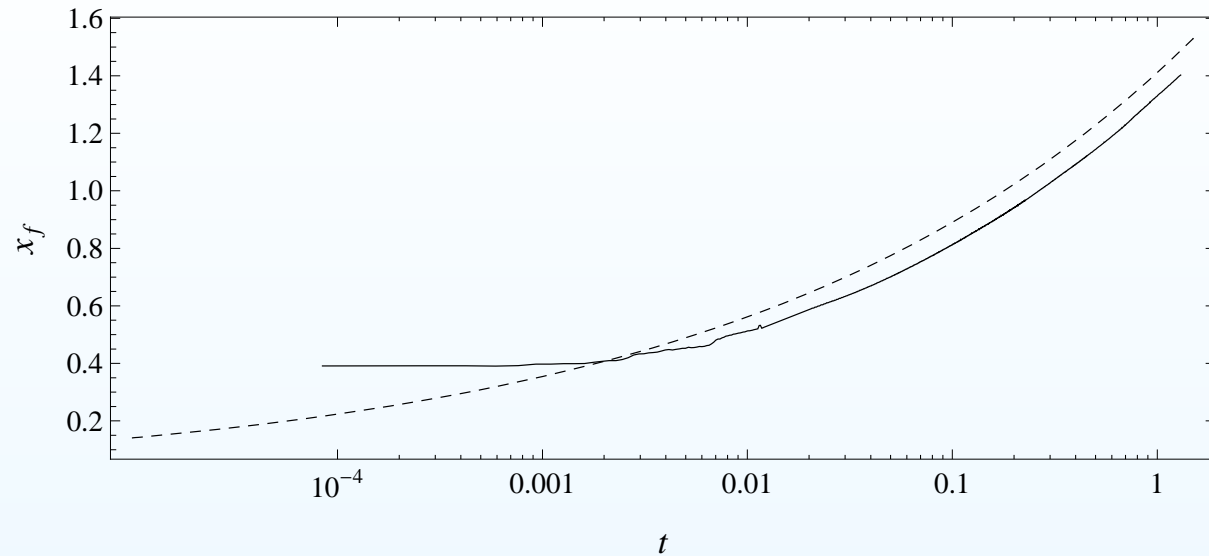
Newtonian fluids

- The dam-break problem
- Navier-Stokes equations
- Flow regimes
- Diffusive regime
- Diffusive regime at $t \ll 1$
- Diffusive regime at $t \gg 1$
- Comparison with experiments

Viscoplastic material

Concentrated particle suspension

Conclusions



Front position over time: experimental data (solid line) and theory (dashed line)

Introduction

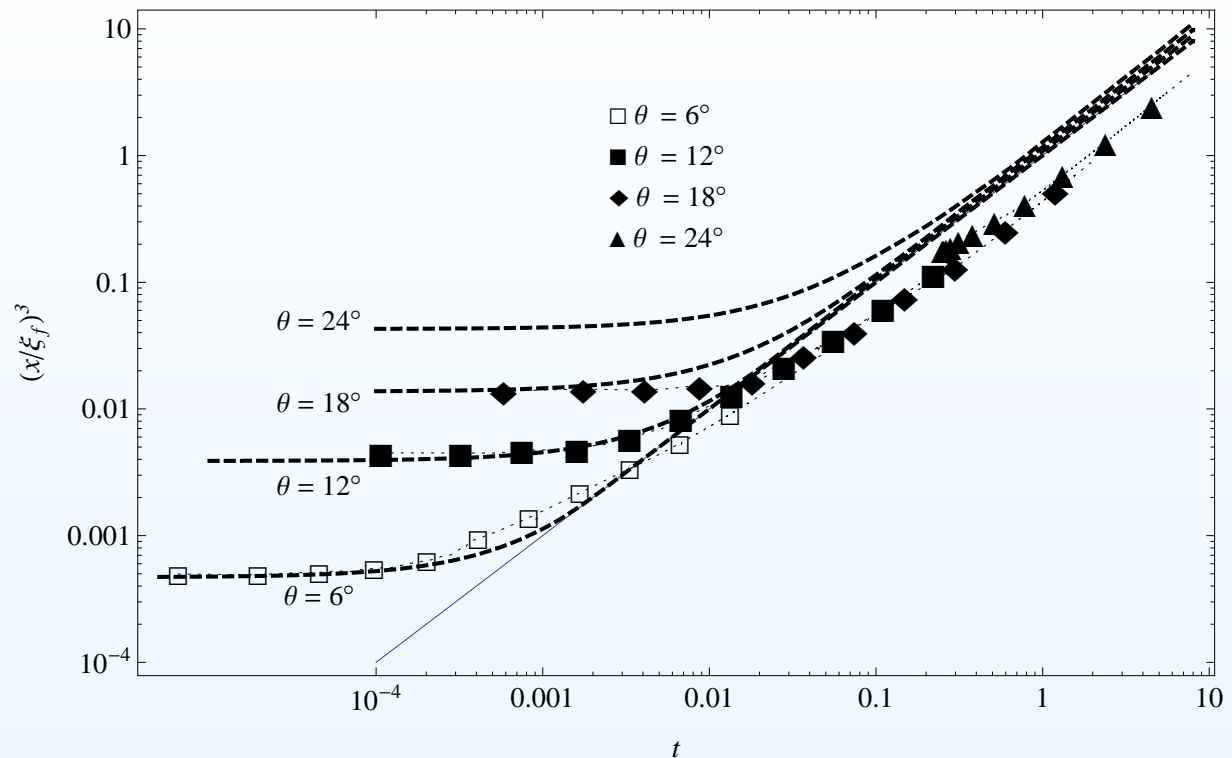
Newtonian fluids

- The dam-break problem
- Navier-Stokes equations
- Flow regimes
- Diffusive regime
- Diffusive regime at $t \ll 1$
- Diffusive regime at $t \gg 1$
- Comparison with experiments

Viscoplastic material

Concentrated particle suspension

Conclusions



Front position over time for slopes ranging from 6° to 24°

Introduction

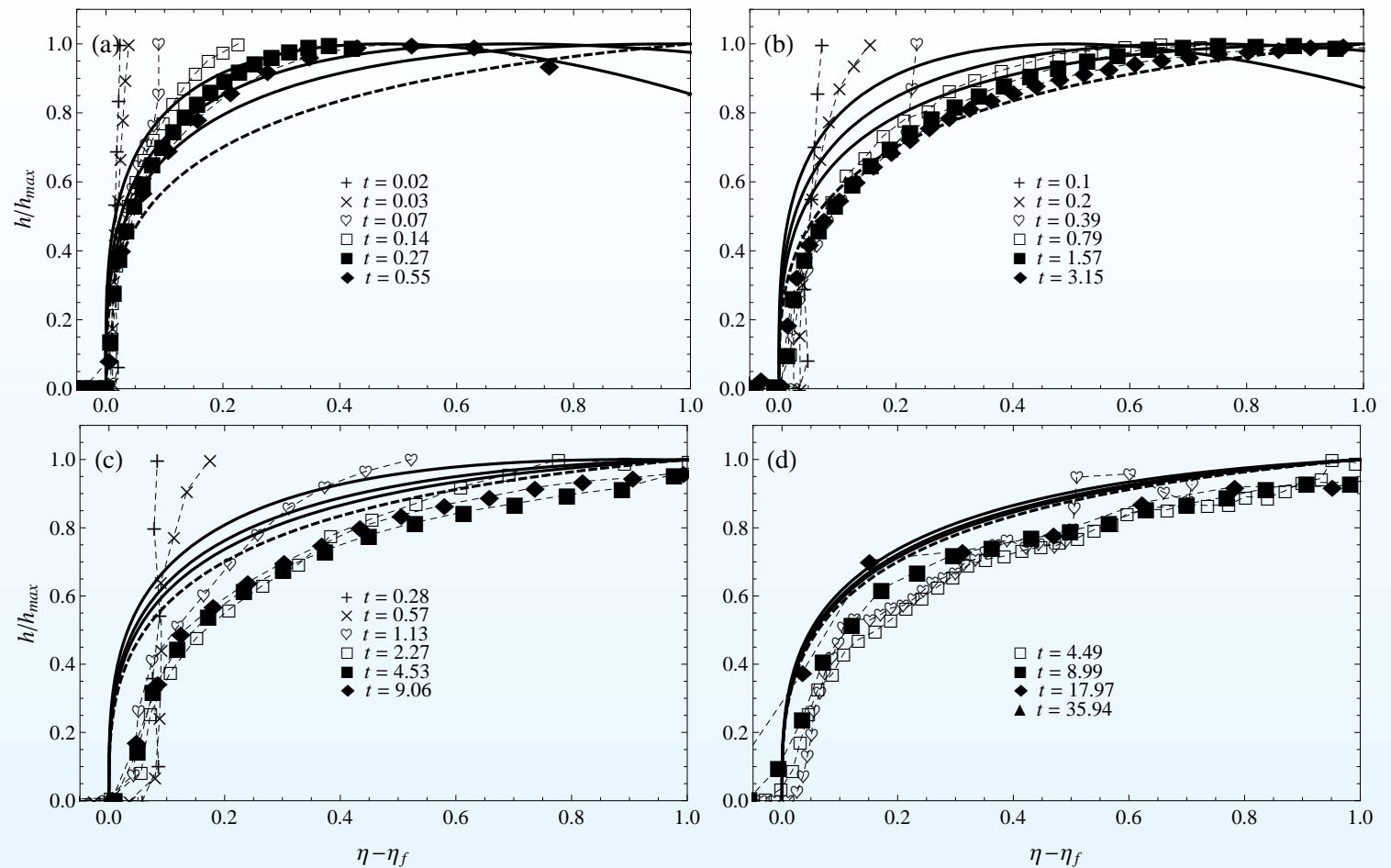
Newtonian fluids

- The dam-break problem
- Navier-Stokes equations
- Flow regimes
- Diffusive regime
- Diffusive regime at $t \ll 1$
- Diffusive regime at $t \gg 1$
- Comparison with experiments

Viscoplastic material

Concentrated particle suspension

Conclusions



Flow depth profiles for slopes ranging from 6° to 24° and different slopes

Introduction

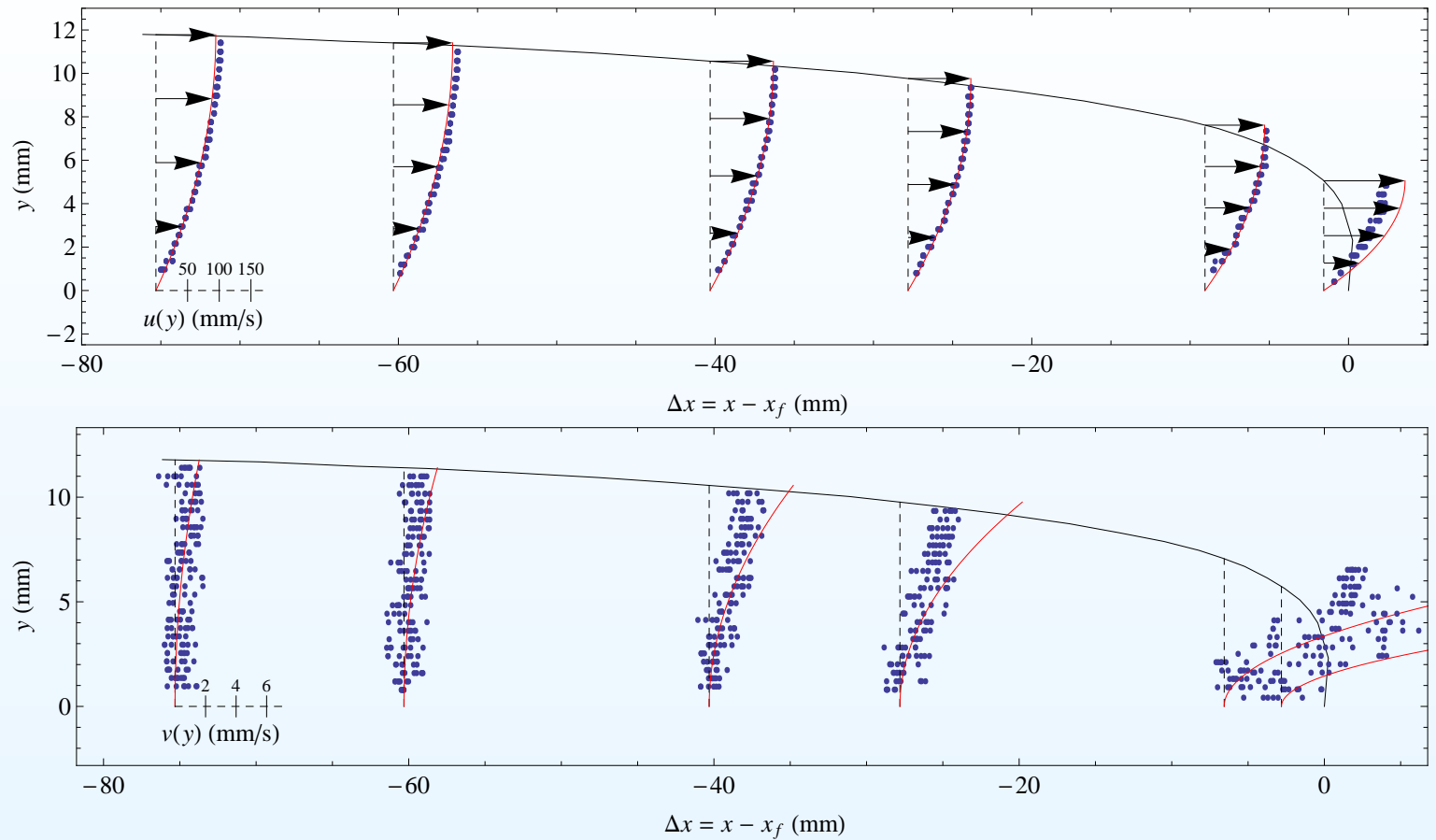
Newtonian fluids

- The dam-break problem
- Navier-Stokes equations
- Flow regimes
- Diffusive regime
- Diffusive regime at $t \ll 1$
- Diffusive regime at $t \gg 1$
- Comparison with experiments

Viscoplastic material

Concentrated particle suspension

Conclusions



Velocity profiles (u and v) in glycerol ($\mu = 1.11$ Pa s) for a 6° slope

Viscoplastic material

Simple shear constitutive law

$$\mu \dot{\gamma}^n = \begin{cases} \tau - \tau_c & \text{for } \tau > \tau_c, \\ 0 & \text{for } \tau \leq \tau_c, \end{cases}$$

Velocity profile for $y \leq Y_0$ or $y > Y_0$ (Liu & Mei, 1990)

$$u(x, y, t) = \begin{cases} \frac{n}{n+1} K \left(Y_0^{1+1/n} - (Y_0 - y)^{1+1/n} \right) \left(1 - \cot \theta \frac{\partial h}{\partial x} \right) \\ \frac{n}{n+1} K \left(1 - \cot \theta \frac{\partial h}{\partial x} \right) Y_0^{1+1/n}, \end{cases}$$

where $Y_0 = \max(0, h - \tau_c / (\rho g \cos \theta (\tan \theta - \partial_x h)))$ denotes the position of the yield surface and $K = \rho g \sin \theta / \mu$.

Introduction

Newtonian fluids

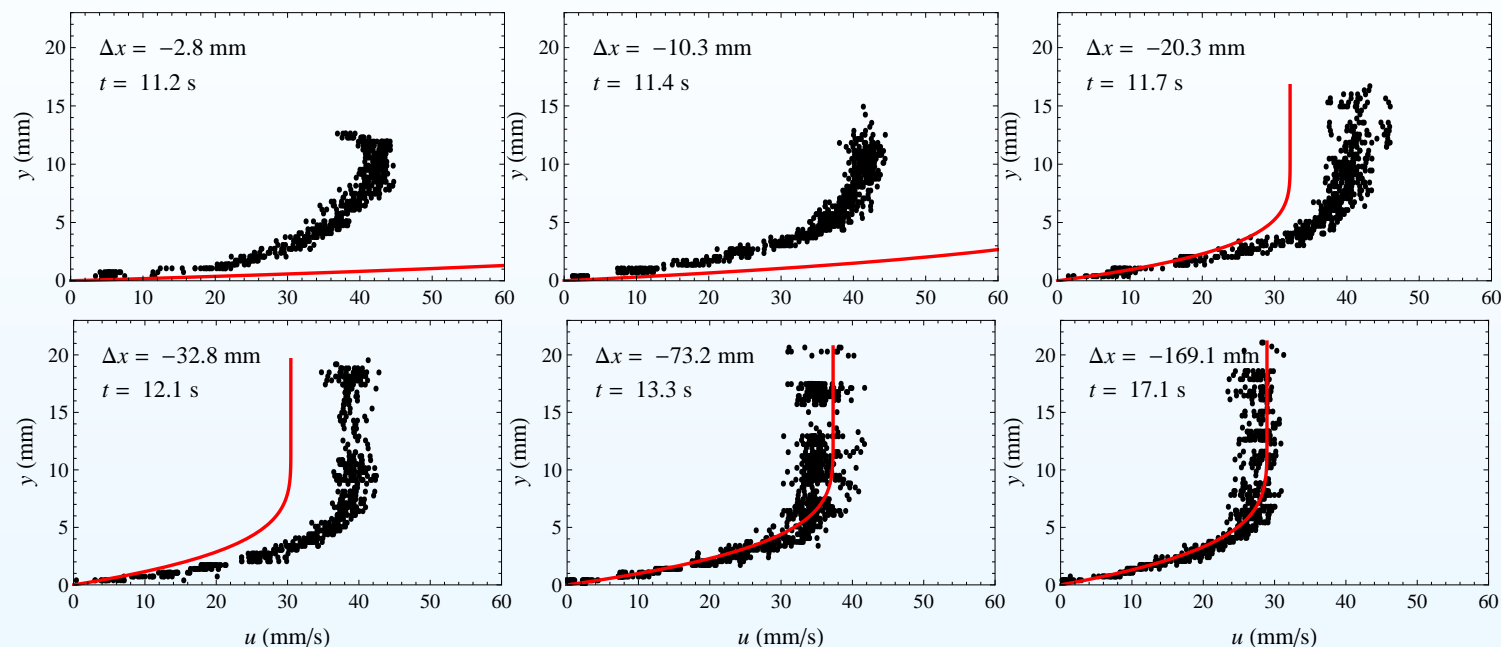
Viscoplastic material

- Viscoplastic material
- Comparison with experiments
- Flow models
- Kinematic wave model
- Diffusive wave equation
- Saint-Venant model

Concentrated particle suspension

Conclusions

Comparison with experiments



Comparison of the velocity profiles for $\theta = 25^\circ$ at different distances Δx to the front. Fluid: Carbopol ultrez 10 ($\mu = 26 \text{ Pa s}^n$, $n = 0.33$, $\tau_c = 33 \text{ Pa}$)

Introduction

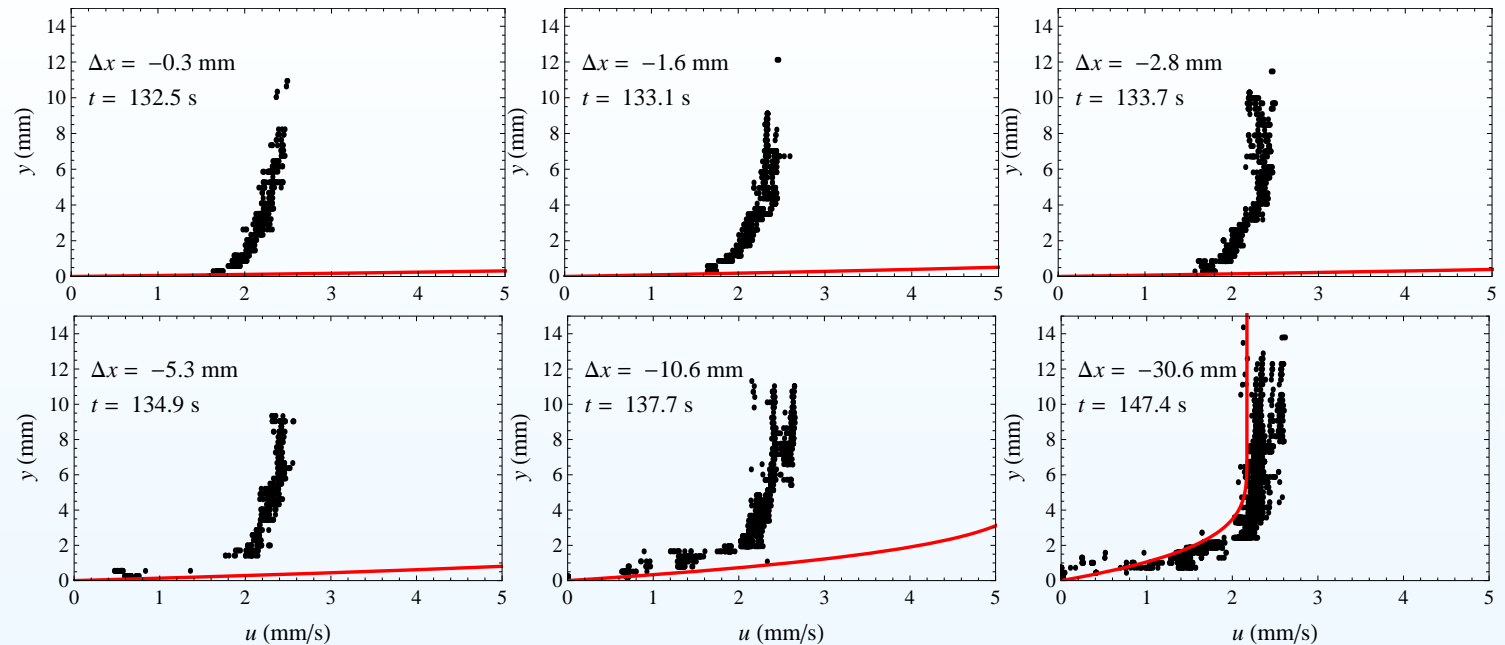
Newtonian fluids

Viscoplastic material

- Viscoplastic material
- Comparison with experiments
- Flow models
- Kinematic wave model
- Diffusive wave equation
- Saint-Venant model

Concentrated particle suspension

Conclusions



Comparison of the velocity profiles for $\theta = 15^\circ$ at different distances to the front. Fluid: Carbopol ultrez 10 ($\mu = 26 \text{ Pa s}^n$, $n = 0.33$, $\tau_c = 33 \text{ Pa}$)

- Viscoplastic material
- Comparison with experiments
- **Flow models**
- Kinematic wave model
- Diffusive wave equation
- Saint-Venant model

Flow models

Dimensionless depth-averaged equations (e.g. Craster & Mater, 2009)

$$\frac{\partial h}{\partial t} + \frac{\partial h\bar{u}}{\partial x} = 0,$$

$$\epsilon Re \left(\frac{\partial h\bar{u}}{\partial t} + \beta \frac{\partial h\bar{u}^2}{\partial x} \right) + \epsilon \cot \theta h \frac{\partial h}{\partial x} = h - \tau_b + \frac{\epsilon^3}{Ca} h \frac{\partial^3 h}{\partial x^3}.$$

Several simplifications developed:

- kinematic wave model (Huang & Garcia, 1994): balance between the driving and ‘viscous’ forces;
- diffusive wave model: balance between the driving and ‘viscous’ forces + pressure gradient;
- Saint-Venant model: in the limit of $Ca \rightarrow \infty$ and $\epsilon \ll 1$, with a closure equation for τ_b .

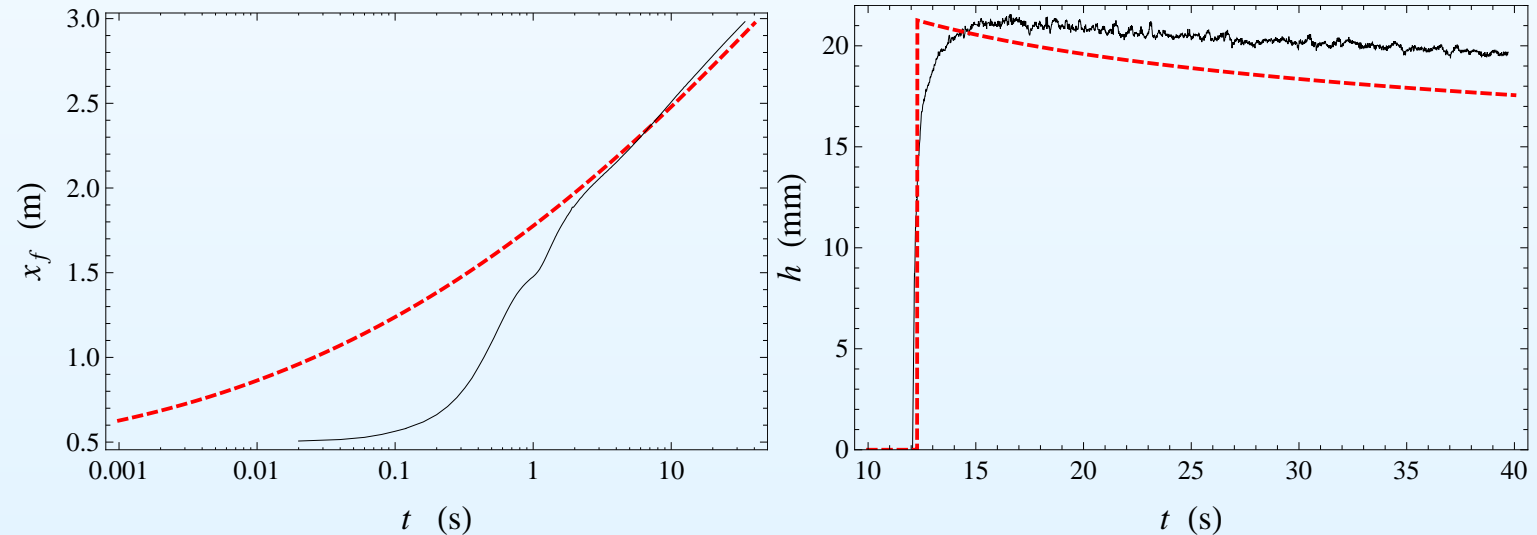
- Viscoplastic material
- Comparison with experiments
- Flow models
- Kinematic wave model
- Diffusive wave equation
- Saint-Venant model

Kinematic wave model

A simple nonlinear advection equation (hyperbolic)

$$\frac{\partial h}{\partial t} + \frac{\partial h\bar{u}}{\partial x} = 0$$

Analytical solutions (using the method of characteristics) in an implicit form.
For a 25° slope



Introduction

Newtonian fluids

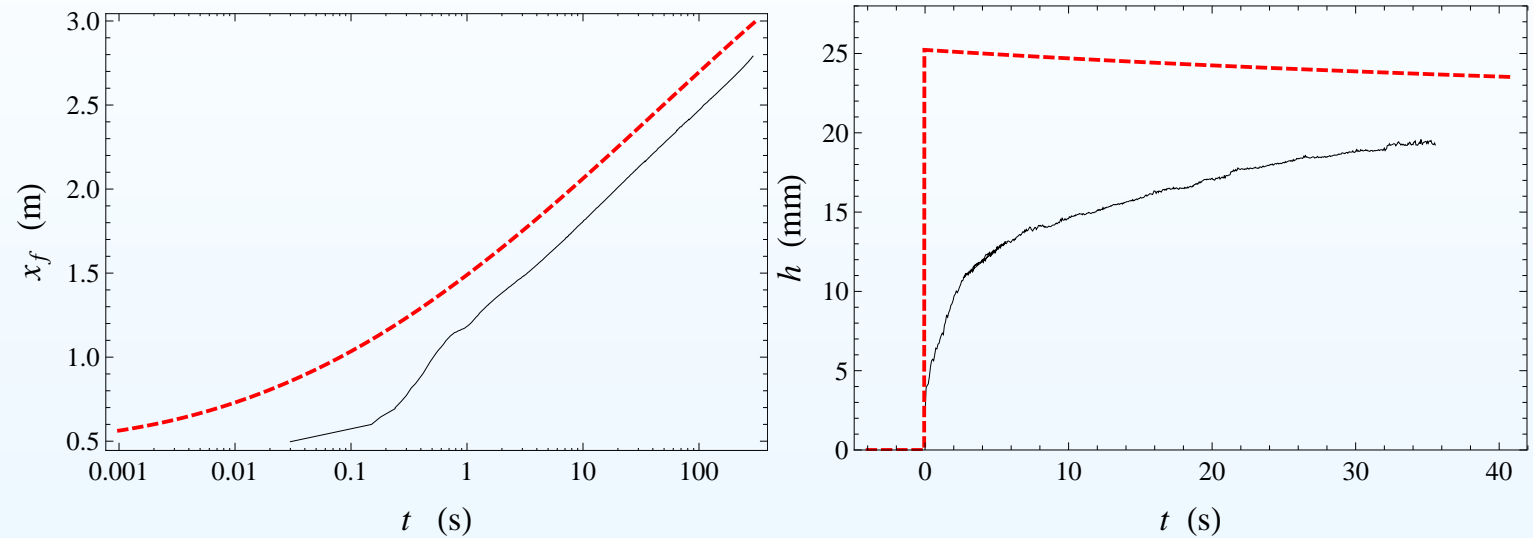
Viscoplastic material

- Viscoplastic material
- Comparison with experiments
- Flow models
- **Kinematic wave model**
- Diffusive wave equation
- Saint-Venant model

Concentrated particle suspension

Conclusions

For a 15° slope



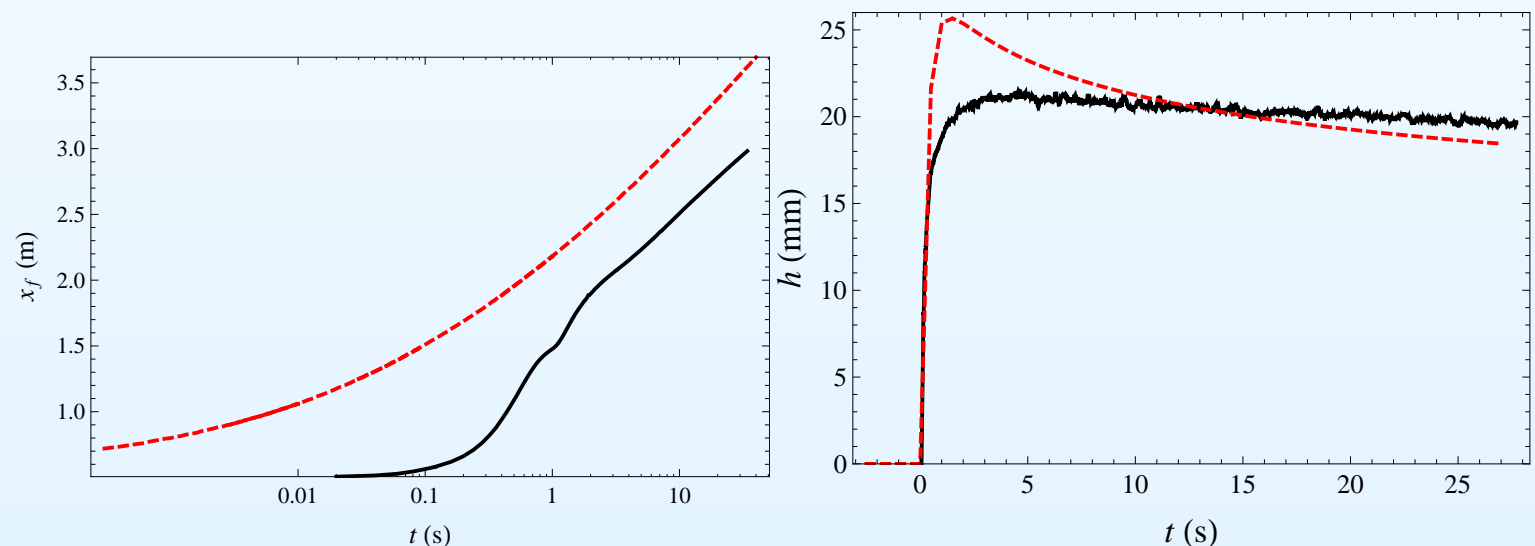
Diffusive wave equation

A nonlinear advection-diffusion equation (parabolic)

$$\frac{\partial h}{\partial t} + nK \frac{\partial}{\partial x} \left[\left(\tan \theta - \frac{\partial h}{\partial x} \right)^{1/n} \frac{h(1+n) + nh_c}{(n+1)(2n+1)} Y_0^{1+1/n} \right] = 0$$

No analytical solution.

For a 25° slope



Introduction

Newtonian fluids

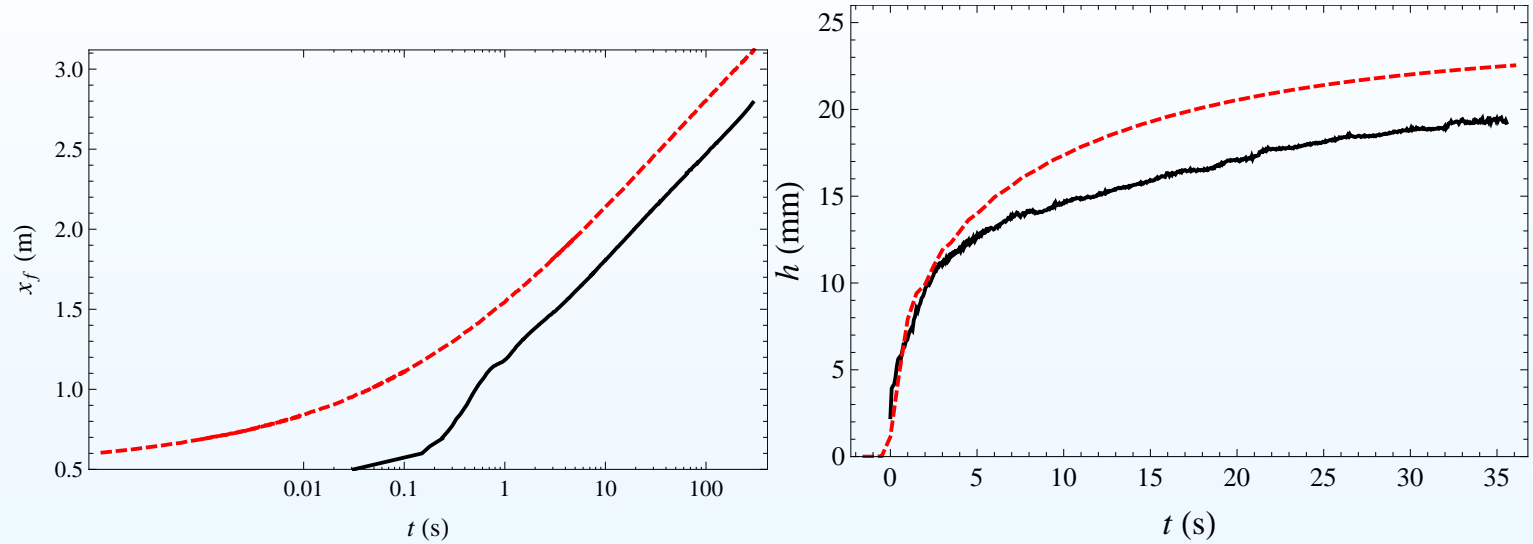
Viscoplastic material

- Viscoplastic material
- Comparison with experiments
- Flow models
- Kinematic wave model
- Diffusive wave equation
- Saint-Venant model

Concentrated particle suspension

Conclusions

For a 15° slope



- Viscoplastic material
- Comparison with experiments
- Flow models
- Kinematic wave model
- Diffusive wave equation

Saint-Venant model

Hyperbolic partial differential equations

$$\begin{aligned}\frac{\partial h}{\partial t} + \frac{\partial h\bar{u}}{\partial x} &= 0, \\ \frac{\partial h\bar{u}}{\partial t} + \frac{\partial h\bar{u}^2}{\partial x} + gh \cos \theta \frac{\partial h}{\partial x} &= gh \sin \theta - \frac{\tau_b}{\rho},\end{aligned}$$

Coussot's closure equation:

$$\tau_b = \tau_c \left(1 + 1.93 G^{3/10} \right) \text{ with } G = \left(\frac{\mu}{\tau_c} \right)^3 \frac{\bar{u}}{h}$$

Introduction

Newtonian fluids

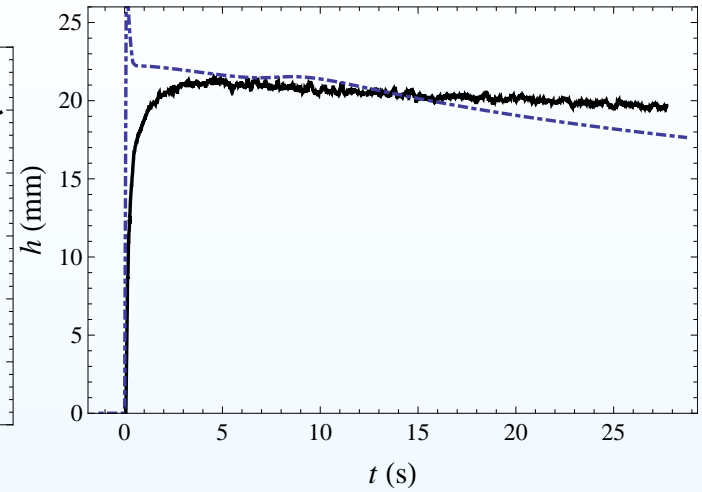
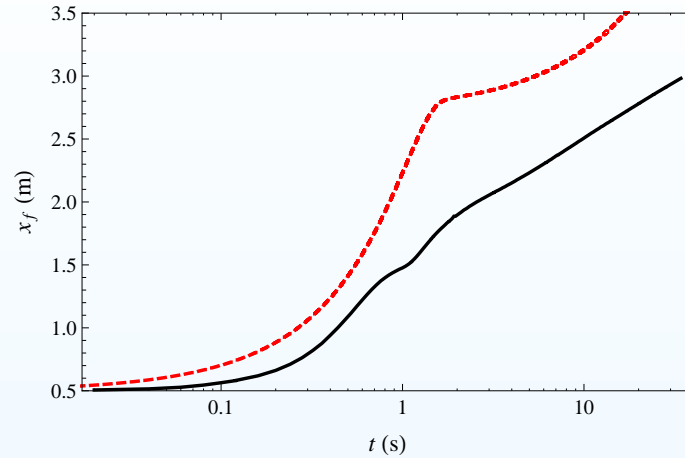
Viscoplastic material

- Viscoplastic material
- Comparison with experiments
- Flow models
- Kinematic wave model
- Diffusive wave equation
- Saint-Venant model

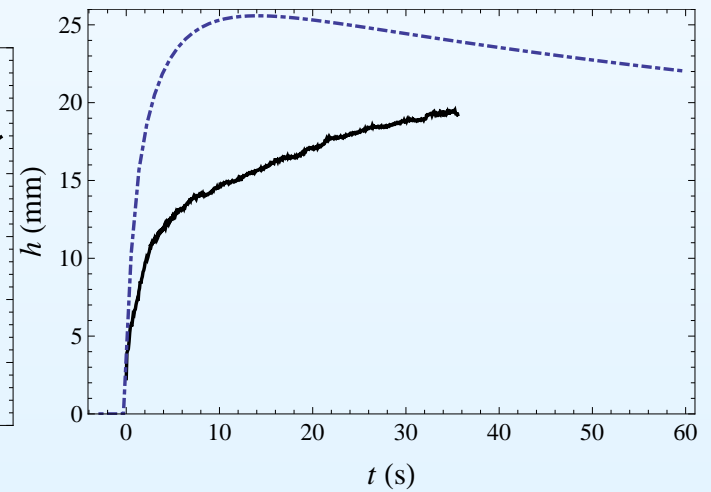
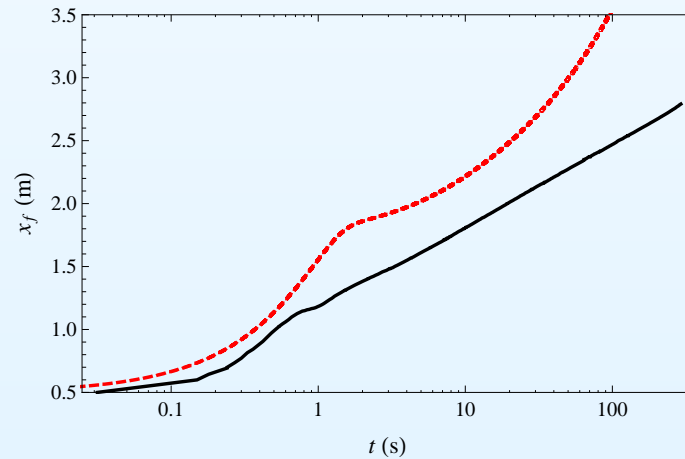
Concentrated particle suspension

Conclusions

For a 25° slope



For a 15° slope



Scientific issues

A density-matched suspension of particles within a Newtonian carrier fluid is assumed to be quasi-Newtonian:

- effective viscosity given by empirical laws, e.g.,

$$\eta(\phi) = \frac{\mu(\phi)}{\mu_f} = \left(1 - \frac{\phi}{\phi_m}\right)^{-\beta}$$

ϕ_m the maximum concentration and β a constant : $\beta = \frac{5}{2}\phi_m$ or $\beta = 2$ (Krieger & Dougherty 1959)

- occurrence of normal stress effects (Zarraga *et al.* JOR, 2001 ; Boyer *et al.* JFM 2001 ; Couturier *et al.* JFM 2011)

Problem: particle migration occurs even for $\Delta\rho = 0$ (effect exacerbated when sedimentation or creaming occurs, depending on $\Delta\rho > 0$ or $\Delta\rho < 0$), so this results in a nonhomogeneous spatial distribution of the particles, thus viscosity.

- Scientific issues
- **Particle migration**
- Shear-induced migration
- Solution for steady state uniform flows
- Solution for time-dependent flows
- Comparison with experiments
- Behaviour at the highest concentrations
- Stick-slip regime
- Experiments

Particle migration

Migration: stratification of particles as a result of shear. Two approaches:

- Phenomenological model developed by Leighton & Acrivos (JFM 1987)

$$\mathbf{j} \propto -\phi^2 \nabla \dot{\gamma} \text{ avec } \mathbf{j} = \phi(\mathbf{u}^p - \mathbf{u})$$

the particle flux relative to the bulk velocity

- Microstructural approach by Nott & Brady (JFM 1994) and Morris & Boulay (JOR 1999)

$$\mathbf{j} \propto -\nabla \cdot \Sigma^p$$

The theoretical underpinning is still disputed (Lhuillier PoF 2009; Nott et al. PoF 2011).

Respective merits subject of fierce debate... with no winner

- Scientific issues
- Particle migration
- **Shear-induced migration**
- Solution for steady state uniform flows
- Solution for time-dependent flows
- Comparison with experiments
- Behaviour at the highest concentrations
- Stick-slip regime
- Experiments

Shear-induced migration

Phillips et al.'s model (PoF 1992) in a dimensionless form

$$\mathbf{j} = -\phi K_c \frac{\epsilon_a^2}{\epsilon} \nabla(\phi \dot{\gamma}) - K_\mu \dot{\gamma} \phi^2 \frac{\epsilon_a^2}{\epsilon} \frac{d \ln \eta}{d\phi} \nabla \phi,$$

Two processes at play:

- diffusion of particles resulting from the anisotropy in the probability of encounter between two particles,
- Fick-like diffusion

Nonlinear advection diffusion equation for ϕ

$$\frac{\partial \phi}{\partial t} + u \frac{\partial \phi}{\partial x} + v \frac{\partial \phi}{\partial y} = -\nabla \cdot \mathbf{j}.$$

- Scientific issues
- Particle migration
- Shear-induced migration
- **Solution for steady state uniform flows**
- Solution for time-dependent flows
- Comparison with experiments
- Behaviour at the highest concentrations
- Stick-slip regime
- Experiments

Solution for steady state uniform flows

With $\beta = 2$ and $\alpha = 3/2$ (otherwise the solution is implicit), one gets the quasi-explicit solution

$$\phi = \frac{\phi_w h}{\phi_m h - (\phi_m - \phi_w)y} \quad \text{with} \quad \frac{\phi_w}{\phi_m - \phi_w} \log \frac{\phi_m}{\phi_w} = \bar{\phi}$$

By integrating the conservation of momentum

$$\dot{\gamma} = \frac{\bar{\eta}}{\eta(\phi)} (h - y),$$

we determine velocity profiles numerically. They take the form

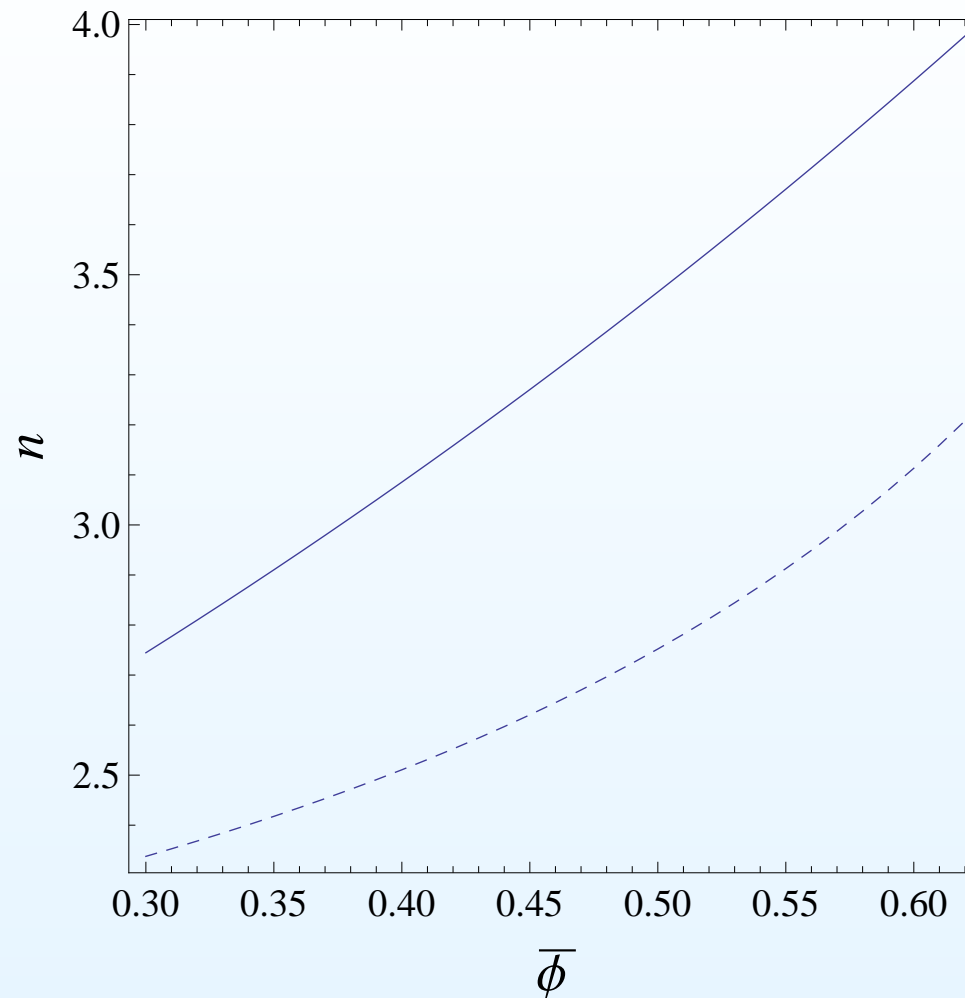
$$u = \kappa (h^n - (h - y)^n)$$

$n = 2$ for a Newtonian fluid. Another index to characterise the deviation of the computed velocity profile from the Newtonian profile ($m = 2/3$)

$$m = \frac{\int_0^h u(y, t) dy}{h u(h, t)} = \frac{\bar{u}}{u(h, t)},$$

- Scientific issues
- Particle migration
- Shear-induced migration
- **Solution for steady state uniform flows**
- Solution for time-dependent flows
- Comparison with experiments
- Behaviour at the highest concentrations
- Stick-slip regime
- Experiments

Variation of n with the particle concentration



Two parameter sets: $\beta = 2$ and $\alpha = 3/2$ (solid line) ; $\beta = 2$ and $\alpha = 1.042\bar{\phi} + 0.1142$ (dashed line) using the model proposed by Tetlow *et al.* (JOR 1998)

- Scientific issues
- Particle migration
- Shear-induced migration
- Solution for steady state uniform flows
- **Solution for time-dependent flows**
- Comparison with experiments
- Behaviour at the highest concentrations
- Stick-slip regime
- Experiments

Solution for time-dependent flows

Using the assumption $\partial_x \phi = 0$

$$\frac{\partial \phi}{\partial t} = K_c \bar{\eta} \frac{\epsilon_a^2}{\epsilon} \frac{\partial}{\partial y} \left(\phi \frac{\partial}{\partial y} \left(\frac{\phi}{\eta(\phi)} (h - y) \right) + \alpha \frac{\phi^2}{\eta(\phi)} (h - y) \frac{d \ln \eta}{d \phi} \frac{\partial \phi}{\partial y} \right).$$

Steady state is reached at time

$$t_c \sim \frac{\epsilon}{\epsilon_a^2} = \frac{H_*^3}{a^2 L_*}$$

Numerically one gets

$$t_{ss} = 2t_c \left(1 - \frac{\phi}{\phi_m} \right)^{-1/3}$$

Introduction

Newtonian fluids

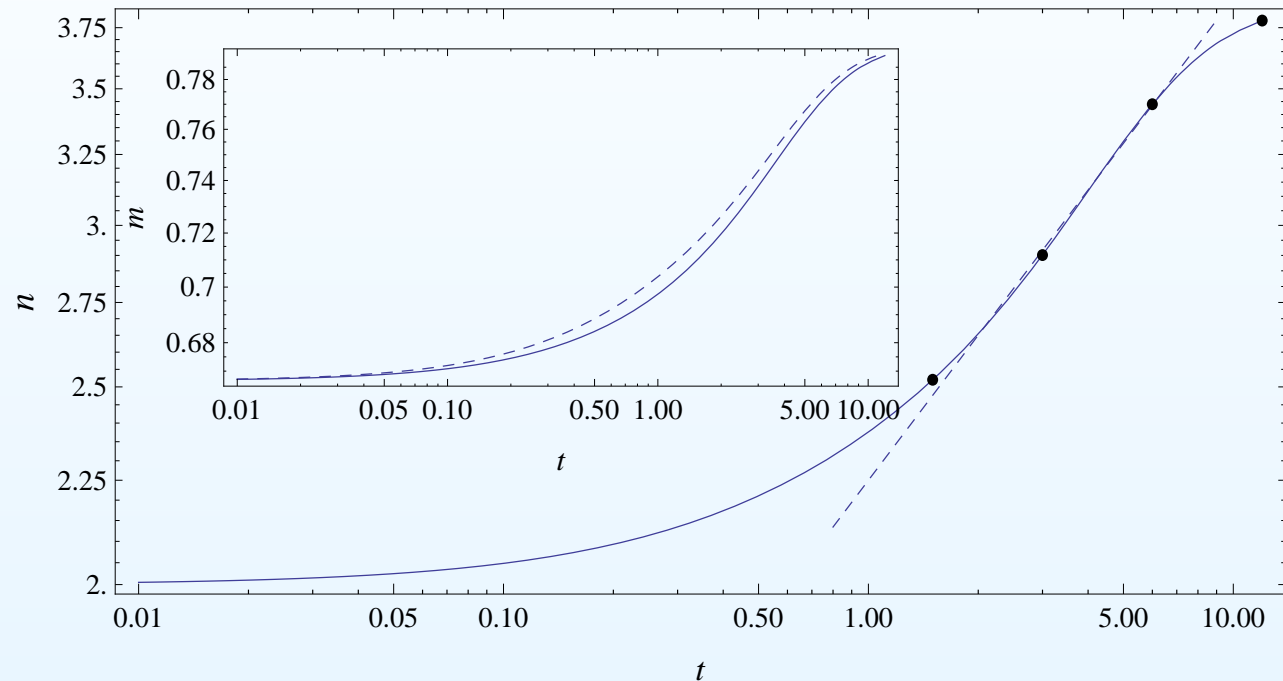
Viscoplastic material

Concentrated particle suspension

- Scientific issues
- Particle migration
- Shear-induced migration
- Solution for steady state uniform flows
- **Solution for time-dependent flows**
- Comparison with experiments
- Behaviour at the highest concentrations
- Stick-slip regime
- Experiments

Conclusions

Variation of n (and m) at short times

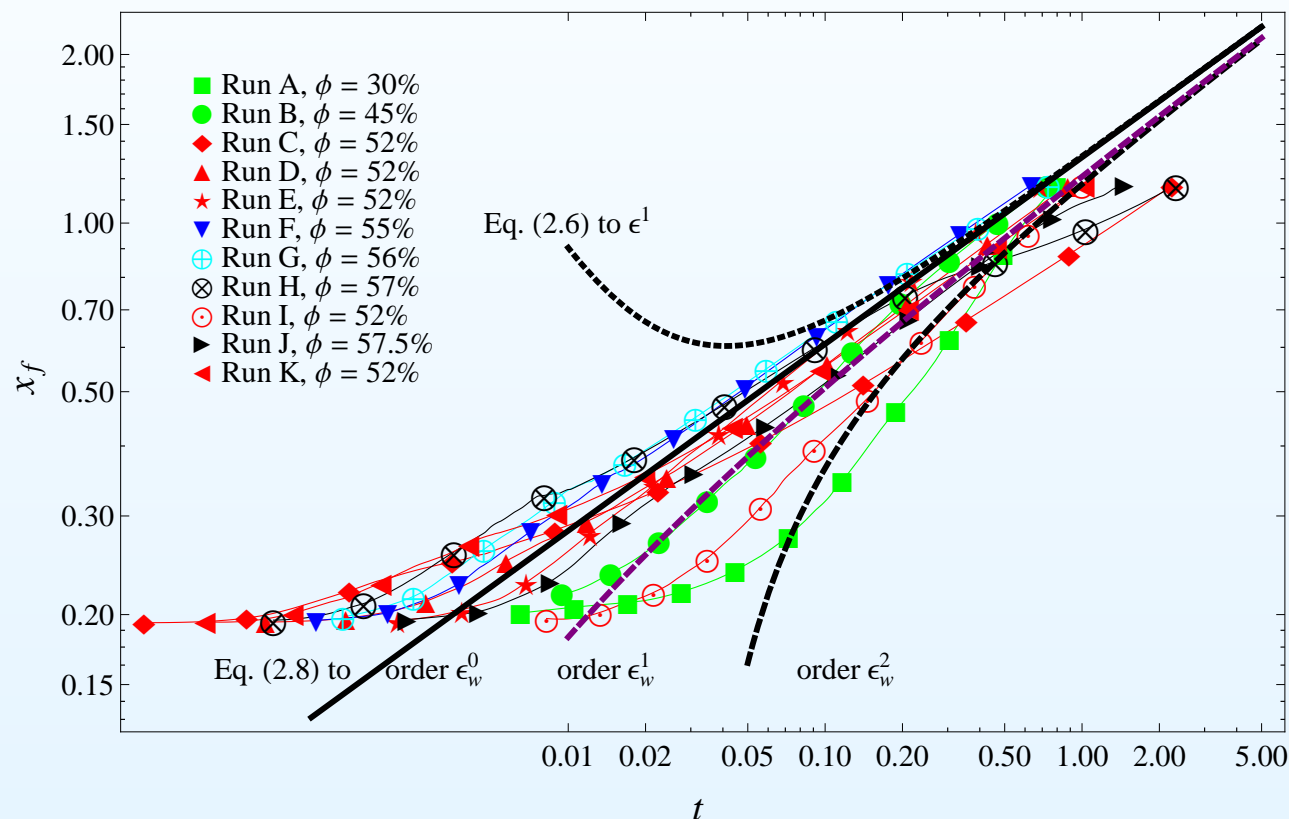


Trend $n = 2.2t^{1/4}$. Computations done for $\bar{\phi} = 52\%$, $K_c \bar{\eta} \epsilon_a^2 / \epsilon = 1$, $\beta = 2$, and $\alpha = 3/2$. Computed steady state time: $t_{ss} = 3.56$.

- Scientific issues
- Particle migration
- Shear-induced migration
- Solution for steady state uniform flows
- Solution for time-dependent flows
- Comparison with experiments
- Behaviour at the highest concentrations
- Stick-slip regime
- Experiments

Comparison with experiments

Variation of $x_f(t)$ (dimensionless)



For a 25° slope

Introduction

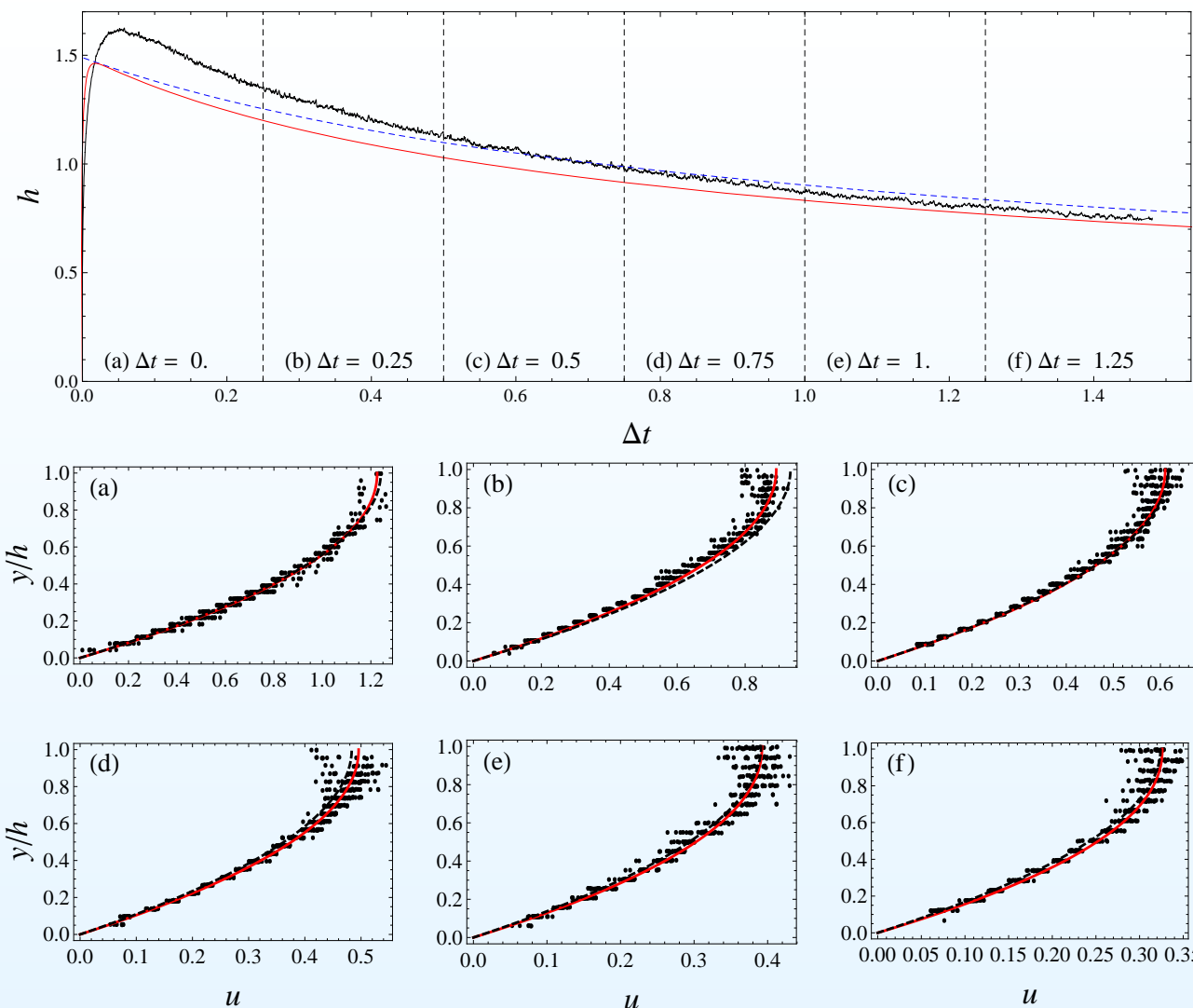
Newtonian fluids

Viscoplastic material

Concentrated particle suspension

- Scientific issues
- Particle migration
- Shear-induced migration
- Solution for steady state uniform flows
- Solution for time-dependent flows
- Comparison with experiments
- Behaviour at the highest concentrations
- Stick-slip regime
- Experiments

Conclusions



For a 25° slope, but $\phi = 0.45$

Introduction

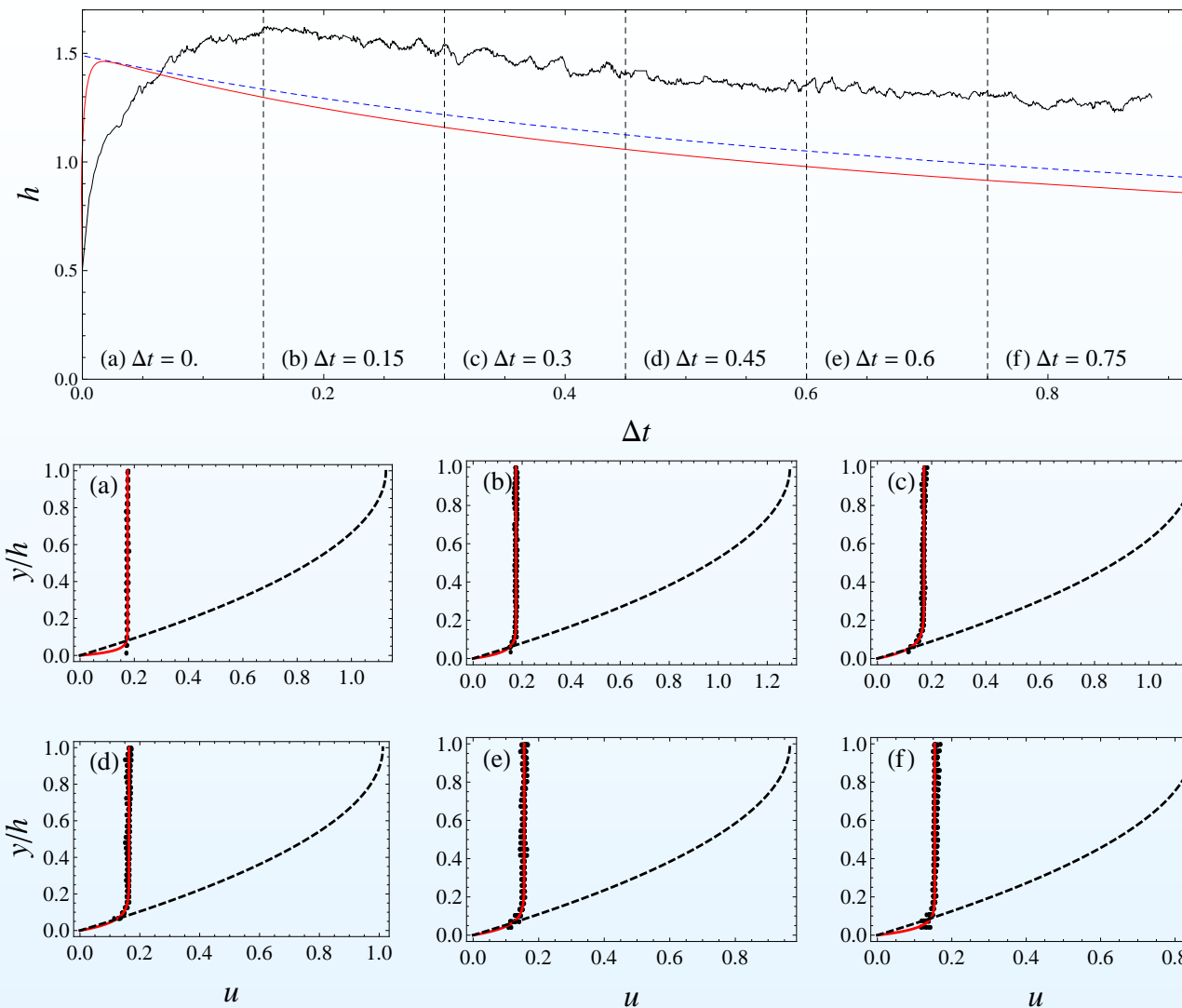
Newtonian fluids

Viscoplastic material

Concentrated particle suspension

- Scientific issues
- Particle migration
- Shear-induced migration
- Solution for steady state uniform flows
- Solution for time-dependent flows
- **Comparison with experiments**
- Behaviour at the highest concentrations
- Stick-slip regime
- Experiments

Conclusions



For a 25° slope, but $\phi = 0.57$

Introduction

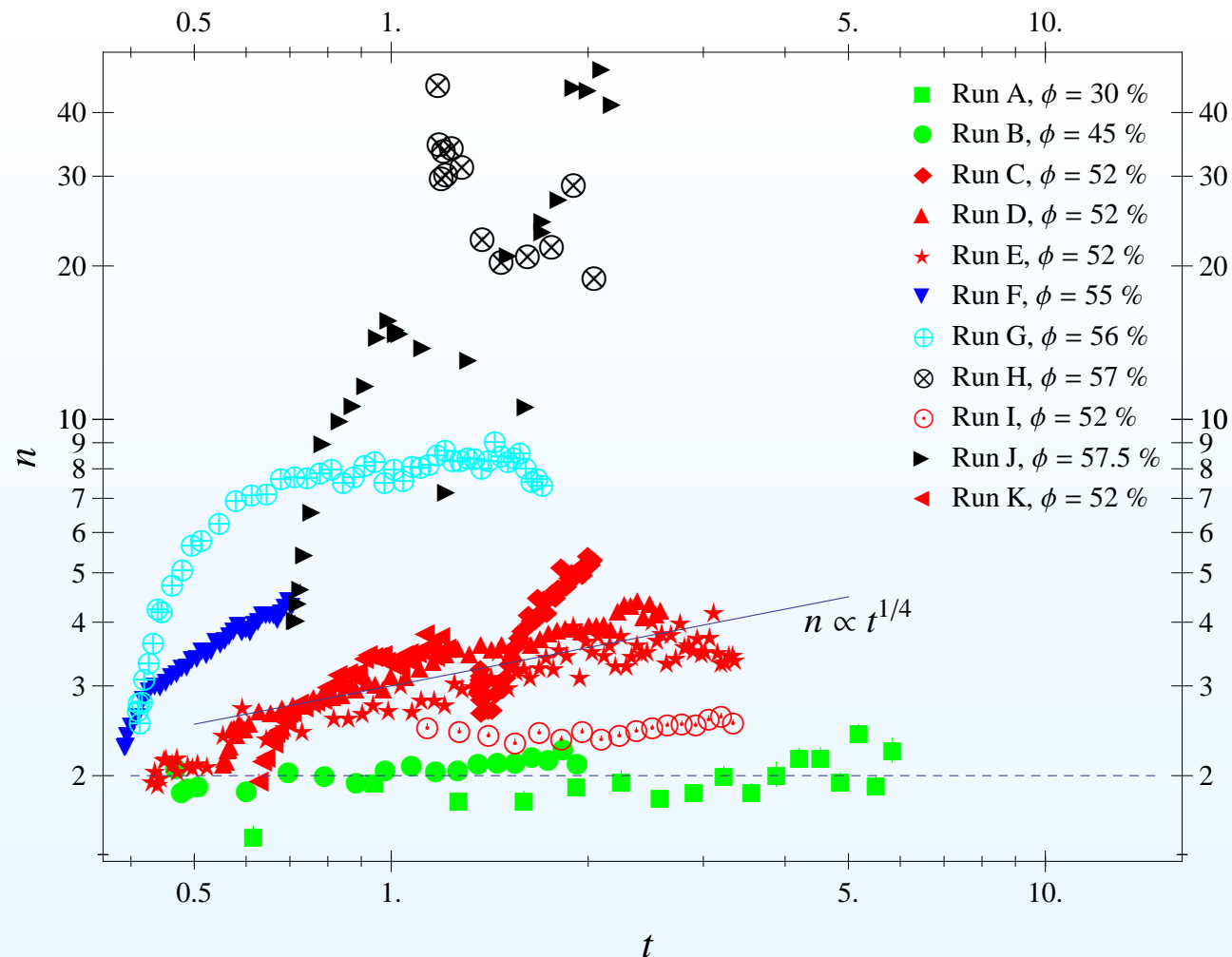
Newtonian fluids

Viscoplastic material

Concentrated particle suspension

- Scientific issues
- Particle migration
- Shear-induced migration
- Solution for steady state uniform flows
- Solution for time-dependent flows
- Comparison with experiments
- Behaviour at the highest concentrations
- Stick-slip regime
- Experiments

Conclusions



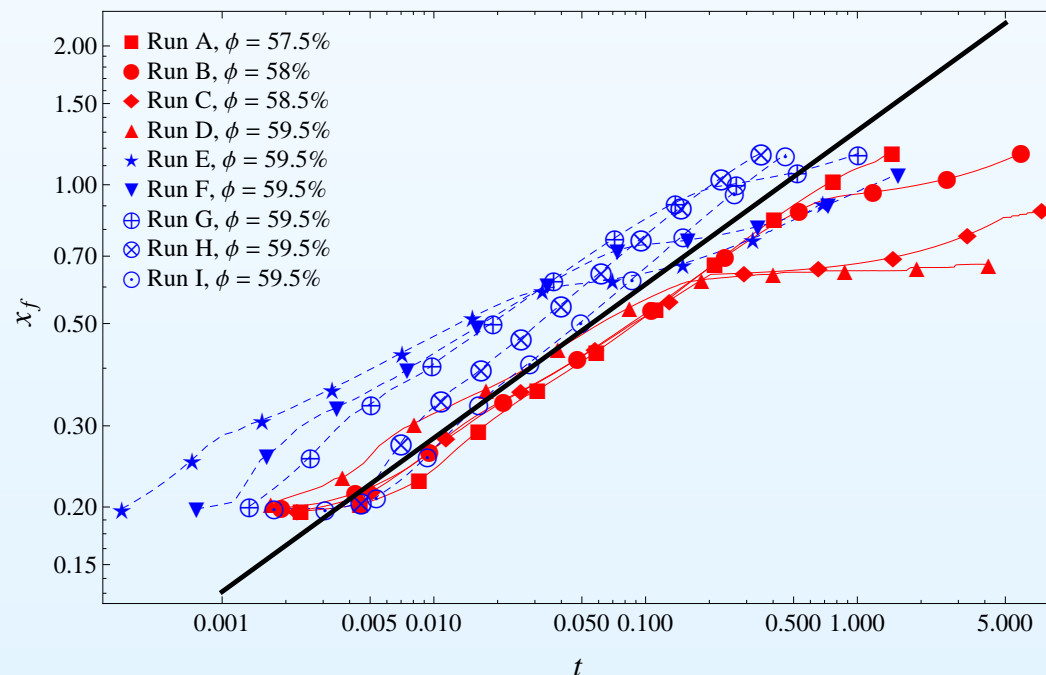
Variation of n with time (dimensionless)

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- Particle migration
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- Behaviour at the highest concentrations
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Behaviour at the highest concentrations

For $\phi > 0.575$, behaviour is complicated, with three phases observed:

- *macro-viscous regime* at short times: $x_f \propto t^{1/3}$, parabolic profile of u ,
- *fracture regime*: wavy free surface, fracture, and *en-masse* flow,
- *plastic regime*: intermittent motion (stick-slip).



Introduction

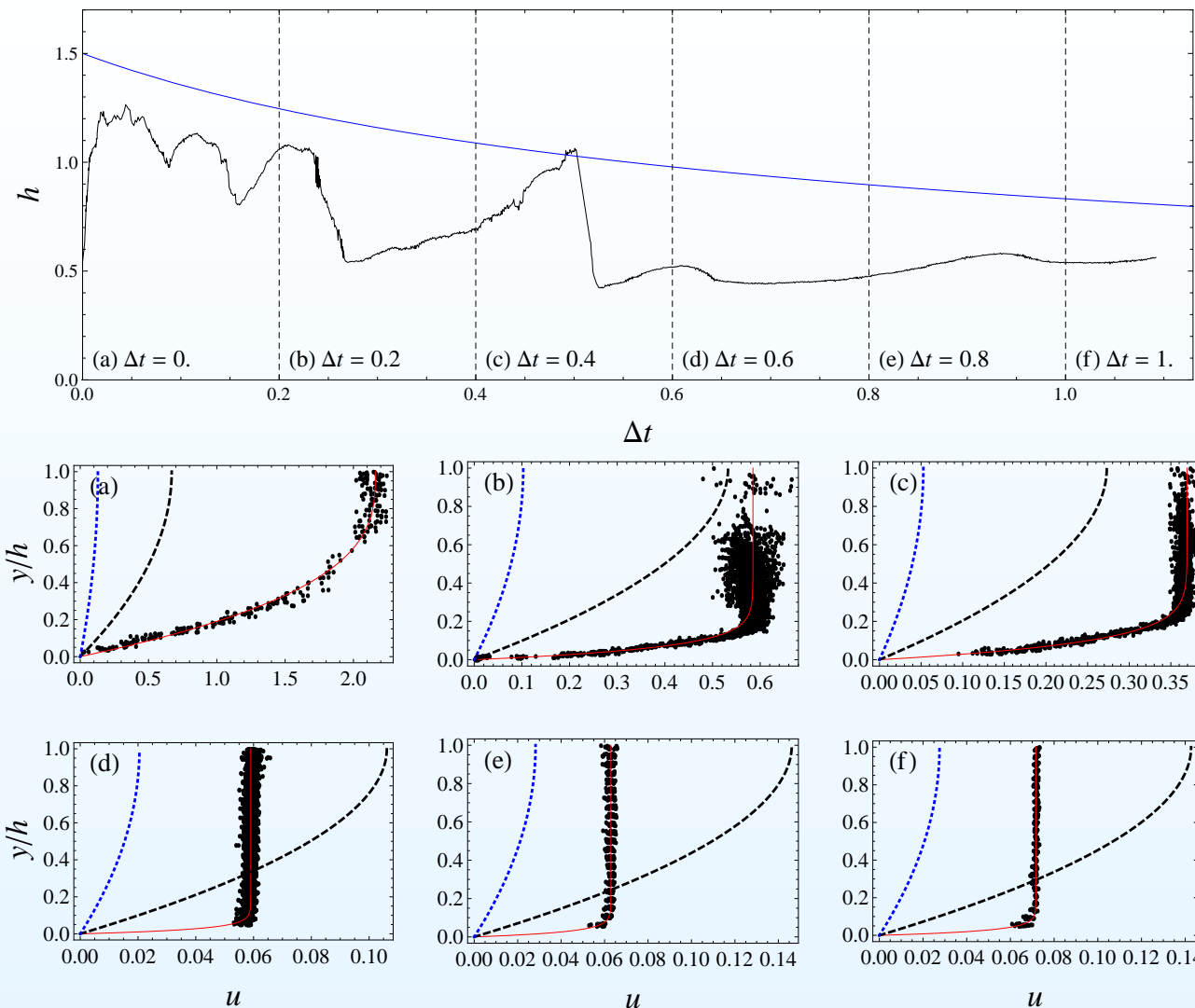
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Viscoplastic material

Concentrated particle suspension

- Scientific issues
- Particle migration
- Shear-induced migration
- Solution for steady state uniform flows
- Solution for time-dependent flows
- Comparison with experiments
- **Behaviour at the highest concentrations**
- Stick-slip regime
- Experiments

Conclusions



For 25° slope, $\phi = 0.595$

Stick-slip regime

Introduction

Newtonian fluids

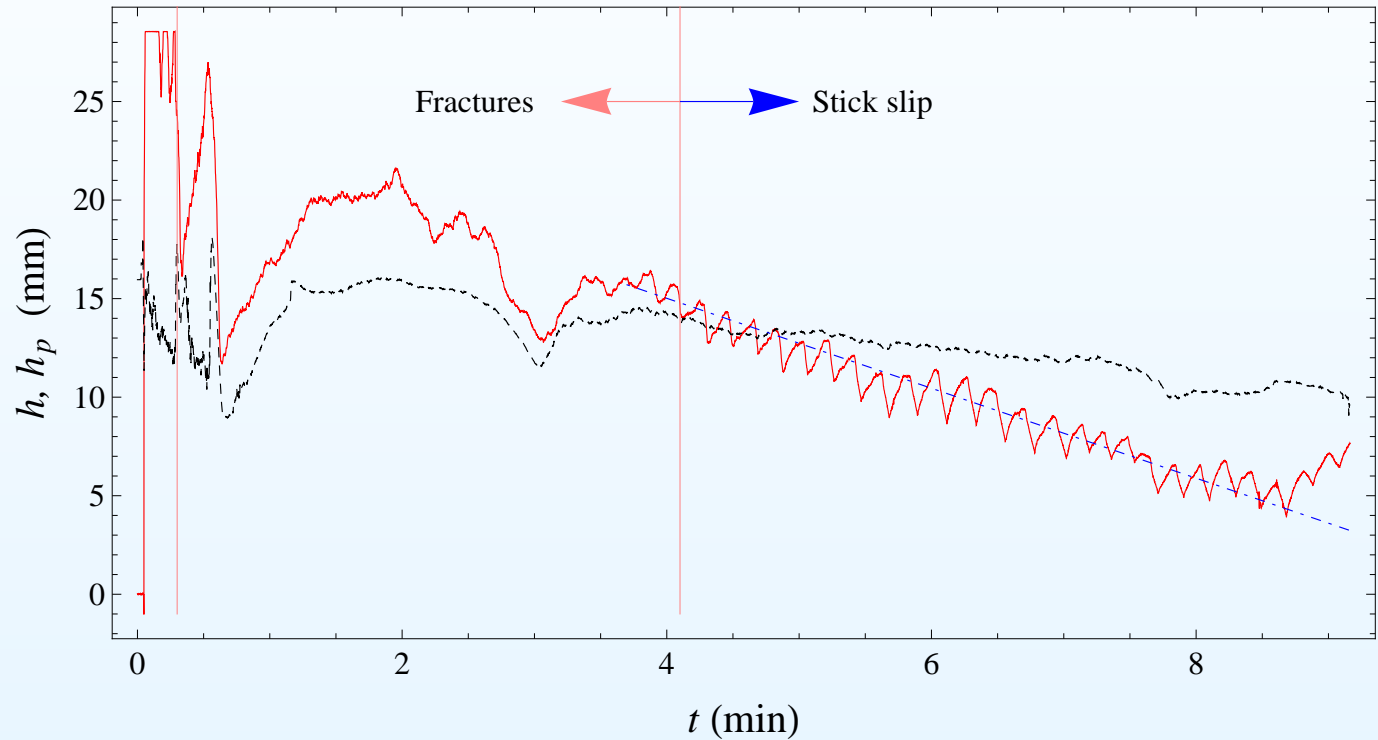
Viscoplastic material

Concentrated particle suspension

- Scientific issues
- Particle migration
- Shear-induced migration
- Solution for steady state uniform flows
- Solution for time-dependent flows
- Comparison with experiments
- Behaviour at the highest concentrations
- **Stick-slip regime**
- Experiments

Conclusions

Variation of the flow depth and the pressure 'head' $h_p = p/(\rho g \cos \theta)$



Experiments

Introduction

Newtonian fluids

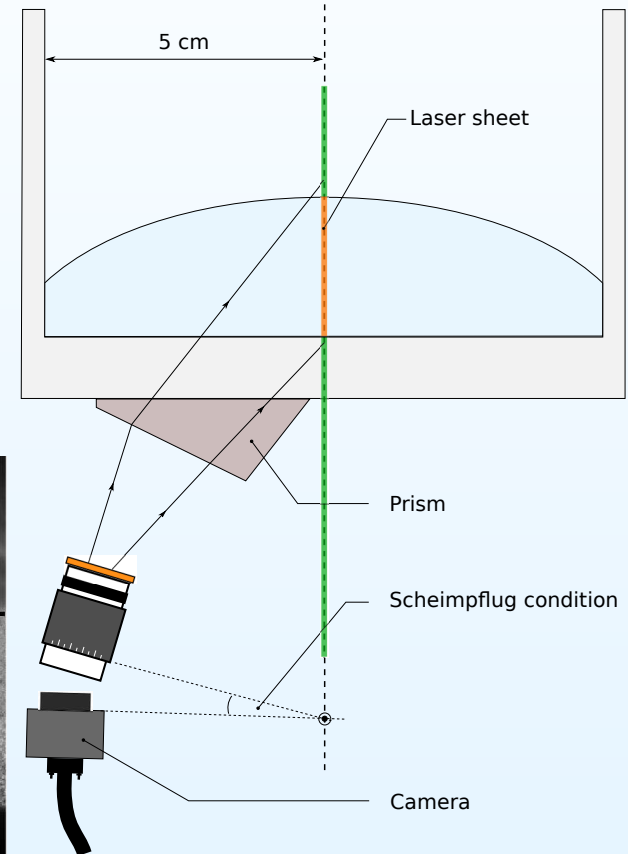
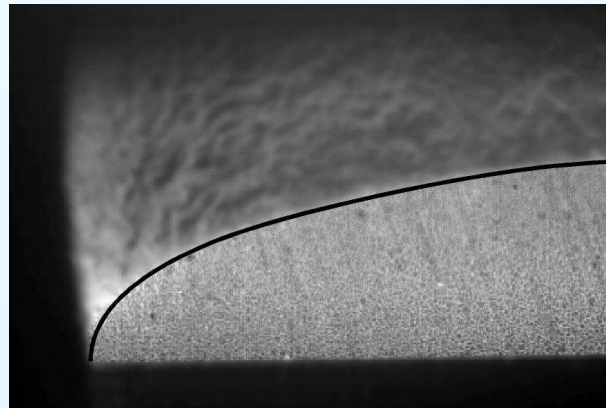
Viscoplastic material

Concentrated particle
suspension

- Scientific issues
- Particle migration
- Shear-induced migration
- Solution for steady state uniform flows
- Solution for time-dependent flows
- Comparison with experiments
- Behaviour at the highest concentrations
- Stick-slip regime
- **Experiments**

Conclusions

$$\phi = 0.56$$



Introduction

Newtonian fluids

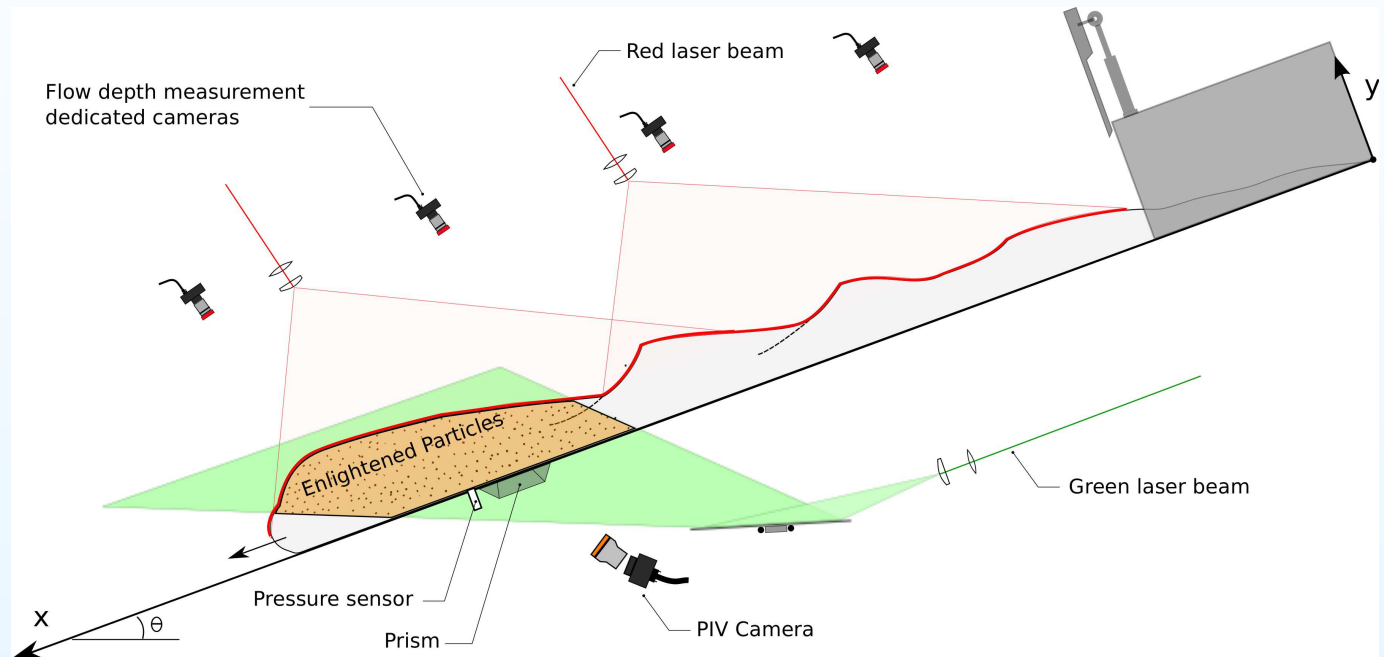
Viscoplastic material

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- Scientific issues
- Particle migration
- Shear-induced migration
- Solution for steady state uniform flows
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- **Experiments**

Conclusions

$$\phi = 0.595$$



Conclusions

The dam-break for different rheologies. Our main findings:

- For Newtonian fluids: fairly good agreement between theory/experiment.
- For viscoplastic fluids: the simplest models perform better than more elaborate models such as Saint-Venant.
- For granular suspensions: we observed *macro-viscous* behaviour for concentrations as high as $\phi = 0.57$, then for higher concentrations, complicated behaviour, including stick-slip motion (resulting from a pore-pressure diffusion mechanism that is still poorly understood).

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